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# Input-Output Modelling Based on Total-Use Rectangular Tables: Is this a Better Way?

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### abstract

resumo

Input-output tables can be presented in different formats, according to three main criteria: 1) symmetric or rectangular format; 2) total or domestic-use flows and 3) valuation prices (basic prices – bp or purchasers' prices - pp). Official National Accounts (at least in EU) produce in a regular base a total use rectangular table at pp – also known as the Make and Use (M&U) format – that is different from the lay-out upon which traditional inputoutput models were developed (domestic use, symmetric, bp). The problem with this latter one is of course that it is only available at times in many countries. The objective of this paper is to prove (under common hypotheses) the equivalence between two alternative procedures, from the point of view of the results of an inputoutput model: 1) to convert the M&U input-output table into the traditional format - a domestic-use symmetric table at bp – and then implement the model; 2) to perform the direct modelling of the original table (the total-use rectangular table at pp). That equivalence is illustrated with Portuguese data for the year 2002.

Os quadros de Input-output podem obedecer a diferentes formatos, consoante três critérios principais: 1) formato simétrico ou rectangular; 2) inclusão ou não de produtos importados nos fluxos de uso; 3) sistema de valorização de preços (preços de base ou preços de aquisição). Pelo menos na UE, os quadros produzidos numa base regular por parte das Contas Nacionais oficiais são quadros de fluxos totais (incluindo importações), rectangulares e a preços de aquisição. Este é um formato diferente daquele em que os modelos tradicionais de input-output foram desenvolvidos (fluxos domésticos, simétricos, a preços de base). Obviamente, o problema é que, em muitos países, os quadros de input-output com essas características são disponibilizados apenas não regularmente. O objectivo deste artigo é provar a equivalência, sob hipóteses comuns, entre dois procedimentos alternativos: 1) converter a matriz de inputoutput rectangular no formato tradicional matriz simétrica, de fluxos domésticos e a precos de base – e só depois implementar o modelo; 2) desenvolver o modelo directamente a partir do quadro original (rectangular, com fluxos totais e preços de aquisição). Esta equivalência é demonstrada usando dados das matrizes portuguesas, para o ano 2002.

JEL Classification: C67, E01.

### 1. Introduction

Input-output tables can be classified according to three main criteria: 1) symmetric or rectangular format; 2) total use or domestic use flows and 3) valuation of goods and services. As a rule, the classical literature on input-output is based on symmetric matrices, with domestic flows, at basic prices. By a symmetric format we mean that the inner part of the input-output table has the same products or the same industries in its rows and columns. As a hypothesis, the classic Leontief tables assumed that each industry produced one and only one product. In input-output jargon. those tables depict product-by-product or industry-by-industry relationships. Remark, however, that in fact each industry may produce several secondary products beyond its main product that is referred in its denomination. Yet, since the end of the 1960's, when the United Nations introduced the 1968 System of National Accounts, countries are recommended (at the national level) to compile and publish the input-output tables on a rectangular, or Make and Use format as it is known as well. In these tables the above-mentioned classical restrictive hypothesis is avoided. The idea is to combine two tables to depict Supply (or Make) and Use product-byindustry relationships. The Use matrix gives information on product consumption made by industries and final users. As to the Make matrix, its columns depict how the various industries contribute to the products' output, while reading along the rows it gives us the distribution of each industry's output over the several products: the primary product of that industry and its various secondary products. Since the number of products included in the model may be higher than the number of industries, this format is called rectangular.

As for the total or domestic-use criterion that refers to the type of flows represented in the intermediate transactions that are part of the Use table and also in the several components of the final demand. Intermediate consumption of products (made by industries) and final uses (made by households, government, firms and foreign countries) involve the use of products which are not only domestically produced, but are also imported. A total-use table records the whole amount of inputs used, whether these have been produced within the country (or the region, depending on whether we are dealing with a national or a regional model) or imported. Conversely, if intermediate and final use flows are expurgated from the value of imported products, then we are facing a domestic (or intra-regional) use table.

Finally, the third criterion is related to the different prices at which goods and services may be evaluated. Current input-output tables may involve two different price systems: basic prices (*bp*), the closest to the value of production factor costs, or purchasers' prices (*pp*), which include taxes on the products (deducted from subsidies) and trade and transport margins.

Combining these criteria in several manners, many different types of input-output tables can be constructed. However, in practice, the starting point to the construction of these tables is usually the total flow Make and Use (M&U) rectangular table at purchasers' prices, since this is the standard format in which statistical information is gathered and published by official statistical institutes, that follows the recommendations of international National Accounts manuals.

The main issue that this paper deals with is whether there is any benefit, for modelling purposes, in relying upon a domestic use symmetric table, or it is equivalent to implement the model directly from the total use rectangular table. That means that we aim to compare two different procedures for input-output modelling, when the original data is produced and available on a total use rectangular format: 1) firstly convert the table into a domestic use symmetric table at basic prices, and then implement the model or 2) perform the direct modelling of the total use rectangular table at purchasers' prices, *i.e.*, implementing the model on the basis of the table in its original format.

Many authors have thought the first procedure as the most adequate for input-output model applications. For example, in what respects the symmetric feature of the table, the EUROSTAT itself advocates in its Input-output manual that «For analytical purposes a relationship is needed





between the inputs and the outputs irrespective of whether the products have been produced by the primary industry or by other industries as their secondary output» (EUROSTAT, 2002, p. 23); as a consequence, symmetric input-output tables «are compiled mainly to be used in input-output analysis» (p. 230). Concerning the content of the intermediate and final use flows, the same manual states that «the separation of domestically-produced and imported goods and services is of great importance for analytical purposes» (p. 145), leading to the option for domestic flow tables.

However, other authors, such as Madsen and Jensen-Butler (1999), Kauppila (1999) and Piispala (1998), suggest that the direct use of the M&U format has considerable advantages at different levels, namely:

- In the assembling process of the tables, since M&U tables are exempt of additional hypotheses (conversely to product-by-product or industry-by-industry tables), being more directly connected to the data collected by official statistical agencies.
- Make and Use tables are more easily intelligible for potential users of the model, since they resemble reality in a closer way.
- M&U format is more suitable for application in certain fields of research which deal specifically
  with spatial interaction flows of commodities such as: environmental modelling (for example,
  when flows of products to be used in different industries are attached with flows of polluting
  elements, such as CO2) and trade modelling (given that it is easier to incorporate trade
  statistics, which report trade taking place with products and not with the output of industries, in
  broad terms).
- Finally, as it will be demonstrated as well in this paper, the direct modelling of the rectangular table is a more timesaving procedure, which can be considered as an advantage of this alternative over the first one (involving the previous transformation into a symmetric table).

This paper is divided into five Sections, including this Introduction. In the next Section, the inputoutput model based on the M&U framework will be presented. The three main criteria used to classify input-output tables are the scope of Section 3. We proceed there to a detailed discussion of the assumed hypotheses used in the transformation of the M&U format into the classic symmetric domestic-use frame, that may be the same (and must be the same for comparison purposes) that are implicit in the rectangular approach. A practical test will be carried out in Section 4, aiming to compare with Portuguese data the results obtained from both above mentioned procedures of building an input-output model. The last Section presents a summary of the main conclusions.

#### 2. Input-output modelling based on a M&U matrix, with total use flows, at purchasers' prices

In this Section we deal with the rectangular or M&U model, with total-use flows, at purchasers' prices (pp) – as it is a less well known procedure of implementing an input-output model –, in order to demonstrate how it can de be directly modelled, avoiding its previous transformation in a symmetric matrix of domestic flows at basic prices (bp).

The simplified structure of an M&U matrix, with total-use flows, at purchasers' prices can be illustrated as in Figure 1, in which:  $U^{pp}$  and  $V^{bp}$  represent the Use and the Make matrix. The Use matrix refers to the product intermediate consumption by industries. It is a product-by-industry matrix: its rows refer to products and its columns to industries as lass of the total-use kind and it is a *pp* matrix. The Make matrix  $V^{bp}$  depicts the industries that produce each product, as primary or secondary production. In Figure 1, industries are along the rows and products in the columns. Although the M&U model works with *pp* flows, this specific matrix is *bp*.  $g^{bp}$  denotes the vector of product of products' final use (both domestically produced and imported); **m**, **d** and **l**, stand for the transformation of domestic to total supply and from *bp* valuation to *pp*. Finally, **w** represents the vector of the industries' value added.

### Figure 1 – Make and Use matrix – simplified structure

	Products	Industries	Final Uses	Total
Products	0	U <sup>pp</sup>	У <sup>рр</sup>	p <sup>pp</sup>
Industries	V <sup>bp</sup>	0	-	g <sup>bp</sup>
Value Added	0	w		
Imports	m	0		
Margins	d	0		
Taxes less subsidies	I	0		
Total	p <sup>pp</sup>	g <sup>bp</sup>		

The relationships involved in the M&U setting can be written in algebraic terms. Using matrix and vector notation, the industry balance may be expressed by<sup>1</sup>:

$$\mathbf{g}^{\mathbf{b}\mathbf{p}} = \mathbf{V}^{\mathbf{b}\mathbf{p}}\mathbf{i} = \left(\mathbf{U}^{\mathbf{p}\mathbf{p}}\right)'\mathbf{i} + \mathbf{w}' \tag{1}$$

At product level, the balance can be expressed as:

$$\mathbf{p}^{\mathbf{p}\mathbf{p}} = \left(\mathbf{V}^{\mathbf{b}\mathbf{p}}\right)'\mathbf{i} + \mathbf{m}' + \mathbf{d}' + \mathbf{l}' = \mathbf{U}^{\mathbf{p}\mathbf{p}}\mathbf{i} + \mathbf{y}^{\mathbf{p}\mathbf{p}}$$
(2)

The nuclear part of the M&U table is represented by the shadowed quadrants in Figure 1. Dividing all the elements of  $U^{pp}$  and  $V^{bp}$  by the correspondent column totals  $g^{bp}$  and  $p^{pp}$ , we obtain the following partitioned matrix, composed by the matrices  ${\bf Q}$  and  ${\bf S}$  and two zero-filled matrices:

$$\mathbf{D} = \begin{bmatrix} \mathbf{0} & \mathbf{Q} \\ \mathbf{S} & \mathbf{0} \end{bmatrix}^2.$$

Using matrix D, we can write the matrix system:

$$\begin{bmatrix} \mathbf{0} & \mathbf{Q} \\ \mathbf{S} & \mathbf{0} \end{bmatrix} \begin{bmatrix} \mathbf{p}^{pp} \\ \mathbf{g}^{bp} \end{bmatrix} + \begin{bmatrix} \mathbf{y}^{pp} \\ \mathbf{0} \end{bmatrix} = \begin{bmatrix} \mathbf{p}^{pp} \\ \mathbf{g}^{bp} \end{bmatrix}$$
(3)

This system may be manipulated in order to the outputs vector:

$$\left(\mathbf{I} - \mathbf{D}\right) \begin{bmatrix} \mathbf{p}^{pp} \\ \mathbf{g}^{bp} \end{bmatrix} = \begin{bmatrix} \mathbf{y}^{pp} \\ \mathbf{0} \end{bmatrix} \Leftrightarrow \begin{bmatrix} \mathbf{p}^{pp} \\ \mathbf{g}^{bp} \end{bmatrix} = \left(\mathbf{I} - \mathbf{D}\right)^{-1} \begin{bmatrix} \mathbf{y}^{pp} \\ \mathbf{0} \end{bmatrix} \Leftrightarrow \begin{bmatrix} \mathbf{p}^{pp} \\ \mathbf{g}^{bp} \end{bmatrix} = \begin{bmatrix} \mathbf{I} & -\mathbf{Q} \\ -\mathbf{S} & \mathbf{I} \end{bmatrix}^{-1} \begin{bmatrix} \mathbf{y}^{pp} \\ \mathbf{0} \end{bmatrix}$$
(4)

1 We will use the vector **i**, consisting of a column-vector filled by 1s, to compute the column sum of the correspondent matrix and the sign ' to indicate a transpose of a matrix or a column-vector.

2 It should be noted that even if the matrices  $U^{pp}$  and  $V^{bp}$  are not square, the partitioned matrix composed of these two (and of zero matrices of the appropriate dimension) will be square. Consider, for example, that there are 30 industries and 50 products. In this case, the matrix  $U^{pp}$  will have a dimension of 50\*30 and  $V^{bp}$  will be a 30\*50 matrix. Consequently, the partitioned matrix **D** will have a dimension of 80\*80 and **I** – **D** can be inverted.

### 3. Análise Empírica

Applying the general formulas for computing the inverse of a partitioned matrix<sup>3</sup>, we obtain:

$$\begin{bmatrix} \mathbf{I} & -\mathbf{Q} \\ -\mathbf{S} & \mathbf{I} \end{bmatrix}^{-1} = \begin{bmatrix} \mathbf{I} + \mathbf{Q}(\mathbf{I} - \mathbf{S}\mathbf{Q})^{-1}\mathbf{S} & \mathbf{Q}(\mathbf{I} - \mathbf{S}\mathbf{Q})^{-1} \\ (\mathbf{I} - \mathbf{S}\mathbf{Q})^{-1}\mathbf{S} & (\mathbf{I} - \mathbf{S}\mathbf{Q})^{-1} \end{bmatrix}$$
(5)

or

$$\begin{bmatrix} \mathbf{I} & -\mathbf{Q} \\ -\mathbf{S} & \mathbf{I} \end{bmatrix}^{-1} = \begin{bmatrix} (\mathbf{I} - \mathbf{Q}\mathbf{S})^{-1} & (\mathbf{I} - \mathbf{Q}\mathbf{S})^{-1}\mathbf{Q} \\ \mathbf{S}(\mathbf{I} - \mathbf{Q}\mathbf{S})^{-1} & \mathbf{I} + \mathbf{S}(\mathbf{I} - \mathbf{Q}\mathbf{S})^{-1}\mathbf{Q} \end{bmatrix}$$
(6)

Inserting equation (6) into (4), and multiplying these partitioned matrices, we get:

$$\mathbf{p}^{\mathsf{pp}} = (\mathbf{I} - \mathbf{QS})^{-1} \mathbf{y}^{\mathsf{pp}} \tag{(7)}$$

and

$$\mathbf{g}^{\mathbf{b}\mathbf{p}} = \mathbf{S} \big( \mathbf{I} - \mathbf{Q} \mathbf{S} \big)^{-1} \mathbf{y}^{\mathbf{p}\mathbf{p}}$$
(8)

The first equation allows us to compute the impact on total product supply originated by changes in final demand for products  $(\frac{\partial p^{pp}}{\partial y^{pp}})$ . Therefore, this is a product-by-product relationship. The second equation is an industry-by-product relationship; it shows the impact on industry's supply caused by changes in final demand for products  $(\frac{\partial g^{bp}}{\partial y^{pp}})$ . As for the right hand blocks in (5), the lower right hand,  $(I - SQ)^{-1}$ , depicts an industry-by-industry relationship: it gives us  $\frac{\partial g^{bp}}{\partial (Sy^{pp})}$ , where  $Sy^{pp}$  is the final demand by industries, transformed from  $y^{pp}$ . The upper right hand corner,  $Q(I - SQ)^{-1}$ , accounts for the impact on product demand, including imports, margins and taxes, created by changes in the demand directed at domestic industries  $(\frac{\partial p^{pp}}{\partial (Sy^{pp})})$ . Hence, it is a product-by-industry relationship.

We may then conclude that by performing a rectangular or M&U model (at *pp*, with total flows) we get within one single model product-by-product, industry-by-industry, product-by-industry and even industry-by-product relationships. This may be seen as an advantage over symmetric models. In these latter, each model provides only one type of relationship: the product-by-product symmetric model generates only a product-by-product impact equation; if we want to quantify an industry-by-industry impact, we will need to build an industry-by-industry symmetric table and develop the corresponding model.

3 These formulas can be found, for example, in Barnett (1990), pp. 71-72.

## 3. Deriving symmetric, domestic-use tables, at basic prices, from the standard M&U format: which issues and assumptions?

It is now time to look at the other way, namely at the previous transformation of the rectangular, total-use, *pp* table (the M&U format) into the classic Leontief-type symmetric, domestic-use, *bp* structure, that in this alternative procedure is the base of the input-output modelling. As a rule the rooted-survey information to deal with this transformation is very scarce, so we mainly have to resort to reasonable assumptions. These assumptions must be the same, for comparisons purposes, of those that are implicit in the M&U direct modelling. This section is devoted to the discussion of these assumptions.

### 3.1. Symmetric and rectangular input-output tables revisited.

The simplifying hypothesis adopted by the traditional symmetric input-output table is that each product is produced by one single industry and each industry produces one single product. However, in reality, the most common situation is that each industry produces a growing diversity of products, one of these being the primary product and the others the secondary ones. These secondary products can be divided into two categories: subsidiary products and by-products (EUROSTAT, 2002): subsidiary products are those secondary products which are technologically dissociated from the primary product; by-products are outputs that unavoidably result from the primary product production process, therefore being technologically related to it. As a rule, national Make and Use tables, following the SNA (System of National Accounts) recommendations, involve some partial refining in the Industry classification. This is due to the fact that industries are grouped according to the concept of kind-of-activity unit, and not according to the concept of enterprise. The term kind-of-activity unit (KAU) is used to denote a part of an institutional unit in which only one particular type of economic activity is carried out (Jackson, 2000). Thus, as a rule, enterprises «must be partitioned into smaller and more homogeneous units, with regard to the kind of production» (ESA, 1995, paragraph 2.105). So, in the National Accounts' industry classification. each industry consists of a group of KAUs which are «engaged in the same or a similar kind of activity» (ESA, 1995, paragraph 2.108). This means that most of the subsidiary products produced in each enterprise is classified under a different industry heading, the one that produces those products as its main activity. Exceptions to this procedure occur whenever it is not possible to separate the secondary from the primary activity, either because secondary production is of byproduct nature, or because the available information obtained from enterprises does not allow for separation (this being the case with most small firms, which have no accounting documents which allow for their partitioning into different KAUs). As a result, the values of production recorded outside the main diagonal in the Make matrix are mostly by-products, along with some residual subsidiary products that could not be separated from the main activity in the firms in which they were produced. The presence of these flows outside the main diagonal of the Make matrix - that represent the production by industries of products that do not fall in their core business - is the reason why the M&U model is not of symmetric type. As a consequence in the Use matrix each column refers to one industry that may produce more than one product; but their inputs still consist of single products. The Use matrix is then of product-by-industry kind.

Thus, symmetric input-output tables (SIOT) cannot be built directly with the statistical data collected by regular firm surveys. As a consequence this kind of tables can only be achieved in a derivative way, departing from the M&U tables, and assuming some hypotheses in order to calculate the product-by-product (or industry-by-industry) intermediate consumption flows<sup>4</sup>. Two alternative hypotheses, connecting the products' output and the industries' output may be used in the transformation of product-by-industry matrixes in symmetric ones, either of product-by-product or of industry-by-industry technology assumption (ITA) and the commodity technology assumption (CTA).

4 As well as to compute the value added by products, or, in industry-by-industry tables, the final demand by industries.



In the ITA case each industry has its own technology, which is common to all the commodities it produces. Thus, the technology assigned to each product depends on the industry where it is produced (ten Raa and Rueda-Cantuche, 2007). This kind of assumption is usually pointed out as preferable when the majority of secondary production is of by-product nature (Miller and Blair, 2009). On its turn, CTA assumes that each product is always produced by the same technology, regardless of the industry in which it is produced. For this reason, it is best suited to treat subsidiary production (Miller and Blair, 2009). In this paper we will deal with both the hypotheses, namely when in Section 4 we proceed with real data and compare the actual values of the input-output multipliers.

#### 3.2. Total use flows versus domestic use flows.

Another major issue concerning input-output tables is the treatment of imported products. In a total Use table, as the one that is comprised in the M&U format, all the use flows (intermediate and final) also include imported products, beyond national produced flows. In fact, this means that the intermediate Use matrix reflects true technical relationships: each of its elements indicates the total amount of a certain input used to produce a certain output. Data collected by means of surveys to firms can be directly used to produce these types of tables. The same does not apply to domestic flow tables. In this case, a Use matrix of imported products is needed in order to subtract its value from the total Use table. Direct information to construct such an Imports matrix is very rare. It is in fact very difficult for many firms to know the origin (imported or domestic flows, based on direct information, is also very hard (or even more complex, since the number of intermediate traders between the importing firm and the final user is usually greater). Being so, Import matrices are very often built merely by resorting to plausible assumptions, seldom complemented by direct information on some particular products.

The most common assumption – and the one that we adopt in this paper – is the imports proportionality hypothesis which asserts that, for each product, the share of imports in any type of use (intermediate or final) of that product is the same and is given by the proportion of imports on total supply of the same product. For example, if 40% of steel's total supply is imported, it is assumed that, in every industry which uses steel, 40% is imported and the same applies to any type of final use. This means that imports are differentiated by type of product but not by type of use.

Although controversial, this hypothesis is adopted in many cases, alone or combined with the incorporation of direct information, even when the domestic-use symmetric table is assembled by the official entities. In what concerns to the estimation of the imports matrix, for example, even OECD recognizes that this happens, stating that «Techniques used to construct the import matrix data vary between countries, but every country in the OECD database made, to some extent, use of the import proportionality assumption in the construction of their import matrices» (OECD, 2000, p.12). Moreover, the Input-output database provided by OECD (consisting of symmetric industry-by-industry tables) is compiled using this kind of assumptions, whenever supplementary information is not available (Yamano and Ahmad, 2006).

One crucial point on this assumption is the product disaggregation level that is applied (EUROSTAT, 2002). If the import coefficients are calculated at a much aggregated level, the imports proportionality hypothesis may not be acceptable. Thus, the most detailed level of disaggregation available on import data should be used. This does not usually originate a great deal of trouble on national tables since international imports data by products is available at a very detailed product level<sup>5</sup>. On the other hand, several authors note that some final uses, like

5 The magnitude of the errors coming from such an assumption, however, can only be accounted for when there is a benchmark survey-based imports matrix against which the estimated one can be compared. This is done in Oosterhaven and Stelder (2007), in their comparison between four alternative non-survey inter-country input-output table construction methods, for nine Asian countries and the USA. In one of the non-survey input-

exports, for example, have less incorporation of imported products than others, like investment. In order to take this differentiation into account, they have proposed to exclude exports from the import proportionality assumption, assuming that there are no re-exports. This is done, for example, in Miller and Blair (2009), and Jackson (1998). As emphasized by Lahr (2001), this approach should be preferred only in those cases in which the researcher knows that the export vector has no (or almost no) re-exports. In the present work, however, the import proportionality assumption will be taken uniformly throughout the various types of intermediate and final uses.

### 3.3. Basic versus purchasers' prices.

Different concepts can be used in the valuation of input-output flows of goods and services, ranging from the factor cost to the purchaser's price. The valuation at factor costs represents the production price and reflects better the production function of each product (Martins, 2004). At the opposite, the purchasers' prices represent the amount paid to obtain «a unit of a good or service at the time and place required by the purchaser» (EUROSTAT, 2002, p. 121). In spite of this multiplicity of concepts, however, in practice SNA input-output tables use only two price concepts: basic price and purchaser's price. Basic prices are similar to factor costs, except for the fact that basic prices include other taxes and subsidies on production, which are not possible to allocate to specific products<sup>6</sup>. Basic prices (*bp*) can be obtained from purchasers' prices (*pp*), subtracting the taxes on products less subsidies on products and the trade and transport margins.

The published M&U tables usually employ *pp* concept to balance supply and use. It is however, sometimes argued, that this valuation is not sufficiently homogeneous to be used for input-output analytical purposes; for example, the ESA's Input-Output Manual states that «a valuation at purchasers' prices is a less homogeneous option as the shares of trade and transport margins differ from industry to industry and also from and between the final uses; the same is true for the shares of product taxes less subsidies» (EUROSTAT, 2002, p.124). It is also true that basic prices are closer to the concept of production costs involved in the technical relationships used in input-output analysis. These relationships assume that a certain amount of an input represents the same physical unit irrespective of the production process in which it is used (EUROSTAT, 2002).

Hence, it would be desirable that prices were cleared from margins and taxes which differently affect the diverse uses of the products. The problem lies in the compilation of the valuation matrices required to transform *pp* into *bp*, since direct information on the value of margins and taxes comprised in each use flow is very scarce. In fact, when someone buys a certain item, he/she doesn't know very often the amount of margins and sometimes taxes comprised in the price that has to be paid. In the absence of direct information to construct valuation matrices and obtain a basic price valuated table, the proposal is to assume the same kind of proportionality hypothesis than for imports: the margin (net taxes) rate comprised in any type of use (intermediate or final) of that product is assumed to be the same for each product, and is given by the proportion of margins (net taxes) on total supply of the same product.

What is the plausibility of such an assumption? In this case, it is useful to look at each of the following items separately: Value Added Tax (VAT), margins, other taxes on products and subsidies on products. In what concerns non-deductible VAT<sup>7</sup>, the problem is quite complex. Ideally, direct information should be available in order to: 1) identify the type of users who support non-deductible VAT. Non-deductible VAT is, in fact, supported mainly by households and, in

output tables, they assume that there is no imports matrix and use the imports proportionality assumption to indirectly estimate it. The comparison between this table and the benchmark (which is a semi-survey based inter-country table) allow the authors to conclude that in general, «The tests show that the impact of using self-sufficiency ratios to estimate the domestic flows is small (...)» (Oosterhaven and Stelder, 2007, p. 258). 6 Taxes (subsidies) on products are those that «are payable per unit for some goods or services produced or transacted» (EUROSTAT, 2002, p. 200); examples: Value added taxes, import duties or tobacco product tax. Taxes (or subsidies) on production are those paid (or received) by firms as a direct result of their production activity, «independently of the quantity or value of the goods and services produced or sold» (*dem*, p. 200). 7 Deductible VAT is not included in the *pp* valuation.



some exceptional cases, by firms, either falling upon intermediate consumption or Gross Fixed Capital Formation (e.g. firms exempt from VAT and sometimes not allowed to deduct it from their purchases) and 2) Perform the linkage between the different VAT taxes and the product classification in the Use matrix; if the level of aggregation is high, some problems can arise because groups of products may well involve different VAT taxes (EUROSTAT, 2002).

Treating margins on a proportional assumption basis is also not completely realistic. In fact, it has to be recognized that different users of a product pay different margins on it. For example, a manufacture will certainly pay a smaller amount of margins on stationery materials than the final consumer. Finally, the use of the proportional assumption in the case of other taxes and subsidies is less controversial. These taxes and subsidies fall upon specific products and as a rule all the users have to support them. For example, taxes on gasoline have to be paid equally by any type of user of this product. As for imports, in any of the items mentioned in this Section, the proportionality assumption must be applied at the most disaggregated level of product classification. This is important in order to avoid situations in which groups of products are heterogeneous in respect to margins or tax rates.

In this paper, however, as our purpose is confined to the theoretical argument of the equivalence of different approaches, the proportionality assumption is allowed by simplification to all these flows, concerning the transformation of *pp* on *bp*.

### 4. A test with Portuguese data

In this Section, it will be shown that the direct modelling of the rectangular M&U matrices, with total use flows and at *pp*, that adopts a framework that is equal or very close from the official statistics, is exactly equivalent to the modelling of a domestic flow symmetric table (at *bp*), when it is derived from the former one, using similar assumptions. To do so, we will begin by computing the input-output multipliers obtained both through the direct modelling of the rectangular table, and through the product-by-product and industry-by-industry symmetric tables that can be obtained from the same rectangular frame. Then we focus on the analysis of the multipliers and conclude that insofar of the method we use for achieving them, we get exactly the same results.

Although this paper focuses in real data from the Portuguese economy, and makes the option of showing the results obtained by both the methods, to conclude that actually they are the same, a mathematical proof of our argument is also provided in an Appendix.

#### 4.1. Deriving the input-output multipliers

With the purpose of comparing the multipliers produced by both methods, we begin by performing a rectangular model, including the computation of the associated inverse matrices. The data in which we based this experience is the Portuguese Make and Use tables for the year 2002, at current prices, provided by the Portuguese Statistics National Institute (INE)<sup>8</sup>. Every year, since 1995, INE provides a set of National Accounts tables, which includes a M&U table. Products and industries are usually presented in a 60 by 60 disaggregate level (ESA95 – A60 classification). The level of aggregation used in this paper, however, corresponds to a less disaggregated classification also provided by INE containing only 31 products and 31 industries. The Portuguese Make matrices are heavily diagonal, meaning that most of the production has been affected by its primary producing industry, in the process of partial refining of Industries' classification, as it has been previously explained. Intermediate and final uses of goods and services are composed of both domestically produced and imported products, but no import matrices are regularly compiled. Additionally, these Use flows are valuated at *pp*. Thus our first step was to implement an input-output rectangular model, as the one described in section 2, based in the M&U table provided by the INE.

8 We are thankful to INE, for its kindness in providing us with the Make table, for the working year, which is not currently published. For the remaining information we downloaded it from the INE's official website: <u>www.ine.pt</u>.

It is important to emphasize that the model developed in section 2 implicitly assumes the ITA hypothesis. Although we did not develop that model in that section, it is possible as well to settle a CTA-based rectangular model. In this model the sub-matrix S of (3) - S represents the relative contributions of each industry to the supply of each product – is replaced by  $H^{-1}(I - \hat{r})(I - \hat{f} - \hat{n})$ . It is derived as well from  $V^{bp}$ , but it displays the product's structure of each industry output. That means that we have now calculated fixed coefficients along the rows of  $V^{bp}$ , and not anymore along its columns as we had done in S. c ( $\hat{c}$ ), f ( $\hat{f}$ ) and n ( $\hat{n}$ )<sup>9</sup> mean the import, margin and taxes (less subsidies) coefficient vectors (diagonal matrixes), that result from dividing vectors  $\hat{n}$ ,  $\hat{d}$  and I (inserted in Figure 1) by the total supply of products  $p^{pp}$ . In fact, pre-multiplying by ( $I - \hat{c}$ )( $I - \hat{f} - \hat{n}$ ) transforms one vector of total supplies at purchasers prices in its equivalent with domestic supplies at basic prices.

Therefore under CTA, instead of equation (3), we have:

$$\begin{bmatrix} 0 & Q \\ H^{-1}(I-\hat{c})(I-\hat{f}-\hat{n}) & 0 \end{bmatrix} \begin{bmatrix} p^{pp} \\ g^{bp} \end{bmatrix} + \begin{bmatrix} y^{pp} \\ 0 \end{bmatrix} = \begin{bmatrix} p^{pp} \\ g^{bp} \end{bmatrix} \Rightarrow$$
$$\begin{bmatrix} p^{pp} \\ g^{bp} \end{bmatrix} = \begin{bmatrix} I & -Q \\ -H^{-1}(I-\hat{c})(I-\hat{f}-\hat{n}) & I \end{bmatrix}^{-1} \begin{bmatrix} y^{pp} \\ 0 \end{bmatrix}$$

The multipliers produced by that version of the rectangular model are the cells of the inverted block matrix defined as follows:

$$\begin{bmatrix} \mathbf{I} + \mathbf{Q} \begin{bmatrix} \mathbf{I} - \mathbf{H}^{-1} (\mathbf{I} - \hat{\mathbf{c}}) (\mathbf{I} - \hat{\mathbf{f}} - \hat{\mathbf{n}}) \mathbf{Q} \end{bmatrix}^{-1} \mathbf{H}^{-1} (\mathbf{I} - \hat{\mathbf{c}}) (\mathbf{I} - \hat{\mathbf{f}} - \hat{\mathbf{n}}) & \mathbf{Q} \begin{bmatrix} \mathbf{I} - \mathbf{H}^{-1} (\mathbf{I} - \hat{\mathbf{c}}) (\mathbf{I} - \hat{\mathbf{f}} - \hat{\mathbf{n}}) \mathbf{Q} \end{bmatrix}^{-1} \\ \begin{bmatrix} \mathbf{I} - \mathbf{H}^{-1} (\mathbf{I} - \hat{\mathbf{c}}) (\mathbf{I} - \hat{\mathbf{f}} - \hat{\mathbf{n}}) \mathbf{Q} \end{bmatrix}^{-1} \mathbf{H}^{-1} (\mathbf{I} - \hat{\mathbf{c}}) (\mathbf{I} - \hat{\mathbf{f}} - \hat{\mathbf{n}}) & \begin{bmatrix} \mathbf{I} - \mathbf{H}^{-1} (\mathbf{I} - \hat{\mathbf{c}}) (\mathbf{I} - \hat{\mathbf{f}} - \hat{\mathbf{n}}) \mathbf{Q} \end{bmatrix}^{-1} \\ \begin{bmatrix} \mathbf{I} - \mathbf{H}^{-1} (\mathbf{I} - \hat{\mathbf{c}}) (\mathbf{I} - \hat{\mathbf{f}} - \hat{\mathbf{n}}) \mathbf{Q} \end{bmatrix}^{-1} \end{bmatrix} (10)$$

After computing the two sets (ITA and CTA-based) of M&U multipliers, we have to derive as well the product-by-product and the industry-by-industry domestic-flow symmetric tables valuated at *bp*, in order to allow for the comparison of the two kinds of the multipliers. Remember that there is no regular production and publication of any symmetric tables (product-by-product or industry-by-industry) in Portugal and in several other EU countries. Thus, whenever the researcher wants to make use of symmetric domestic flow tables he/she may have to assemble the import matrix and to symmetrize the table, relying on a set of different hypotheses <sup>10</sup>. The methodology used to build the SIOTs must follow exactly the same hypotheses than when we were dealing with the direct modelling of the M&U tables. The method involved three stages:

- 1. Computing Use matrices for margins and for taxes (less subsidies), in order to subtract them from the purchasers' prices Use table and obtain the basic prices Use table.
- 2. Computing the Use matrix of imported products, in order to subtract it from the basic prices Use table and thus obtain the domestic flow basic prices Use table. To do this, the proportionality hypotheses were used. In practice, most of the countries that construct an official import matrix also support their work in this kind of hypothesis (OECD, 2000).
- 3. Obtaining the product-by-product and industry-by-industry symmetric tables, resorting either to the ITA hypothesis or accepting the CTA instead.

9 We are using notation ^ to represent a diagonal matrix with the non-null entries being the elements of the correspondent column or row-vector.

10 It must be noted, however, that semi-official domestic flow symmetric input-output tables at basic prices has been provided every five years, since 1995. The compiling work was not directly done by the INE, but by a partnership between it and a governmental body: the Planning and Prospective Department. The description of the methodology of assembling these tables, and the matrices themselves, are available, for instance, at Dias (2008).

# $\bigcirc \blacksquare$

(9)



#### 4.2 Multipliers' comparison

The results of the partitioned matrix inversion, based on the M&U table, are displayed in Annex A.1 and A.2, corresponding to ITA and CTA hypotheses, respectively. We may find the productby-product multipliers in the upper left-hand blocks of these partitioned matrices. For example, when we assume ITA in the Annex A.1, this upper left-hand block corresponds to  $(I - QS)^{-1}$  in (6) and it shows the impact of changes in  $y^{pp}$  over  $p^{pp}$ . Let's take value 0.0217, located at [EE, DJ] in that matrix: this cell means that when final demand for «DJ – Basic metals and fabricated metal products» valuated at pp is exposed to an unitary increase, the direct and indirect extra demand (at pp) for product «EE – Electricity, gas and water supply» increases 0.0217 units. This increase also includes the increase for imported «EE» products, since the effect evaluated here is on  $p^{pp}$  as a whole. The correspondent product-by-product multiplier in the CTA-based partitioned matrix (Annex A.2) is 0.0229, which illustrates the fact that a different technological assumption does not originate extremely diverse values.

However, these multipliers comprised in the upper left-hand blocks of the matrices of Annexes A.1 and A.2 cannot be directly compared with the results obtained through domestic flows bp product-by-product symmetric tables, displayed in the Annexes A.3 and A.4. The reason is that in those blocks of those two annexes we have the impacts of the total demands - addressed to the domestic economy but also to imports, at pp - on total transactions, also at pp, imports included; that is of  $y^{pp}$  on  $p^{pp}$ . On the other hand, in symmetric models the results we should reach concern only shocks on domestic perceived demand, at bp, and their effect on domestic production valuated at bp as well. That means that for comparison purposes the upper left-hand blocks of the matrices of the Annexes A.1 and A.2 must be previously transformed by pre-multiplying those blocks by the diagonal matrixes  $(I - \hat{c})$  and  $(I - \hat{f} - \hat{n})$ , where c, f and n mean the import, margin and taxes (less subsidies) coefficients, in a first step, and then in a second stage post-multiplying by the inverses of those matrixes<sup>11</sup>. When we do that with our [EE, DJ] entry of 0.0217 pulled apart of ITA-based Annex A.1 matrix, we divide it by 0.6086 and 0.8874 and multiply it by 0.9886 and 0.9815, getting 0.0390. This is exactly the same value that is displayed in the [EE, DJ] cell of the domestic flow product-by-product inverse matrix (bp) of the Annex A.3. As for the CTAtechnology we proceed in the same way with 0.0229 extracted from the [EE, DJ] upper left-hand block of the matrix of the Annex A.2, and we obtain 0.0412 that is the cell [EE, DJ] of the domestic flow, bp, product-by-product matrix derived by CTA, depicted in Annex A.4. In fact, the matrices included in Annexes A.3 and A.4 as a whole may be obtained starting from the upper left-hand blocks of the matrices of Annexes A.1 and A.2 and applying the recommended transformations.

The lower right-hand blocks of the partitioned inverse matrices (Annexes A.1 and A.2) tell us about the industry-by-industry relationships. They correspond to the inverse matrices implicit in equations (5) and (6) for ITA and (10) for CTA. From these matrices one can assess the effects in each industry and in the total economy-wide caused by changes in the demand addressed to each industry. Looking again at the ITA case (Annex A.1), if the demand addressed to the output of industry «DJ» increases by 1, the «EE» industry will have to increase 0.0395 (through direct and indirect effects). As referred to before, the values of these lower right-hand block matrices should be equal to the values of the inverse matrices derived from a domestic flow industry-by-industry symmetric table (valuated at *bp*), constructed taking as original data the same rectangular table, and using similar hypotheses. Such matrices are presented in Annex A.5 for ITA and in Annex A.6 for CTA. In this case direct comparison is allowed, so then the same value 0.0395 may be found in the corresponding entry of the matrix of the Annex A.5. The same conclusion may be drawn to CTA-based matrices: as can be easily checked the lower right-hand block of the table in A.2 is the same matrix that is depicted in A.6.

11 Because the final impacts on  $p^{pp}$  and the initial shocks on  $y^{pp}$  must be both transformed multiplying by  $(I-\hat{t})(I-\hat{f}-\hat{n})$ , then, for counterbalancing, each multiplier is multiplied by the transformation coefficient corresponding to its row and divided by the one corresponding to its column.

### 5. Conclusions

The main issue of the present essay fell upon input-output modelling when the starting available matrix produced by official statistics is a total-flow rectangular table at purchasers' prices. Two alternative procedures have been analyzed: 1) to perform the direct modelling of the total-flow rectangular table at purchasers' prices; 2) to convert the initial matrix into a domestic-flow symmetric table at basic prices and then implement the traditional Leontief-type input-output model. It has then been proved that, when the hypotheses used to make the table symmetric and to operate the conversion from total use to domestic use flows (and from purchasers' prices to basic prices) are also used in the direct modelling of the starting rectangular matrix, the results we obtain are exactly the same. Thus, there is not a clear advantage, in most cases, in performing a previous transformation of the original tables, as some authors advise, into the symmetric domestic flow format, before implementing the model. Of course, in specific context – for instance, if one wishes to infer only the direct and indirect impact on domestic production resulting from an increase of final demand towards domestic products, it may be more appropriate to build the adequate symmetric input-output table (domestic-use and basic prices), instead of going into the process of solving the whole rectangular system previously described.

The equivalence between the results of both alternative procedures has been attested through a numerical example. In fact, an algebraic proof may be produced as well, as we have done in the Mathematical Appendix ahead. The numerical example consisted in using the Portuguese M&U table as a starting point (which is a total-flow rectangular table at purchasers' prices) and implementing the input-output model, applying both the previously referred procedures. As we expected, the input-output multipliers when referring to the same impact and the same effect are exactly the same, either by one or by the other procedure. We may even say, following that equivalence, that the direct use of the rectangular format has an important advantage over the use of symmetric tables: in the rectangular framework, the simple inversion of a partitioned matrix generates a set of four different inverse matrices (product-by-product, industry-by-industry, product-by-industry and industry-by-product ones); conversely, the symmetric tables originate only one type of inverse matrix (product-by-product or industry-by-industry).

In this paper, the development of the input-output model directly from the total-flow rectangular table at purchasers' prices, involved the use of proportionality hypotheses concerning imports, margins and taxes comprised in the intermediate and final use flows. Additionally, the model was developed in two versions - one using ITA and another using CTA. The proportionality and the technology hypotheses adopted are of course controversial. This doesn't however jeopardize the validity of the conclusions, as the important is that the same hypotheses have been used either in the direct modelling of the starting matrix, or in the conversion of this matrix into a domestic-flow symmetric table at basic prices. Besides, in many cases, even the official organisms of statistics use these kinds of simplifying hypotheses (or similar procedures) when assembling symmetric tables. In other cases, of course, these hypotheses are sometimes complemented or substituted by the inclusion of direct information, which however and as a rule can be incorporated in the rectangular model as well. For example, if a true import matrix is available, it is obviously better to use such information than to use the proportionality hypothesis (even though the gathering of direct information involves high costs and, in many cases, originates only a marginal improvement in the results). That however does not refute our point that equivalent hypotheses generate equivalent results.

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## $\frac{20}{21}$

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# Annex A.1 – Partitioned matrix inverse; ITA (results from the rectangular M&U model with total flows at pp)

	14.4	20	<b>1</b>	20	DA 1	D0 -	00	00	DC 1	DC 1	DO 1	DU 1	<b>D</b>	D	
2.5	1.1313	0.00000	0.0000	0.0076	0.3065	0.0010	0.00000	0.0722	0.0510	0.0001	0.0036	0.0001	0.0001	0.0022	0.0011
	1,1313	0.0020	0,0000	0,0030	0,2000	0.0215	0.0019	0,2120	0,0315	0,0004	0,00050	0.0004	0,0001	0,0036	5,0017
DD //	0.0003	1,0165	3 0000	0,0002	0,002.1	0.0001	0.0001	0,0002	0,0001	0,0000	0,00005	0.0001	0,0002	0,0001	0,0001
	0.0014	0,0003	0.0000	1 0 3 10	0.0042	0.0045	0,0002	0.00057	0,0055	0,2230	0,0177	0.0000	0,0100	0,0044	0,0022
00	0.1426	0.0003	0,0000	0.00420	1 1550	0.0061	0.0005	0.0072	0.0548	5 6655	0,002.0	0.0014	0,1040	0,0020	5 0037
DA ND	0,1420	0.0046	0,0000	0.0040	0.5518	1 3600	0.0295	0,0372	0,0140	0,0002	0.00003	0.0035	0,0045	0,0034	0,0021
NA	0.0000	0.0005	0,0000	0,0001	0.0010	0.0012	1 2204	0.0004	0,0027	6,0001	0.0041	0.0000	0.0001	0.00040	5 0001
D0	0.0002	0.0001	0,0000	0.0001	0.0001	0.0017	0.0000	1 3601	0.0006	0.0000	0.0001	0.0013	0.0001	0,0004	0.000
DD NE	0.0041	0.0008	0,0000	0.00000	0.0042	0.0000	0.0022	0.0228	1.0004	0.000	0.0014	0.0047	0.0001	0.0177	0.0020
DE DE	0.0000	0.0067	0,0000	0.1354	0.0253	0.0100	0.0077	0,0236	0.0110	1.0347	0.0120	0.0108	0.0403	0.0100	0.000
DC	0.02.00	0.0040	0.0000	0.0400	0.0482	0.0405	0.0497	0.0530	0.0573	0.0047	1.1454	0.0103	0.0510	0.0220	0.0000
00	0.0042	0.0016	0.0000	0.0014	0.0142	0.0000	0.0000	0.0130	0.0502	0.0000	0.008.1	1.0404	0.0120	0.0455	0.0562
51	0.0110	0.0014	0.0000	10100012	0.0122	0.0023	0.0024	0.0091	0.0000	0.0002	0.0001	0.0048	4 4 4 8 4	0.0140	0.0000
51	0.0000	0.0042	0.0000	0.0444	0.0477	0.0002-3	0.0193	0.0257	0.0420	0.00000	DISSES	0.0408	0.0445	3,0004	0.0047
55 752	0.0000	0.0024	0.0000	0.00141	0,0171	0.0001	0.0020	0.0002	0.0045	0,0000	0,00110	0.0104	0.0004	0.0133	1 1007
un	0.0004	0.0003	0.0000	0.0000	0.00000	0.0000	0.0004	0.0047	0.0012	0,0000	0.00012	0.0020	0.0003	0.0038	0.0082
502	0.0013	0.0032	0,0000	0,0001	0,000.8	0.000.4	0.0010	0,0047	0,0011	5,0002	0,00000	0.0000	0,0093	0,0085	0,0211
	0.0012	0.0001	0.0000	0.00013	0.0010	0.0014	0.0010	0.0017	0,0013	0,0001	0,0015	0.0000	0.0000	0.0000	0,0044
E F	0.0000	0.0000	3,0000	0,0013	0,0010	0.0134	0.0027	0.0002	0.0002	5,0001	0,0014	0.0070	0.0825	0.0317	5,000
TE .	0.0419	0.0000	0.0000	0,0001	0,0100	0.0000	0.0105	0.0201	0.0555	0,0000	0.0041	0.000	0.0040	0.0277	5 6 5 4
0.0	0.0135	0.0030	0.0000	0,0230	0.000	0.0001	0.000	0.0071	0,0130	5,0021	0,0001	0.0000	0.0270	0.0034	5,0140
	0.000	0.000	3,0000	5,0130	0.0040	0.0000	0.0021	0.0012	0.000	5,0000	0.0000	0.0004	0.0105	0.0032	5,0021
	0.0040	0.0001	0.0000	0,0131	0.0000	0.0075	0.0071	0.0033	0,0001	0.0002	0.0040	0.0003	0.0009	0,0000	5,0050
	0.01/1	0.0212	3,0000	0,1000	0,0199	0.0193	0.0007	0,0301	0,0305	0,0011	0,0104	0.0000	0,0005	2/4237	0,0150
N	0.0312	0.0268	0,0000	0,0631	0,0258	0.0327	0.0285	0,0530	0,0365	0,0016	0.0197	0.0230	0,0442	9,0229	0,0228
NA	0.0629	0.0335	0,0000	0,0996	0.9642	0.0499	0.0443	0,0625	0,0783	0.0023	0,9668	0.0492	0.0780	0,0434	0,033.
ul.	0.0000	0,0000	0,0000	0.0000	0,0000	0.0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000
VIV.	0.0004	0,0009	0,0000	0,0014	0,0008	0.0011	0,0009	0,0011	0,0014	0,0000	0,0008	0.0011	0,0016	0,0014	0,0000
NN CO	0.0027	0.0009	0,0000	0,0011	0,0010	0.0007	0.0008	0,0018	0,0006	0,0000	0,00002	0.0004	0,0008	0,0001	0,0004
00	0.0019	0.0019	0,0000	0,0038	0,0023	0.0021	0.0018	0,0027	0,0037	0,0001	0.0053	0.0018	0,0035	0,0016	0,0010
PP	0.0000	0,0000	0,0000	0,0000	0,0000	0.0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000
COLUMN SUM	1,5534	1,2239	1,0000	1,7723	1,6403	1,6601	1,6857	2,0902	1,6827	1,2879	1,3832	1,5192	1,0205	1,6033	1,6020
4A	0,7502	0,0015	0,0000	0,0025	D, 1564	0.0144	0,0058	0,1804	0,0344	0,0002	D,002/5	0,0044	0,0042	0,0029	0,0014
58	0.0002	0,4059	0,0000	0,0001	0,0010	0.0001	0,0001	0,0001	0,0001	0,0000	D,0001	0,0001	0,0001	0,0001	0,0000
CA	0.0000	0,0000	0,0000	0,0000	0,0000	0.0000	0,0000	0,0000	0,0000	0,0000	D,00000	0,0000	0,0000	0,0000	0,0000
CB	0.0013	0,0002	0,0000	0,8060	0,0017	0.0005	0,0004	0,0013	0,0010	0,0001	0,0023	0.0009	0,0890	0,0021	0,0012
DA	0.0718	0,0027	0,0000	0,0032	0,5794	0.0033	0.0149	0,0189	0,0078	0,0001	0,0029	0.0020	0,0029	0,0019	0,0012
DB	0.0033	0,0022	0,0000	0,0037	0,0013	0,7943	0,0240	0,0032	0,0026	0,0001	0,0046	0.0055	0,0027	0,0043	0,0014
DC	0.0002	0,0001	0,0000	0,0001	0,0001	0.0014	0.8021	0,0003	0,0004	0,0000	0,0001	0.0022	0,0001	0,0005	0,0001
DD	0.0033	0.0007	0,0000	0,0025	0,0033	0.0028	0.0019	1,0281	0,0127	0,0001	0,0012	0.0059	0,0115	0,0068	0,0026
DE	0.0067	0.0057	0,0000	0,0111	0,0185	0.0075	0.0135	0,0167	0,8173	0,0003	0,0082	0.0165	0,0200	0,0089	0,004
DF	0.0070	0.0098	0,0000	0.04/0	0,0036	0.0034	0.0027	0,0061	0,0040	0,2793	0.0208	0.0053	0,0118	0,0034	0.001
36	0.0111	0,0013	0,0000	0,0127	0,0070	0.0166	0.0138	0,0165	0,0178	0,0082	0,3520	0.0673	0,0165	0,0091	0,0041
DH	0.0021	0.0008	0,0000	0,0017	0,0065	0.0044	0.0170	0,0068	0,0074	0,0002	0,0082	0,4662	0,0067	0,0076	0,008.
DI	0 0090	0,0013	0,0000	0,0057	0,0065	0.0019	0,0019	0,0072	0,0046	0,0004	0,00036	0.0040	0,0294	0,0106	0,007
51	0.0054	0.0024	0,0000	0,0078	0,00066	0.0054	0,0105	0,0142	0,0067	0,0005	0,00078	0.0003	0,0244	0,6794	D)0644
DK.	0.0015	0,0010	0,0000	0,0034	0,0016	0.0013	0,0010	0,0026	0,0017	0,0001	0,0015	0.0085	0,0134	0,0160	0,4071
DL	0.0014	0.0013	0,0000	0,0035	0,0012	0.0012	0,0010	0,0019	0,0018	0,0001	0,00015	0,0044	0,0037	8003B	0,012
DM NO	0 0003	0,0013	0,0005	0,0011	0,0003	0.0003	0.0005	0,0005	3000/0	0,00000	Deccol	0.0008	0,0011	0,0040	0,004)
DN	0.0003	0.0004	0,0005	0,0000	0,0006	0.0148	0.0021	0,0140	0,0344	0,0000	0,0011	0.0051	0,0021	0,0105	0,002
EE.	0.0213	0,0084	0,0005	0,0796	0,0155	0.0224	0.0132	0,0243	0,0254	0,0008	0,0141	0.0163	0,0815	0,0211	0,009
**	0.0151	0,0057	0,0000	0,0232	0,0116	0.0000	0,0105	0,0198	0,0163	0,0026	0,00080	0.0088	0,0293	0,0248	0,017
36	0.0498	0,0647	0,0000	0,0884	0,0355	0.0285	0.0251	0,0827	0,0415	0,0027	0,0621	0.0316	0,0847	0,0241	0,0215
нн	0.0047	0.0049	0,0005	0,0122	0,0052	0.0069	0.0065	0,0085	0,0075	0,0002	0,0046	0.0050	0,0108	0,0078	0,005
	0.0165	0.0254	0,0005	0,0943	0,0191	0.0184	0.0170	0,0355	0,0347	0,0010	0,0176	0.0200	0,0551	0,0226	0,0144
ม	0.0288	0.0234	0,0005	0,0452	0,0244	0.0300	0.0261	0,0480	0,0333	0,0015	0,0188	0.0216	0,0408	0,0213	0,0208
0K	0.0396	0.0255	0,0000	0,0747	0,0480	0.0373	0.0334	0,0495	0,0821	0,0017	0,0426	0.0476	0,0585	0,0330	0,025
u.	0.0035	0.0018	0,0000	0.0074	0.0037	0.0028	0.0025	0.0037	0,0122	0.0001	0.0029	0.0027	0,0057	0,0026	0.0011
VM	0.0006	0.0010	0.0000	0.0016	0.0010	0.0012	0.0010	0,0013	0.0021	0.0000	0.0009	0.0012	0,0019	0.0015	0.0004
NN	0.0029	0.0009	0.0000	0.0013	0.0011	0.0003	8000.0	0,0019	0,0009	0,0000	0.0003	0.0005	0,0010	0.0002	0,0001
00	0.0021	0.0021	0.0000	0.0041	0.0024	0.0022	0.0019	0.0029	0,0040	0,0001	0.0023	0.0020	900036	0,0018	0,0011
PP	0.0000	0,0000	0,0000	0,0000	0,0000	0.0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0001
COLUMN SUM	1.0603	0.6024	0.0000	1,3537	0,9686	1,0331	1.0612	1,6738	1,1647	0,3006	0,5806	0.7952	1,3897	0,8327	0.644/



# Annex A.1 – Partitioned matrix inverse; ITA (results from the rectangular M&U model with total flows at pp) (cont.)

								_							
	DL.	DM	DN	tt:	++	99	нн		4J	KK.	LL.	MIN	NN	00	PP
AA	0,0022	D,0016	0,0244	0,0022	0,0129	0,0615	0,0894	0,0054	0,0031	0,0077	D,0055	0,0030	D,0255	0,0061	0,0000
88	0,0001	0,0000	0,0001	0,0001	0,0001	0,0025	0,0112	0,0003	0,0002	0,0002	0,0002	0,0001	0,0003	0,0002	0,0000
CA	0,0021	0,0016	0,0048	0,1349	0,0185	0,0570	0,0085	0,0216	0,0030	0,0074	0,0067	0,0042	0,0183	0,0138	0,0000
CB	0,0006	0,0011	0,0071	0,0014	0,0310	0,0141	0,0025	0,0015	0,0006	0,0019	0,0025	0,0006	0,0009	0,0015	0,0000
LIA.	0,0025	0,0013	0,0063	0,0025	0,0048	0,0863	0,2849	0,0082	0,0045	0,0083	0,0115	0,0064	0,0565	0,0077	0,0000
DB	D,0055	0,0056	0,0607	0,0015	0,0052	0,0363	0,0132	0,0031	0,0000	0,0005	0,0037	0,0011	0,0175	0,0090	0,0000
DC	0,0007	0,0004	0,0116	0,0001	0,0003	0,0044	0,0002	0,0003	0,0001	0,0004	0,0000	0,0001	0,0001	0,0007	0,0000
DD	0,0025	0,0002	0,0941	0,0020	0,0524	0,0401	0,0009	0,0006	0,0016	0,0045	0,0005	0,0014	0,0015	0,0106	0,0000
DE	0,0006	0,0047	0,0157	0,0107	0,0129	0,2050	0,0160	0,0255	0,0210	0,0315	0,0155	0,0195	0,0124	0,0057	0,0000
DP DO	0,0066	0,0042	0,0145	0,0757	0,0824	0,1731	0,0242	0,0686	0,0071	0,0168	0,0308	0,0101	0,0720	0,0334	0,0000
DO DU	0,0206	0.0136	0,0362	0,0113	0.0405	0,1004	0.0145	0.0106	0.0041	0.0111	0,0075	0.0047	0,1116	0.0266	0.0000
DH DI	0,0400	0,0100	0,0020	0,0038	0,0161	0,1123	0,0080	0,0082	0,0027	0.0004	0,0006	0,0016	0,0000	0,0075	0,0000
5.I	0.000400	0.00007	0.0708	0.00002	0,1010	0.0000	0.04172	0.0001	0.04000	0.00000	0.00077	0.00028	D. COLOR	0.0077	0.0000
55	0,00000	0.00000	0,0001	0,0122	0,1282	0,2204	0,0182	0.0008	0.0002	0,0172	0.00048	0.0040	0,0000	0,0107	0,0000
50 D	1 1883	0,0100	0.0004	0.0000	0000000	0,0000	0.0072	0.000000	0.0012	0.0041	0.00000	0,0012	0.00008	0.0002	0,0000
79.7	0.00037	1 1876	5 205	0,00170	5,0000	0,1227	0,0120	0,0007	0.00011	0,0122	0.00138	0,0001	0.00010	0,00.00	0,0000
PM PM	5 25 15	0.0171	1 (18.15)	0.0013	000113	0,1200	0.0118	0.00070	0.0031	0.0036	0.0080	0.0047	0.00010	0.0163	0.0000
FF	0.0083	0.0000	0.0158	1 5565	010050	0 1857	0.0071	000754	0.0137	1000100	0.0351	0.0330	0.00151	0.0575	0.0000
FF	0.0070	0.0053	0.0114	0.0294	1 3515	0.1896	0.0142	0.01241	0.0173	0.0457	0.0159	0005100	0.0066	0.5407	0.0000
00	0.0038	0.0000	0.0040	0.0045	0.0044	1 1418	0.0065	0.0726	0.0007	0.0106	0.0073	0.0000	0.0072	0.0060	0.0000
нн	0.0005	0.0000	0000001	0.00042	DODDAR!	0.1470	1.0064	0.00225	0.0122	0.0110	0.0165	0.0057	0.0200	0.0108	0.0000
	0.06150	0.0105	0.00255	000355	DOD 554	0.6530	<b>DODAUS</b>	1.2741	0.00124	0.0450	0.0450	1000055	I (DOPES	0.1253	0.0000
	0.0180	0.0125	0.0268	0.0630	0.0530	0.4466	0.0407	0.0605	1 1010	0.0008	0.0207	0.0150	0.0278	0.0580	0,0000
22	0.0458	0.0776	0.0433	0 1112	01012120	1,4552	0.0462	0.1516	0.2446	1 2265	0,0207	0.0730	0.1078	0,0000	0.0000
	0.0000	0.0000	0.0000	0.0000	100000	0.0000	0,0000	0.0000	0.0000	0.0000	1 0000	0.0000	0.0000	0.0000	0.0000
NM	0.0017	0.0012	0.0011	0.0017	0.0009	0.0123	0.0011	0.0018	0.0018	0.0015	0.0003	1.0045	0.0006	0.0012	0.0000
NN	0.0004	0.0007	0.0000	0.0000	DODDON N	0.0046	0.0013	0.00010	0.0001	0.0006	0.0011	0.0004	1.0401	0.0004	0.0000
00	0.0015	0.0011	0.00054	1000024	000000	0.0633	1000074	DOGREE	0.0040	0.00155	0.0067	1005105	0.0066	1,1227	0.0000
PP	1000000	0.00000	1000000	1000000	1000000	0.0000	1000000	1000000	1000000	1000000	1000000	1000000	1000000	0.0000	1.0000
COLUMN SUM	1.4012	1,4352	1,6236	2,1016	2,2256	5.9560	1,0001	1.0026	1.5100	1.6250	1,4121	1,2457	1.6656	1,0501	1.00001
44	0.0016	0.0011	0.0163	0.0017	0.0097	0.0607	0.0641	0.0040	0.0004	0.0063	0.0040	0.0022	0.0179	0.0057	0.0000
18	1000000	0.00000	10000001	100000	0000001	0.00089	0000214	1000004	DESCO	1000003	DESCO	1000000	1000004	1033601	1000000
CA	0.00000	0.00000	0.0000	1000000	000000	0.0000	0.00000	1000000	0.00000	1000000	0.00000	1000000	1000000	0.00000	0.0000
CB	0.0006	0.0009	0.0056	0.0012	0.0250	0.0138	0.0021	0.0013	0.0006	0.0021	0.00000	0.0005	0.0006	0.0013	0.0000
DA	0.0015	0.0008	0.0004	0.0017	0.00011	0.0817	0,1411	0.0053	0.00000	0.00016	0.00003	0.00015	LOCOLE AND	0.0047	0.0000
08	0,00054	0,0004	0.00550	0,00016	1000055	0,0416	10000/1	1000045	0,00008	10000007	1000003	1000000	0,0108	0.0055	0,0000
00	Labored	LOBOROM	100000	10000001	MO2001	0,0058	1000004	LOCCO.	LOBOGO I	LOCCE.	1000006	LOCCOLI	LORGEO I	1000003	1000000
DD	1000041	0,00027	0,08501	0,00017	1005203	0,0448	10000N	1000030	0,0014	DODGN	LODGOPH	D000IN	DOOLE	1000034	10,00000
DE	0,00068	0.0008	0,0158	0,00074	0000000	0,1356	000118	0.0175	0.0138	0.0214	0,0103	0.0125	00008	0.0384	10,0000
DF	0.0018	0.0014	0.0045	0,0215	0.0179	0.0520	0.0070	0.0245	0.0025	0.0074	0.0066	0.0030	0,0211	0.0006	0.0000
DG	0.00072	0.0044	0.0115	0.00000	0.0129	0,0499	0.000460	0.00088	0.0016	0.0047	0.00035	0000115	0.00445	DISCOUT	0.0000
DH	0,0219	0,0148	0,0158	0,0019	0.0085	0,0584	0.00038	0,0044	0,0013	0,0046	0,0019	0.0009	0.0027	0.0006	0,0000
DI	0,0031	0.0066	0.0082	0,0049	0,1352	0,0739	0.0130	0.00065	0.0027	0.0065	0.0060	0.0020	0.0029	0.0060	0,0000
DJ La	DOTE: N	0,00554	0,0422	0,00011	0,0681	0,1349	0,01100	0,00005	0.00000	0,0100	000000	0,000151	00000	0.0000	0,0000
DK	00068	0,0004	0,0041	LOCOPE	DOM: N	0,0359	100000	0,00010	0,0003	0,00018	00018	100002	0,0018	DODE	100000
DL	0,4475	D/0/153	DOORE .	0,0108	0,0128	D,0765	0002	0,0000	00002	00002	00000	000000	0,00010	0,00001	10,00000
DM	0,00040	0,4120	100000	1000002	0,00017	0,0621	LOCALS	0,00054	Discos	DOCCH.	0,0051	0,0004	00000	0,0015	0,0000
DN	0,0018	0,0064	0,5375	0,0008	0,0065	0,0243	0,0061	0,0018	0,0016	0,0021	0,0041	0,0022	0,0017	0,0063	0,0000
EE	0,0081	0,0068	0,0157	1,4881	0,0474	0,1925	0,0360	0,0248	0,0132	0,0193	0,0350	0,0232	0,0177	0,0743	0,0000
FF	0.0079	0.0054	0,0114	0.0284	1,2716	0,2140	0.0142	0.0410	0.0178	0.0542	0,0158	0.0099	0.0102	0.0356	0.0000
GG	0,0565	0,0151	0,0343	0,0316	0,0629	6,4351	00335	0,1363	0,00028	0,1177	0,0466	0,0216	0,0410	0,0642	0,0000
нн	0,00000	0,0000	0,0067	0,0000	0,0072	0,1567	DUIRI	0,0211	0,0116	0,0163	0,0151	0,0004	0,0108	0,0176	0,0000
	0,0171	0,0164	PO0955	0,0044	0,0468	D,6235	0000	1,1675	0,6458	00000	0,6458	DOTTO	District	D, 1175	0,0000
m –	0,0175	0,0117	0,0245	0,0488	0,0488	0,4331	0,0381	0,0575	0.9660	0,1158	0,0214	0,0152	0,0275	0,0580	0,0000
RK.	0,0401	0,0205	0,0320	D,0827	0,0680	1,1483	0,0754	D, 1130	0,1813	D,9082	0,0835	D,0545	D,0804	D, 1664	0,0000
LL	0,0025	0,0014	0,0025	0,0261	0,0174	0,0722	0,0113	0,0006	0,0114	0,0555	1,0068	0,0045	0,0061	0,0303	0,0000
MM	0,0015	0,0012	0,0012	D,0025	0,0017	0,0192	0,0017	0,0022	0,0003	0,0042	0,0025	1,0050	0,0011	0,0019	0,0000
NN	and the second se	and the second se	and the second se			the second se				and the second se				A REAL PROPERTY AND INC.	ED CODEC
	0,0006	0.0000	0.0004	0,0006	0,0009	0,0087	0,0060	0,0006	0,0006	0,0021	0,0013	0.0006	1,0/91	0,0011	0,0000
00	0.0006	0.0013	0.0004	000000	0.0005	0.0067	0.0060	DESIG	0.0006	0.00055	0,0013	0.0006	0,0064	0,9774	0.0000
00 PP	000000 000011/ 000000	0.0013 0.0000	000000	0.00000	0.00005	0,0087	0.00080 0.0081/ 0.00000	DESCS DESES	0.00005	0000340	0.00015	000000	0,0004	0.9774	0,0000

# Annex A.1 – Partitioned matrix inverse; ITA (results from the rectangular M&U model with total flows at pp) (cont.)

	AA .	88	CA	CB	DV	DB	OC I	DD .	DE	DF	DG	OH	0	βŬ	DK
AA	0.1965	0,0051	0,0000	0,0046	D,4052	0.0366	0,0131	0,3562	0,0793	0,0013	D,0105	0,0109	0,0081	0,0065	0,0040
58	0.0005	0,0470	0,0000	0,0002	0,0041	0.0002	O LOON	0,0002	0,0002	0,0000	D,00008	0.0002	0,0002	0,0002	0,0000
CA	0.0112	0.0213	0,0008	0,0576	0,0078	0.5076	0.0055	0,0038	0,0075	0,8205	0,0261	0.0114	0,0248	0,0082	0,0058
CB	0.5024	0.0007	0,0008	0,0540	0,0041	0.0009	0.0003	0,0017	0,0017	0,0005	0,0058	0.0021	0,1405	0,0047	0,003
DA	0.2157	0,0114	0,0000	0,0063	0,3052	0.0103	0.0490	0,0483	0,0225	0,0007	0,0161	0.0065	0,0064	0,0061	0,005
DB	0.0060	0.0088	0,0000	0,0073	0,0633	0.6364	0.0658	0,0052	0,0035	0,0004	0,0060	0.0183	0,0053	0,0054	0,002
DC	0.0003	0.0002	0,0000	0,0002	0.0002	0.0026	0.5651	0.0003	0,0010	0,0000	0,0002	0.0023	0,0002	0,0005	0,000
DD	0.0062	0.0019	0,0000	0,0039	0.0060	0.0042	0.0036	0,4561	0,0252	0,0006	0,0038	0.0075	0,0197	0,0134	0,006
DE	0.0153	0.0218	0,0000	0.0217	0.0654	0.0174	0.0337	0,0303	0,4036	0,0019	0,0373	0.0274	0,0410	0,0243	0,015
DF	0.0361	0.0690	0.0000	0,2191	0.0223	0.0167	0.0125	0,0251	0,0176	0,0906	0.0837	0.0212	0,0527	0,0202	0,015
DG	0.05222	0,0100	0,0000	0,0526	0.0000	0.0634	0,0715	0,0679	0,00015	0,09811	0,4645	0,4194	0,0689	0.03510	0.0222
DH	0.0064	0 00039	0,0000	0,0043	0.00210	0.0129	0.05-95	0,0160	0,0163	0.0009	0.0240	0.0940	0,0171	0,0284	0,041
DI	0.0180	0.0005	0,0000	0,0093	0,00045	0.0007	0.0040	0,0115	0,0090	0,0021	0,0127	0.0094	0,1583	0,0258	0,021
DJ LO	0.0149	0.0108	0,0000	0,0181	000003	0.0149	0.0017	0,0318	0,0180	124000	0,0014	0.0025	0,0590	0,5654	0,236
DK	0.00835	0.00000	0,0000	0,0106	000000	0.0052	0.0001	0,0078	0,00012	0,0010	0,00903	0.0417	0,0434	0,0300	02110
DL	0.0051	0.0000	MOON STREET	0,0112	1000035	D DOHO	ditter/	0,0036	B002B	1000000	000003	0.0127	0,0122	0,0142	LODM1
DM	0.0017	di.com	L00016	0,00010	000000	0.0025	0.0015	0,0018	0,00115	1000000	0,00041	0,0211	0,0028	B00216	LODD N
DN	OLCO 12	0.0015	10000	0,00010	DEGIS	DIGHT	0.0044	0,0021	DOM:NO	1000005	000043	0.0161	0,0044	0,05001	10063
EE	010551	0.0215	0,0000	0,1068	DESCH	0.0354	Ultran	0,0580	0,0523	0,00310	D(0428)	0.0055	0,1133	0,0405	0,0745
FF	0.0054	0.0133	0,0000	0,0303	0,03241	0.0153	0.0177	0.0005	0,0234	0,0100	0,0228	0.0155	0,0358	0,0449	0,032
86	0.0123	0.0083	0,0000	0,0193	0,00078	0.0064	0.0042	0,0035	0,0088	0,0015	0,0005	0.0065	0,0140	0,0058	0,008
нн	0.0073	0,0128	0,0000	0,0160	0,0003	0.0127	0,0118	0,0116	0,0121	0,0007	0,0137	0.0104	0,0156	0,0155	0,014
	0.0050	0,0680	0,0000	0,1293	0,0371	0.0322	0.0286	0,0474	0,0552	0,0030	0,0454	0.0415	0,0781	0,0437	0,037
μ.	0.0472	0.0646	0.0000	0.0683	0.0487	0.0653	0.0467	0.0675	0.0536	0.0058	0.0565	0.0447	0.0588	0.0418	0.058
KK .	0.0796	0.0839	0.0005	0,1280	0.1216	0.0639	0.0716	0.0796	0,1170	0.0085	0,1616	0.0938	0,1036	0.0794	0.082
LL	0.0000	0.0000	0,0000	0.0000	0.0000	0.0000	0.0000	0,0000	0,0000	0,0000	0.00000	0.0000	0,0000	0,0000	0.000
MM	0.0000	0.0021	0.0000	0.0017	0.0016	0.0010	0.0014	0.0014	0.0021	0,0001	0.0004	0.0022	0.0023	0.0025	0.000
NN	0.0041	0.0021	M0000	0.0014	0.00019	0.0010	0.0010	0,0024	200012	1000000	0.00000	0.0001	0,0011	200000	0,0001
00	010081	0.0050	DECO10	0.00419	Discussion	0.00014	010081	DITORN D	10035	10000001	0.000541	DICORN	0.0045	000000	100004
PP .	<b>D</b> ICCO	010000	00000	1000000	100000	Discol	DECODE	00000	0000000	1000000	1000000	0.0000	0.0000	000000	100000
COLUMN SUM	0.8365	0.5605	0.0000	0.9927	1,0352	1,1330	1,1217	1,5601	1,0378	1,0565	1,1183	1.0591	1.0913	1.1178	1,012
2.4	1.1351	0.0037	0.0000	0.0033	0 2 2 3 3	0.0245	0.0094	0.2375	0.0530	0.0000	0.0074	0.0074	0.0054	0.0046	0.0021
RB.	0.0002	1.0184	0.0005	0.0001	0.0017	0.0001	0.0001	0.0001	0.0001	5,0007	0.0004	0.0001	0.0001	0.0001	0.000
CA	0.0000	0.0000	1,0005	0.0007	0.0000	0.0000	0.0002	0.0005	0.0005	0.0007	0.0000	0.0003	0.000	0.0005	0.000
CB	0.0020	0.0005	0.0005	1.0471	0.000	0.0003	0.0007	0.0014	0.0014	100004	0.00070	0.0017	0.1094	0.00016	0.001
DA	0.1064	0.0068	0.0005	0.0041	1.1534	0.0054	0.0249	0.0247	0.0118	0.0004	0.0069	0.0037	0.0034	0.0034	0.000
DB	0.0050	0.0054	0.0005	0.0048	0.0023	1.3665	0.0398	0.0034	0.0027	0.0004	0.006-4	0.0117	0.0034	0.0047	6.003
DC	0.0002	0.0002	0.0005	0.0000	0.0000	0.0017	1,3395	0.0002	0 0004	0.0000	0.000	0.0015	0.0002	0 0004	6.000
DD	0.0049	0.0017	0.0005	0.003.5	0.0063	0.00045	0.0024	1.3499	0.0195	0.0004	0.0004	0.0001	0.0153	0.0104	0.004
DE	0.010*	0.01.44	0.0004	0.01/3	0.0000	0.0117	0.0223	0.0199	1.2610	0.0015	0.0040	0.0184	0.0299	0.0161	0.014
DE	0.0100	0.02,45	0.0004	0.0674	0.0067	0.0067	0.0044	0.0074	0.00047	1,0252	0.0084	0.0104	0.0154	0.0001	0.004
00	0.0164	0.00023	0.000	0.031	0.0109	0.0064	0.0224	0.0213	0102210	0.0303	1 1435	0.1304	0.0214	0.0105	0.000
DH	0.0001	0.0022	0.0000	0.0073	0.0127	0.0063	0.0000	0.0077	0.008.1	0.0002	0.0116	1.0422	0.0001	0.0122	0.019
0	0.0157	0.0002	0.000	0.0074	0.011-0	0.00000	0.0001	0.0023	0.0024	10000512	0.00000	0.0074	1.110	0.0191	0.014
51	0.0002	0.0051	0.000	0.0304	Distant	0.0004	0.0174	0.0175	Distance.	DODOSIL!	Distant	0.0454	0.0020	1,223,11	0.171
72	O COLORA	0.0000	0.000	0.004	Libron for	0.0021	0.0014	0.0073	Di Colora	1000000	0.000	0.0163	0.0121	0.0124	1.004
71	0.0021	0.0001	0.000	In constant	Librore and	0.0020	0.0015	0.0023	DODDE-	La Da Casa da C	Labora Fi	0.0052	0.0040	0.005	0.021
100	0.0002	0.0002	0.000	0.00015	Laborer 1	0.000101	0.000	0.0002	010004	Dependent.	0.0001	0.0072	0.0014	0100515	000071
DN	0.0003	0.0010	0.000	0.0011	0.00011	0.0145	0.0003	0.0035	0.0045	0.0000	0.00010	0.0085	0.0024	0.0543	0.000
FF	0.0000	0.0010	0.000	0 5845	0.000	0.0190	0.0210	0.0311	0.0336	0.00010	0.041	0.0335	0 100 1	0.0335	0.000
FF	0.000	0.01/2	0.000	0.0380	0.0000	0.0151	0.0173	0.0047	5 (1221)	5 0 0 0 0 0	0.0337	0.0154	0.0353	0.0436	5 (177
0.0	0.0753	0.1600	0.0005	0 1155	0.5210	0.0454	0.0204	0.0417	0.0587	0.0450	0.0710	0.0530	0.0951	0.0400	5 (144
н	0.007*	0.0123	0.0000	0.0150	0.002.0	0.0116	0.0104	0.0104	0.01111	5 0007	0.0120	0.0004	0.01.44	0.0144	6.011
	0.00011	0.0620	0.0000	0.9150	0.0000	0.0309	0.0974	0.04/10	0.0523	5,00001	0.0476	0.0305	0.0723	0.0414	0,012
	0.0450	0.0600	0.0000	0,1200	0,0001	0.0603	0.0220	0.0013	0.0020	0,0000	0.0470	0.0410	0.0545	0.000	0.000
90 90	0.0405	0.0600	0,000	0,0036	0,0461	0.0607	0.0429	0.0613	0,0002	0,0004	0.1360	0.0213	0.0295	0,0305	0,003
~	0.0668	0.0641	0,0000	0.0964	0,0000	0.0627	0.0640	0,0677	0,0885	0.0064	0,1208	0.0/12	0,0180	0,0995	0.042
1.1.	0.0045	0.0045	0,000	0,0078	0,0001	0.0008	0.0040	0.0046	0,0087	0.0006	0.0064	0.0001	0.0071	0.0048	0,004
100	0.0009	0.0026	0,000	0,0021	0,0019	0.0020	0.0016	0,0016	0,0025	0.0001	0.0027	0.0024	0.0025	0.0028	0,002
an	0.0042	0.0024	0,000	0,0016	0,0021	0.0014	0.0014	0.0025	9,0012	0,0000	0,0008	0.0009	0,0013	0,0004	0,001
00	0.0031	0.0052	0,0000	0,000.3	0,0045	0.00.00	0.0030	0,0035	0,0057	0.0003	0,0066	0.0034	0,0048	0.0015	0,002
PP	0.0000	0,000	0,0000	0,0000	0,0000	0.0000	0,0000	3,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,000
COLOWN SOM	1,6029	1,6136	1,0000	1,7427	1,8614	1,7608	1,7347	2,0172	1,7826	1,1946	1/6700	1,6030	1,8623	1,7246	1,6195



# Annex A.1 – Partitioned matrix inverse; ITA (results from the rectangular M&U model with total flows at pp) (cont.)

			-												
	0.	UM	UN	EE.	FF	93	HH	1	uu T	KK.	u.	MM	NIN	00	PP
AA	0.0049	0,0040	0,0431	0,0022	0,0134	0.0110	0,1013	0,0059	0,0035	0,0066	D,00055	0.0030	0,0256	0,0092	0,0000
00	0.0002	0,0001	0,0002	0,0001	0,0001	0.0004	0.0128	0,0003	0,0002	0,0002	0,00002	0.0001	0,0003	0,0003	0,0000
CA PD	0.0048	0,0041	0,0091	0,1405	0,0178	0.0005	0,0005	0,0235	0,0034	0,0082	0,0001	0.0042	0,0184	0,0145	0,0000
00	0.0014	0.0024	0.0141	0,0014	0.002.0	0.0018	0.0028	0,0017	0,0007	0,0010	0.0025	0.0005	0.0009	0,0016	0.0000
DA	0.0007	0.0034	0,0116	0.0025	0.0048	0.0021	0.0230	0,0090	0,0052	0.00000	0.00115	0.0004	0,0567	0,0088	0.0000
DC	0.0018	0.0010	0.0232	0.00014	0.0000	0.0005	0.0003	0.0003	0.0002	0.0004	0.00001	0.0001	0.0001	0,0008	0.0000
00	0.0059	0.0095	0 1815	0.0021	0.0556	0.0069	0.0044	0.0039	0.0016	0.0044	0.0006	0.0014	0.0015	0.0121	0.0000
DE	0.0224	0.0121	0.0298	0.0110	0.0130	0.0350	0.0203	0.0290	0.0240	0.0366	0.0155	0.0194	0.0125	0.0406	0.0000
DF	0.0121	0.0099	0.0277	0.0786	0.0643	0.0296	0.0299	0.0996	0.0076	0.0154	0.0306	0.0101	0.0722	0.0371	0.0000
DG	0.0520	0.0009	0.0091	0.0117	0.0426	0.0226	0.0159	0,0117	0.0046	0.0103	0.000755	0.0047	0,1120	0.0302	0.0000
DH	0.1266	0.0428	0,0645	0,0040	0,0190	0.0191	0.0090	0,0101	0,0030	0,0102	0.00010	0.0018	0,0053	0,0085	0.0000
DI	0.0095	0.0243	0,0205	0,0064	0,1900	0.0106	0,0195	0,00088	0,0037	0,0096	0,00077	0.0026	0,0035	0,0086	0,0000
נם	0.1610	0,1736	0,1290	0,0127	0,1350	0.0074	0.0200	0,0166	0,0056	0,0170	0,00094	0.0040	0,0098	0,0178	0,0000
DK	0.0192	0.0422	0,0108	0,00058	00082	0.0091	0,0081	0,0008	0,0014	DODDE	0,000133	0.0012	0,0039	0,0036	0,0000
DL	0.4671	0,1090	0,0030	DOD1112	0,0001	0.0026	0,0153	0,0576	0,0103	0,0126	0.0000	0.0051	0,0201	0,02252	0,0000
DM	0.0077	0,4742	0,0032	0,0016	DECE	0.000	0.002	0,00315	0,0012	100004	0,03150	0.0003	0,0015	0,0035	1000000
DN	0.0042	0,0476	0,1619	0,0013	0,0119	0.0045	0,0133	0,0035	0,0035	0,0084	0,00030	0.0042	0,0035	0,0185	60000
25	0.0193	0,0185	0,0293	0,5812	0,0308	0.0307	0,0417	0,0282	0,0150	0,0155	D,0361	0.0052	0,0181	0,0722	0,0000
PP	0.0179	0,0139	0,0210	0,0304	D,3728	0.0510	0.0159	0,0459	0,0197	0,0585	D,0159	0.0100	0,0100	0,0462	0,0000
GG	0.0080	0,0051	0,0074	0,0046	0,0101	0.0250	0.0098	0,0250	0,0042	0,0115	0,0075	0.0032	0,0073	0,0105	0,0000
нн	0,0152	0,0085	0,0137	0,0055	0,0074	0.0258	0,0104	0,0250	0,0138	0,0146	D,0165	0,0057	0,0209	0,0214	0,0000
	0.0386	0,0250	0,0433	0,0366	0,0323	0,1144	0,0300	0,2994	0,0438	0,0439	D,0459	0.0298	0,0226	0,1428	0,0000
μ	0.0432	0.0331	0,0505	0,0540	0,0647	0.0770	0.0452	0,0994	0,1156	0,1090	0,0207	0.0150	0,0279	0,0968	0,0000
KK.	0.1083	0.0731	0,0767	0,1147	0.0869	0.2541	0.1177	0,1654	0,2799	0,2648	0,1112	0.0730	0,1082	0,2641	0.0000
LL	0.0000	0,0000	0,0000	0,0000	0,0000	0.0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000
NW	U DURH	0.0002	0,0021	0,0017	D. CCCCS	0.0001	0.001.0	0,0019	0,0020	0,0016	0,000-3	0.0004	0,0008	0,0013	0,00000
NN CO	0.0003	0.0000	0,0005	0,00000	Discost l	0.5105	0.00011	0.0000	0,0002	DODDDA	0,0011	0.0105	0,0004	0,0005	0,00000
00	0.0000	0.0003	0.0000	0,0021	Liberti I	0.0103	0.0000	0.0000	000000	DOCTORIES INTO NO.	LOCOLD I	0.0000	0,0000	010000	10000000
COLUMN SUM	1.1505	1.1023	1.1916	1.1447	1.2001	0.1057	0.9013	0.9617	0.5112	DOC SHI	0.4119	0.2457	0.6703	1.0038	0.00000
24	0.0035	0.0028	0.0289	0.0016	0.0053	0.0078	0.0726	0.0043	0.0027	0.0047	0.0040	0.0022	0.0180	0.0085	0.0000
BB	0.0001	0.0001	0.0001	0.0001	0.00001	0.0002	0.0051	0.0007	0.0001	0.0001	0.0001	0.0000	0.0002	0.0007	0.0000
CA	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
CB	0.0012	0.0024	0.0111	0.0012	0.0864	0.0016	0.0023	0.0014	0.0007	0.0016	0.00020	0.0005	0.0008	0.0014	0.0000
DA	0.0034	0.0021	0.0062	0.0017	0.0029	0.0074	0.1623	0.0057	0.0034	0.0042	0.0062	0.0035	0.0289	0.0053	0.0000
DB	0.0086	0,0093	0,0710	0,0012	0,0036	0.0035	0,0089	0,0025	0,0009	0,0016	0,0024	0.0008	0,0106	0,0064	0,0000
DC	0,0013	0,0007	0,0141	0,0001	0,0002	0,0004	0,0002	0,0003	0,0001	0,0003	0,0002	0,0001	0,0001	0,0006	0,0000
DD	0.0049	0.0071	0,1404	0,0017	0.0427	0.0056	0.0036	0,0033	0,0016	0,0036	0.0022	0.0012	0,0013	0,0096	0,0000
DE	0,0154	0,0082	0,0199	0,0073	0,0067	0,0231	0,0133	0,0191	0,0158	0,0240	0,0102	0,0126	0,0082	0,0266	0,0000
DF	0.0041	0.0032	0.0085	0.0220	0.0183	0.0068	0.0078	0,0268	0,0027	0,0049	0.0086	0.0030	0,0212	0,0110	0,0000
DG	0.0172	0,0100	0,0222	0,0036	0,0134	0,0074	0,0055	0,0040	0,0017	0,0035	0,0025	0,0015	0,0347	0,0097	0,0000
DH	0.0572	0,0225	0,0296	0,0019	D, ODEM	0.0090	0,0042	0,0048	0,0015	0,0048	0,0019	0,0009	0,0027	0,0041	0,0000
	0.0073	0.0182	0,0155	0,0045	0,1436	0.0005	0.0147	0,0071	0,0030	0,0078	0,0060	0.0020	0,0029	0,0068	0,0000
12	0.0000	0.0173	0.0024	0,0072	0,0020	0.0004	0.0073	0.001	0.0004	Distance in	0,0003	0.0002	0.001-	0.0014	0,0000
55 51	1 1545	0.0416	0.0033	0.00014	Distant Street	0.0127	0.0000	0.0220	0100545	0.0053	0,00010	0.0000	0.0077	0.0300	0.00000
70/	0.0054	1.1679	0.0037	0.0007	0.0014	0.0079	0.0011	0.0005	0.00000	0.0011	0.000451	0.0004	0.0009	0.0017	information of
DN	0.0029	0.0245	1.0830	0.0007	0.0067	0.0000	0.0060	0.0010	0.0015	0.0019	0.0041	0.0021	0.0017	0.0095	1000000
EE	0.0189	0.0180	0.0287	1.5565	00055	0.0304	0.0404	0.0262	0.0150	0.0151	0.0350	0.0255	0.0177	0.0711	10,00000
FF	0.0180	0.0140	0.0207	0.0295	1,3519	0.0313	0.0159	0.0448	0.0203	0.0573	0.0158	0.0099	0.0102	0.0452	0.0000
88	0.0655	0.0372	0.0517	0.0324	0.0639	1,1530	0.0622	0,1485	0,0365	0,0773	0.0466	0.0216	0,0495	0,0727	0.0000
нн	0.0139	0,0079	0,0126	0,0057	0,0071	0.0241	1,0099	0,0231	0,0132	0,0139	0,0151	0.0053	0,0189	0,0199	0,0000
1	0,0369	0,0263	0,0410	0,0352	0,0353	0,1083	0,0291	1,2765	0,0438	0,0440	0,0435	0.0253	0,0221	0,1342	0,0000
11	0.0409	0.0310	0,0464	0,0505	0.0503	0.0747	0.0430	0,0628	1,1091	0,1029	0,0214	0.0152	0,0276	0,0959	0,0000
KK	0.0634	0.0662	0,0582	0,0854	0,0662	0,1900	0.0879	0,1244	0,2075	1,1968	0.0829	0.0544	0,0806	0,1891	0,0000
u	0.0065	0.0038	0,0045	0,0132	0,0061	0.0125	0.0063	0,0089	0,0130	0,0131	1,0059	0.0040	0,0055	0,0154	0,0000
NM	0.0047	0.0034	0,0024	0.0020	0.0013	0.0028	0.0016	0.0024	0,0027	0.0022	0.0026	1,0067	0,0010	0,0019	0,0000
NN	0.0011	0.0008	0,0006	0,0005	0,0009	0.0012	0.0013	0,0010	0,0006	0,0006	0,0013	0.0005	1,0833	0,0009	0,0000
00	0.00036	0.0032	0,0118	0,0030	0,0004	0.0109	0.0082	0,0131	0,0063	0,0211	D.ODEA	0.0096	0.0065	1,1242	0,0000
PP DOLLARS	4,0000	0,0000	0,000	0,0000	0,0000	0,0000	0,0000	0,000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	1,0000
COLUMN SUM	1,7028	1,6317	1,8108	1,8835	2,0060	1,7704	1,8349	1,8903	1,0144	1/6262	1,3448	1,2114	1,4698	1,0916	1/0000

# Annex A.2 – Partitioned matrix inverse: CTA (results from the rectangular M&U model with total flows at pp)

	44	88	ICACB.	DA	DB	DC	DD 1	DE	DF	DG	DH	DI	DJ	DK
44	1 1236	0.0010	0.00/10	0.2174	0.0214	0.0020	0.2979	0.0535	0.0004	0.0022	0.0047	0.0074	0.0032	0.00*
DD	0.0000	1.0103	0.0000	0,2174	0.0210	0,0000	0.2938	0,0000	0,0004	0,0020	0.0047	0,0000	0,0002	0.001
00	0,0002	0.0007	1.0000	0,0022	0,0001	0,0001	0.0001	0,0001	0,0000	0,0003	0.0001	0,0001	0,0001	0,000
UNUS DA	0,0094	0,0097	1,0207	1.10063	0,0040	0,0034	0.0000	0,0001	0,2491	0.0110	0.0000	0,1224	0,0009	0,000
Lin.	0,1400	0,0036	0.0013	1,1941	0,0008	0,0302	0,0391	0,0149	0,0002	0,0048	0,0029	0,0040	0,0031	0,001
DB	0,0053	0,0034	0,0016	0,0015	1,3852	0,0400	0,0018	0,0011	0,0004	0,0019	0,0075	0,0031	0,0018	0,000
DC	0,0002	0,0000	0.0000	0,0001	0,0013	1,3464	-0.0003	0,0005	0,0000	0,0000	0.0002	0,0001	0,0001	0,000
DD	0,0038	0,0005	0,0006	0,0042	0,0020	0,0020	1,3764	0,0172	0,0002	0,0012	0,0030	0,0148	0,0067	0,001
DE	0,0084	0,0085	0,0048	0,0294	0,0099	0,0207	0,0234	1,2749	0,0009	0,0133	0,0126	0,0300	0,0132	0,005
DF	0,0248	0,0369	0.0524	0,0117	0,0096	0,0076	0.0202	0,0118	1,0382	0,0305	0,0110	0,0266	0,0107	0,005
DG	0,0396	0,0033	0,0118	0,0181	0,0500	0,0448	0,0547	0,0579	0,0253	1,1700	0,2302	0,0503	0,0277	0,011
эн	0,0031	0,0013	0.0007	0,0146	0,0074	0,0335	0,0109	0,0103	0,0000	0,0081	1,0496	0,0125	0,0145	0,018
N	0,0111	0,0010	0,0006	0,0128	0,0018	0,0022	0.0064	0,0056	0,0004	0,0042	0.0038	1,1209	0,0142	0,008
N	0,0083	0,0037	0,0034	0,0178	0,0073	0,0189	0,0213	0,0108	0,0011	0,0105	0,0389	0,0438	1,3281	0,092
ж	0,0034	0,0023	0.0022	0,0035	0,0028	0,0017	0.0057	0,0037	0,0005	0,0031	0.0210	0,0327	0,0069	1,115
ЯL —	0.0029	0.0027	0.0024	0.0021	0.0024	0.0018	0.0034	0.0038	0.0006	0.0023	0.0030	0.0079	0.0048	0.030
DM	0,0009	0,0029	0.0005	0,0003	0,0009	0,0002	0.0005	0,0007	0,0001	0,0008	-0.0022	0,0010	0,0029	0,002
3N	0,0006	0,0005	0.0003	0.0008	0.0126	0.0025	0.0041	0,0082	0,0001	0.0012	0.0071	0.0030	0,0165	0.001
E	0.0229	0.0089	0.0257	0.0163	0.0241	0.0136	0.0262	0.0273	0.0062	0.0155	0.0188	0.0844	0.0229	0.009
1	0.0143	0.0050	0.0050	0.0111	0.0084	0.0105	0.0121	0.0149	0.0034	0.0076	0.0070	0.0239	0.02.48	0.012
20	0.0014	0.0116	0.0045	0.0009	000002	0.0024	0.0068	0.0050	0.0012	0.032	0.0220	0.0093	0.0029	0.002
HH I	0.0047	0.0051	0.0059	0.0047	0.0074	0.0089	0.0069	0.0079	0.0004	0.0047	0.0050	0.0107	0.0094	0.005
	0.0185	0.0278	0.0305	0.0185	0.0183	0.0167	0.0000	0.0595	0.0074	0.0120	0.0201	0.0518	0.0292	0.013
	0,0100	0,0010	0.0000	0.0355	0,0100	0.0784	0.0574	0.0000	0.0077	0,0110	0,0220	0,0404	0.0010	0,013
u 	0,0013	0.0294	0.0156	0,0255	0,0028	0,0284	0.0534	0,0356	0,0037	0,0200	0.0222	0,0404	0,0219	0,023
in i	0,0505	0,0326	0.0290	0,0625	0,0484	0,0425	0.0559	0,0773	0,0048	0,0571	0,0455	0,0683	0,0408	0,031
L	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,000
en 👘	0,0004	0,0009	0.0004	0.0008	0,0011	0,0009	0.0010	0,0014	0,0001	0,0006	0.0011	0,0016	0,0014	0,000
IN	0,0028	0,0009	0,0003	0,0010	0,0007	0,0008	0,0020	0,0008	0,0001	0,0002	0,0004	0,0008	0,0000	0,000
20	0,0017	0,0018	0,0010	0,0021	0,0018	0,0017	0,0021	0,0036	0,0000	0,0022	0,0014	0,0029	0,0014	0,000
<sup>sp</sup>	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,000
VA.	0,7976	0,0007	0.0006	0,1543	0,0153	0,0057	0.2065	0,0380	0,0003	0,0016	0.0033	0,0039	0,0022	0,000
38	0,0001	0,4184	0.0000	0,0009	0,0000	0,0001	0.0001	0,0000	0,0000	0,0001	0.0000	0,0001	0,0000	0,000
CACB	0,0023	0,0024	0.2456	0,0015	0,0012	0,0008	0,0019	0,0015	0,0608	0,0028	0,0012	0,0297	0,0017	0,000
5A.	0,0272	0,0007	0.0005	0.6153	DECONS.	0.0157	0.0062	0,0054	0,0001	-0.0008	0.0007	0,0016	0,0014	0,000
8	0.0030	0,0019	0.0009	0.0008	0,8289	0.0228	0.0014	-0.0007	0,0002	-0,0005	0,0021	0,0017	0,0009	0,000
xc	0,0001	0,0000	0.0000	0,0000	0,0006	0,8240	-0.0002	0,0003	0,0000	0,0000	-0,0015	0,0000	0,0001	0,000
0	0.0030	0.0003	0.0004	0.0033	0.0012	0.0016	1,1180	0,0139	0,0001	0.0009	0.0018	0,0119	0.0054	0,001
)E	0.0056	0.0057	0.0032	0.0198	0.0063	0.0138	0.0157	0.8598	0.0006	0.0089	0.0049	0.0201	0.0089	0.003
ar -	0,0073	0,0109	0.0155	0.0034	0.0029	0.0072	0.0050	0,0035	0,3068	0,0090	0.0033	0.0065	0.0032	0,001
3G	0.0123	-0.0001	0.0032	0.0061	0.0158	0.0158	0.0191	0.0204	-0.0095	0.4225	0.0784	0.0162	0.0076	0.003
я́н	0.0014	0.0008	0.0003	0.0076	0.0037	0.0164	0.0023	0.0004	0.0001	0.0004	0.5875	0.0061	0.0018	0.008
N	0.0035	0.0007	-0.0063	0.0006	0.0013	0.0015	0.0064	0.0043	-0.0013	0.0030	0.0020	0.8626	0.0107	0.005
N.	0.0044	0.0020	0.0039	0.0101	100021	0.0104	0.0102	0.0057	0.0004	0.0020	0.0242	0.02/5	0.7600	0.000
K	0.0013	0.0000	0.0000	0.0010	0.0000	0.0004	0.0012	0.0010	0.0000	0.0011	0.0067	0.0158	-0.0115	0.483
9	0.0004	0.0000	0.0000	0.0000	0.0007	0.0004	0.0040	0.0010	0.0001	0.0000	0.0000	0.0000	-0.0003	0.010
	0.0000	0.0002	0.0000	0.0000	0.0000	0.00000	0.00010	0.0000	0.0001	0.0002	0.0000	0.0000	0.0000	0.000
AL.	0,0002	0,0000	0.0000	0.0004	0.0000	0,0000	0.0001	0,0000	0,0000	0,0002	0.0200	0.0003	0.0026	0,000
mi T	0,00012	0,0001	0.0001	0.0000	0,0000	0,0013	0.0300	0,0041	0,0000	0,0000	0.0025	0.0012	0,0045	-0,000
2	0.0235	0.0095	0.0264	0.0168	0.0246	0.0142	0.0268	0,0278	0,0061	0.0158	0.0183	0.0867	9,9230	0,009
r	0,0108	0,0041	0.0032	0,0063	0,0085	0,0095	0.0163	0,0128	0,0022	0,0064	0.0065	0,0189	0,0228	0,011
1.3	0,0805	0,0653	0.0268	0,0157	0,0155	0,0103	0.0263	0,0315	0,0075	0,0177	0,0107	0,0404	0,0108	0,007
н	0.0043	0.0047	0.0035	0.0043	0.0067	0.0063	0.0060	0,0072	0,0007	0.0043	0.0045	0.0067	0,0079	0.004
	0,0158	0,0267	0.0293	0,0178	0,0175	0,0160	0.0347	0,0350	0,0071	0,0163	0,0192	0,0494	0,0222	0,013
1	0,0302	0,0250	0.0150	0,0246	0,0317	0,0274	0.0516	0,0348	0,0036	0,0193	0,0214	0,0389	0,0211	0,022
ж	0.0358	0.0194	0.0185	0.0475	0.0369	0.0332	0.0356	0,0589	-0.0061	0.0447	0.0355	0.0482	0.0297	0.024
L	0,0000	0,0000	0.0000	0,0000	0,0000	0,0000	0.0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,000
M	ERCO2	0,0010	0.0004	0.0008	DOCUMENTS OF	0,0002	0.0011	0,0014	0,0001	0,0028	0.0011	0,0016	0,0014	0,000
IN .	0.0028	0.0009	0.0003	0.0010	0.0008	0.0006	0.0020	0.0006	0.0001	0.0002	0.0004	0.0008	0.0000	0.000
0	0.0014	0.0016	0.0008	0.0019	0.0016	0.0015	0.0018	0.0031	0.0000	0.0020	0.0012	0.0021	0.0011	0.000
0	1000000	0.0000	0.0000	0.0000	MOORE	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.000



# Annex A.2 – Partitioned matrix inverse: CTA (results from the rectangular M&U model with total flows at pp) (cont.)

	0	DM	DN	ec.	EC.	88	нн			KK.		ABA	NN	00	99
2.2	0.0017	0.0013	0.0227	0.0010	0.0134	0.0403	0.0030	0.0044	0.0024	0.0051	0.0038	0.0008	0.0252	0.0073	0.0000
AR .	0.0001	000000	0.0001	0.0001	0.0001	0.0019	OD1115	0.0003	0.0001	0.0007	0.0001	Interest in	0.0003	0.000	0.00000
CLOB	0.0023	10100000	0.0123	0.1538	0.0407	0.0657	0.0114	0.0003	0.0027	0.0056	0.0113	0.0040	0.0100	010151	0.0000
04	0.0021	0.0011	0.0059	0.0018	0.0000	0.0559	0.2055	0.0077	0.0038	0.00050	0.0102	000051	0.0554	0.0060	0.0000
00	0.0056	0.0055	0.0567	0.0009	0.0045	0.0175	DO SHOE	0.0025	0.0005	000012	0.0005	0.00009	0.0173	1000000	0.00000
DC	0.0007	0.0000	0.0129	0.0000	0.0001	-0.0010	0.0002	0.0002	0.0001	0.0003	0.0002	0.0001	0.0001	0.0006	0.0000
DD	0.0022	0.0031	0.1016	-0.0015	0.0563	0.0314	0.0038	0.0025	0.0012	0.0006	0.0008	0.0012	0.0013	0.0103	0.0000
DE	0.0090	0.0042	0.0158	0.0104	0.0119	0.2064	0.0181	0.0270	0.0203	0.0334	0.0110	0.0194	0.0125	0.0372	0.0000
DF	0.0048	0.0032	0.0142	0.0369	0.0604	0.1767	0.0241	0.0632	0.0053	0.0130	0.0315	0.0101	0.0734	0.0344	0.0000
D3	0.0233	0.0115	0.0380	0.0102	0.0419	0.0927	0.0138	0.0092	0.0029	0.0077	0.0051	0.0043	0.1143	0.0274	0.0000
DH	0.0538	0.0161	0.0356	0.0028	0.0185	0.1029	0.0079	0.0089	0.0018	0.0066	0.0024	0.0016	0.0052	0.0070	0.0000
DI	0.0037	0.0069	0.0110	-0.0052	0,1931	0.0658	0,0171	0.0051	0.0022	0,0063	0.0025	0.0020	0.0031	0.0067	0,0000
DJ	0.0683	0,0658	0.0700	0,0047	0,1365	0.2072	0,0179	0,0123	0.0034	0,0142	0.0048	0,0034	0.0091	0,0143	0,0000
DK	0.0075	0,0153	0,0052	0,0043	0,0344	0.0500	0,0071	0,0026	0,0008	0,0031	0.0038	0,0011	0,0038	0,0027	0,0000
DL	1,2065	0,0413	0,0000	0,0287	0,0319	0,1575	0,0131	0,0544	0,0083	0,0004	0,0077	0,0048	0,0195	0,0000	0,0000
DM	0.0020	1,1504	0,0033	0,0009	0,0014	0,1281	0,0014	0,0050	0,0004	0,0011	0,0160	0,0000	0,0015	0,00022	0,0000
DN	0.0016	0,0181	1,0903	0,0002	0,0115	0.0234	0,0120	0,0024	0,0030	0,0029	0.0005	0,0042	0.0029	0,0165	0,0000
23	0.0081	0,0068	0,0153	1,6235	0,0276	0,1873	0,0388	0,0249	0,0126	0,0131	0.0346	0,0247	0,0187	0,0686	0,0000
FF	0.0070	0,0046	0,0106	0,0097	1,3710	0,1694	0,0129	0.0376	0,0139	0.0536	0.0005	0.0060	0.0096	0.0410	0,0000
99	0.0031	0,0017	0,0037	0,0044	0,0063	1,1568	0,0063	0,0239	0,0029	0,0102	0,0067	0,0031	0.0072	0.0062	0,0000
нн	0.0062	0,0030	0,0070	0,0056	0,0066	0,1588	1,0090	0,0237	0,0119	0,0130	0.0172	0,0065	0.0209	0,0193	0,0000
1	0,0162	0,0060	0,0218	0,0375	0,0261	0,7198	0,0254	1,2894	0,0370	0,0380	0,0455	0,0263	0,0224	0,1324	0,0000
ш	0.0174	0,0117	0,0261	0,0548	0,0518	0.4590	0,0400	0,0611	1,1038	0,1009	0.0070	0,0146	0.0283	0,0604	0,0000
KK .	0.0432	0,0252	0,0378	0,1140	0,0789	1,5410	0,1030	0,1530	0,2498	1,2435	0,0899	0,0721	0,1085	0,2315	0,0000
LL	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	1,0000	0,0000	0,0000	0,0000	0,0000
NM	0.0018	0,0012	0,0011	0,0018	0,0008	0.0124	0,0011	0,0018	0,0018	0,0014	0.0025	1,0066	8000.0	0,0011	0,0000
NN	0.0004	0,0002	0,0002	0,0003	0,0007	0.0041	0,0010	0,0006	0,0001	0,0003	0.0011	0,0004	1,0839	0,0004	0,0000
00	0,0012	0,0010	0,0066	0,0009	0,0025	0.0695	0,0074	0,0125	0,0035	0,0209	0.0057	0,0106	0.0098	1,1330	0,0000
P.P.	0.0000	0,0000	0,0000	0,0000	0,0000	0.0000	0,0000	0,0000	0,0000	0,0000	0.0000	0,0000	0,0000	0,0000	1,0000
AA	0.0012	0,0009	0,0161	0,0007	0,0066	0.0296	0,0667	0,0031	0,0017	0,0036	0.0022	0,0020	0.0179	0.0052	0,0000
88	0.0000	0,0000	0.0000	0,0000	0,0000	0.0008	0,0048	0,0001	0,0001	0,0001	0.0001	0,0000	0.0001	0,0001	0,0000
GAGB DA	0.0009	0.0006	0,0030	0.0374	0.0121	0.0100	0,0028	0,0001	0.0007	0.0014	0.0027	0.0012	0.0048	0.0031	0,0000
DP.	0.0009	0.0000	0.0021	0,0006	0.0001	-0.0005	0,1930	0.0031	0.0018	0.00022	0.0019	0.0000	0.0284	0.0026	0.0000
00	0.0002	0.0000	0.5022	0,0000	0.0024	0.0001	0.00076	0.5000	0,0002	6,0000	0.0015	0.0000	0.0101	0.0040	3,0000
00	0.00012	0.0004	0.0768	-0.0013	0.0456	0.0112	0,0001	0.5017	0.0005	0.0008	0.0005	0.0000	0.0000	0.0063	8.0355
DE	0.00%9	D.0027	0.0105	0.0040	0.0019	0.1330	0.0121	0.0180	0.0136	0.0216	0.0034	0.0128	0.0083	0.0248	0.0000
DF	0.0014	DOCIDE OF	0.0042	0.0257	0.0178	0.0519	0000001	0.0275	0.0015	1001053	0.0093	1001050	0.0217	Intellos	0100000
DC	0.0077	0.00020	0.0127	0.0017	0.0155	-0.0502	0.0041	0.0003	0.0007	0.00019	0.0009	0.00015	0.0397	0.00022	0.0000
DH	010800	1000000	0,0179	0,0013	0,0050	0.0474	MODELS	0,0040	0,0007	1001063	0.0013	1004000	DIONN	1000001	10,0000
DI	0.0035	000000	0,0000	-0,0050	0,1477	0.0419	O/MAN D	0,0007	0,0017	LODICO1	0.0017	DOGE	01008b	000630	0,0000
DJ	0.0037	LODIES:	0,0059	0,0026	0,0770	0,1121	0,01100	0,0000	0,0019	1001010	0.0025	<b>D</b> EGIS	0.0031	1001000	10,0000
DK	0.0012	0,0038	0.0007	0,0017	0,0112	0.0103	0,0027	0,0007	0,0002	0,0010	0.0015	0,0004	0.0014	0.0008	0,0000
DL	0.5030	0,0164	-0.0007	0,0116	0,0123	-0.0346	0,0048	0.0205	0,0031	0,0018	0.0027	0,0017	0.0075	0.0090	0,0000
DM	-0.0013	0,4444	-0.0015	0,0001	-0.0006	0.0395	0,0001	-0,0044	-0,0001	0.0000	0.0057	0.0001	0.0003	0.0000	0,0000
DN	0.0003	0,0094	0,6097	-0,0001	0,0062	0.0017	0,0065	0,0010	0,0016	0,0014	0.0047	0.0022	0.0015	0,0044	0,0000
EE	0.0082	0,0070	0,0167	1,6684	0,0285	0,1923	0,0366	0,0256	0,0130	0,0136	0.0290	0,0254	0.0192	0,0705	0,0000
FF	0.0063	0,0038	0,0094	-0,0512	1,3489	0,1447	0,0101	0,0218	0,0125	0,0488	-0.0247	0,0063	0.0081	0,0357	0,0000
88	0.0174	0,0033	0,0135	0,0181	0,0487	7,4839	0,0384	0,1502	0,0164	0,0517	0.0434	0,0170	0.0432	0,0406	0,0000
нн	0.0056	0,0027	0,0064	0,0052	0,0060	0.1445	0,9199	D,0215	0,0108	0,0118	0.0097	0,0047	0,0153	0,0152	0,0000
-	0.01-45	0,0017	0,0209	0,0342	0,0260	0.6902	0,0245	1,2367	0,0355	0,0384	0.0416	0,0255	0.0214	0,1269	0,0000
11	0.0168	0,0113	0,0252	0,0529	0,0500	0,4388	0,0388	0,0661	1,0673	0,09/5	0.0067	0,0140	0.0273	0,0580	0,0000
KK .	0.0321	0,0193	0,0005	0,0346	0,0503	0.9029	0,0745	0,0941	0,1241	1,1262	-0.0645	0,0539	0.0079	0,1004	0,0000
LL	0.0000	Distant	0,0000	0,0000	0,0000	0.0000	0,0000	0,0000	0,0000	0,0000	1,1964	D/GEED	0,0000	0,0000	0,0000
NW	0.0019	0,0012	0,0011	0,0018	0,0008	0.004	0,0011	0,0018	0,0018	0,0014	0.00022	1/0167	0.0008	0,0011	0,0000
NN CO	0.0004	0,0000	0.0002	0,0003	0,0007	0.0041	0,0010	0.0006	0.0001	0,00003	0.0005	DOCOM	Central Contral	D.GLUM	0,0000
00	0.0011	D.GLAN	0.0000	0.0110	0,0001	0.0000	0.0000	0.0000	0.00012	0.0160	0.00007	Digitality of the local distance of the loca	0.0000	1,00.31	1 0 0 0 0 0
P P	0,0000	0,0000	0,0000	0,0000	0,0000	0.0000	0,0000	0,0000	0.000	LUUUUU	U LULU	DUDUUU	U LLLLU	LUGULUU	1,14,000

## Annex A.2 – Partitioned matrix inverse: CTA (results from the rectangular M&U model with total flows at *pp*) (cont.)

#### AC8 DВ 0.004 0.01 0.15 0.00 0.4 0.0 0.00 0.047 000 0.0002 0.00 0.00 0.000.0040 0.0 0.0 CAC 0.0141 0.0240 0.1145 0.0119 0.0062 0.0057 0.8448 0.033 0.01 0.048 **a**cc: 0.0100.008 008 0.64 0.0 0.0172 0.00 0.001 0.003 0.0131 0.0 0.02 0.090 0.0169 0.012 0.0223 0.036 221730.02 0.1341 0.00 0.0 0.074 0.003 0.006 0.012 0.000 0.01 0.00 0.0 0.00 0.02 0.00 0.00 0.002 0.0 0.00 0.0410.007 0.0014 0.007 0.00 0.0016 0.001 0.022 0.0343 0.040 0.013 0.02 0.012 0.0140.014 0.01 0.07 0.01 0.028 0.004 0.006 0.013 diab 0.00 0.011 0.013 0.070 0.0487 0.041 0.02 0.028 0.025 0.005 0.045/ 0.0477 0.0471 0.0570 0.0156 0.08 0.08 127 0.071 0.16 0.0940.00 0.00 0.002 0.0014 0.002 0.0 0.0013 0.001 0.0 0.0047 0.0021 0.0031 0043 0.0042 0.0011 0.00 5041 0.000 0.000 **DOM:** 0.0000 200 10000 0.0000 0.000 0.000 0.0000 0.000 0.002 1.1412 0.00 0.0 D DC 0.007 1.019 0.0001 0.0001 0.0001 0.0002 0.0017 0.0001 0.0000 0.00 0.005 0.0034 0.0014 0.002 A 0.002 0.00 0 D D07 1.0035 0,1071 0,0045 0.002 0.0034 0.0257 0.0080 0.0004 0.0064 0.0016 0.002 0.002 0.0044 0.004 001 1.354 0.0346 0.009 0.007 0.000/ 0.000 0.0003 0.000 -0.000 0.0001 000 0.0013 0.000 0.0 0.001 0.004 0.000 0.000 0.0 0.0103 0.014 0.0140.0373 0.0114 0.022 0.02 0.025 0.018 0.01640.0108 0.00 064 0.006 0.0 0.003 0,0180 -0,0000 0.0138 0.0113 0.0291 0.0260 0.1550 0.0245 0.0311 0.0373 1.1656 0.022 0.0180 0.009 0.0 0.001 0.0140.028 0.0 0.000.0 0.002 0.003 0.01 0.0184 0.005 0.0060 009 0.0191 0.0070 0.017 0.0032 0.0173 0.0470.0094 0.0019 0.002 0.003 0.002 0.0017 0.000 0.000 0.0010 0.0033 0.016 0.0169 0.0011 0.0007 0.000 5.002 0.0010 0.0011 0.000 0.001 0.001 0.0006 0.0018 0.003 0.003 0.002 0.0000 .000 -0.000 0.000 -0.00100 0.000 D D000 0.0046 000 0.000 0.0003 0.000 0.002 0.0017 0.0116 0.0147 0,0357 0.023 0.1120.0318 0.042 0.073 0.0247 0.0450 0.0384 0.113 0.0202 0.011 0.0184 0.012 0.015 0.01 0.0190 0.0124 0.1843 0.0752 0.0440 0.0354 0.073 0.057 0.0294 0.055-0.036 0.0305 0.012 0.0 0.067 0.024 0.026 D D 46 0.039 0.063 0.0460 0.04 0.01 0.0430.05 0.0613 0.02 0.0000 0.000 000 0.0000 0.0000 0.0000 0.000/ 0.0000 0.0000 0.0000 0.000 0.0000 0.0 0.00 0.0 0.0041 0.0021 001 0.0019 0.0013 0.0013 002 0.0001 0.0003 0.0005 0.0003 0.001 0.0001 0.0 0.0043 0036 0.0037 0.0 0.0025 0026 0.0048 0.0009 0.00 0.0022 003 0.00 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000



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# Annex A.2 – Partitioned matrix inverse: CTA (results from the rectangular M&U model with total flows at pp) (cont.)

	D	DM -	DN	EE.	EE .	88				KK .		00	D.D.	00	00
4.6	0.0042	0.0035	0.0452	0.0016	0.0136	0.0096	0.1035	0.0049	0.0030	0.0056	0.0052	0.0026	0.0255	0.0035	0.0000
RR	0.0002	0.0001	0.0002	0.0001	0.0001	0.0003	0.0128	0.0003	0.0002	0.00002	0.0002	0.0001	0.0003	0.0003	0.0000
CACB	0.0057	0.0087	0.0226	0.1517	0.0506	0.0111	0.0127	0.0272	0.0034	0.0054	0.0128	0.0049	0.0199	0.0165	0.0000
DA	0,0052	0,0031	0,0116	0,0021	0,0040	0,0111	0,3246	0.0052	0.0045	0.0056	0.0112	0.0022	0.0567	DICONS.	0.0000
DB	0,0135	0.0148	0,021212	0,0012	0,0046	0,00011	0,0146	0,0028	0.0007	0.0014	010034	0.0010	0.0173	Lilcost/	0.0000
DC	0,0016	0,0009	0,0234	0,0000	0,0001	0,0003	0,0002	0,0002	0.0001	0,0004	0.0002	0.0001	0,0001	0.0008	0.0000
DD	0,0054	0,0085	0,1890	0,0007	0,0572	0,0064	0,0043	0,0034	0,0016	0,0042	0.0025	0.0013	0,0013	0.0120	0.00000
DE	0,0221	0,0118	0,0093	0,0113	0,0126	0,0355	0,0207	0,0254	0,0245	0,0372	0.0158	0.0196	0,0128	0.0414	0.0000
DF	0,0118	0.0032	0,0267	0,0874	0,0616	0,0294	0,0269	0,0365	0,0065	0,0147	0.0307	0.0102	0.0732	0.0377	0.0000
DG	0,0567	0,0310	0,0725	0,0120	0,0428	0,0217	0,0156	0,0105	0.0036	0.0095	0.0069	0.0044	0,1139	0.0300	0.0000
DH	0,1293	0,0434	0,0650	0,0037	0,0150	0,0189	0,0090	0,0099	0.0028	0,0100	0.0037	0.0017	0.0053	0.0083	0.0000
DI	0,0091	0,0242	0,0202	0,0021	0,1962	0,0058	0,0191	0,0079	0,0032	0,009/	0.0075	0.0025	0,0032	0.0077	0.0000
50	0,1631	0,1777	0,1305	0,0100	0,1364	0,0500	0.0000	0,0156	0.0014	0.00037	D DUSC	0.0014	0.0000	0.0035	0.0000
N.	0,0100	0.1108	0.0000	0,0005	0.0353	0.0319	0.0549	0.0579	0.0096	0.0110	0.0090	0.0050	0.0156	0.0255	0.0000
DM DM	0.0054	0.4787	0.0005	0.0011	0.0015	0.0201	0.0017	0.0076	0.0005	0.0014	0.0090	0.00007	0.0015	0.0022	0.0000
DN	0.0039	0.0483	0.1631	0.0008	0.0118	0.0042	0.0132	0.0029	0.0034	0.0032	0.0030	0.0042	0.0029	0.0184	0.0000
11	0.0196	DOGINA	DODGEN	0.0000	DODAS	DOMENT	DIDENSI	DIDNEY	0.055	DEGISIO	DOMS	DIST	DUGINE	10107651	DIOXC
FF	0.0174	0.0105	000308	0.0230	0,3773	DOBIO	0.0152	0.0450	0.0200	0.0397	0.0156	0.0039	0.0090	0.0499	0.0000
88	0.0077	0.0049	0.0072	0.0050	0.0097	0.0252	0.0095	0.0254	0.0040	0.0114	0.0073	0.0032	0.0073	0.0106	0.0000
HH	0,0150	0,0084	0,0135	0,0061	0,0070	0,0259	0,0103	0,0253	0.0137	0,0145	0.0165	0.0056	0.0209	0.0214	0.0000
1	0,0373	0.0233	0,0422	0,0398	0,0294	0,1153	0,0296	0,3035	0,0423	0,0429	0.0460	0.0265	0,0226	0.1441	0.0000
ш	0,0431	0,0329	0,0504	0,0570	0,0539	0,0789	0,0459	0,0676	0,1179	0,1111	0.0216	0,0156	0,0288	0.0688	0.0000
KK -	0,1067	0,0718	0,0749	0,1191	0,0835	0,2584	0,1187	0,1685	0.2839	0,2687	0,1128	0.0741	0,1097	0.2583	0.0000
LL	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
MM	0,0044	0,0032	0,0021	0,0018	0,0008	0,0021	0,0013	0,0019	0,0020	0,0015	0.0023	0,0065	0,0008	0.0013	0,0000
NN	0,0009	0,0005	0,0005	0,0003	0,0007	0,0007	0,0011	0,0006	0,0001	0,0004	0.0011	0.0004	0,0835	0.0004	0,0000
00	0,0032	0.0028	0,0120	0,0022	0,0027	0,0107	0,0085	0,0136	0,0059	0,0229	0.0039	0,0107	0,0067	0.1425	0.0000
pp	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0.0000	0,0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
<u>~~</u>	0,0030	0.0025	0,0321	0,0012	0,0097	0,0070	0,0735	0,0035	0.0021	0.0041	0.0004	0.0020	0,0101	0.0001	0.0000
0400	0.0001	0.0000	0.0001	0.0000	0.0000	0.0001	0.0052	0,0001	0.0001	0.0016	0.0001	0.0043	0.0001	0.0001	0.0000
DA DA	0.0014	0.0016	0.0000	0,0000	0.00123	0.0021	0.1854	0.0000	0.0000	0.0016	0.0051	0.0012	0.0040	0.0040	0.0000
D8	0.0077	0.0079	0.0605	0.0006	0.0024	0.0021	0.0054	0.0014	0.0005	0.0007	0.0015	0.0005	0.0101	0.0055	0.0000
DC	0.0007	0,0005	0.0141	0.0000	0.0000	0.0001	0.0001	0.0000	0.0001	0.0002	0.0001	0.00000	0.0000	0.0004	0.0000
DD	0.0042	0.0096	0.1502	0.0006	0.0463	0.0049	0.0033	0.0024	0.0013	0.0032	0.0019	0.0010	0.0010	0.0095	0.0000
DE	0.0143	0.0078	0,0198	0,0075	0,0063	0,0236	0,0138	0,0196	0.0163	0.0248	0.0105	0.0132	0.0085	0.0277	0.0000
DF	0,0035	0,0027	0,0079	0,0258	0,0182	0,0087	0,0079	0,0291	0,0020	0,0044	0,0091	0,0030	0,0216	0.0111	0,0000
DG	0,0189	0,0103	0,0247	0,0025	0,0135	0,0055	0,0045	0,0005	0,0010	0,0024	0.0015	0.0012	0,0395	0.0095	0.0000
DH	0,0686	0.0223	0,0336	0,0017	0,0092	0,0084	0,0044	0,0048	0.0009	0.0047	0.0017	0.0007	0.0022	0.0037	0.00000
DI	0,0068	0,0185	0,0153	0,0006	0,1506	0,0074	0,0146	0,0058	0.0024	0,0074	0,0055	0.0017	0,0023	0.0058	0.0000
DJ	0,0940	0,1005	0,0736	0,0056	0,0750	0,0207	0,0113	0,0087	0,0028	0,0094	0.0050	0.0021	0,0051	0.0094	0.0000
DK	0,0052	0,0145	0,0025	0,0021	0,0126	0,0029	0,0030	0,0010	0,0004	0,0012	0.0016	0.0004	0,0014	0,0010	0.0000
DL DH	1,2050	0.0451	0,0017	0,0118	0,0125	0,0108	0,0052	0,0218	0.0004	0.0000	0.0040	0.00017	0.0075	0.0004	0.0000
DN	0.0022	0.0290	1.0694	0.0001	0.0053	0.0004	0.0002	0.0013	0.0018	0.0015	0.0048	0.0001	0.0015	0.0094	0.0000
EFF FFF	0.0013	0.0280	0.0305	1,0003	0,0000	0.0015	0.0442	0.0013	0.0016	0.0015	0.0045	0.0022	0.0015	0.0094	0.0000
77	0.0156	0.0117	0.001-0	0.0001	1,3050	Disku	0.0125	0.0305	0.0150	0.0571	0.0132	0.0035	0.0055	0.0402	0.0000
GG	0.0455	0.0254	0.0397	0.0268	0.0551	1,1586	0.0565	0.1609	0.0225	0.0099	0.0452	0.0188	0.0446	0.0020	0.0000
HH	0.0137	0.0076	0.0123	0.0056	0.0063	0.0236	1.0094	0.0230	0.0124	0.0131	0.0150	0.0051	0.0187	0.0192	0.0000
1	0,0358	0.0223	0.0404	0,0375	0,0282	0,1105	0,0283	1,2911	0.0406	0.0411	0.0441	0.0255	0.0217	0.1381	0.0000
11	0,0416	0.0518	0,0485	0,0550	0,0520	O)ONEO	0,0445	0,054-4	1,1130	0,1075	0.0207	0.0150	0,0275	0.0661	0.0000
KK .	0.0670	DISCH	0.0576	0,0954	0,0017	0.2153	0,0976	DARGO	0.2464	1,2293	0.0904	0.000is	0.0324	0.2077	0.0000
LL	0.0000	0.0000	0.0000	0,0000	0,0000	0,0000	0,0000	0,0000	0.0000	0.0000	1,0000	0.0000	0.0000	0.0000	0.0000
MM	0,0045	0,0032	0,0022	0,0018	0,0008	0,0021	0,0013	0,0019	0,0020	0,0016	0.0024	1,0066	0,0006	0.0013	0.0000
NN	0,0009	0,0006	0,0005	0,0003	0,0007	0,0007	0,0011	0,0006	0,0001	0,0004	0,0011	0,0004	1,0839	0.0004	0,0000
00	0,0028	0.0025	0,0110	-0,0024	0,0024	0,0098	0,0077	0,0126	0.0054	0,0214	0.0081	0.0099	0,0061	1,1333	0.0000
pp	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0.0000	0,0000	0.0000	0.0000	0.0000	0.0000	1,0000

### Annex A.3 – Domestic flow bp product-by-product inverse matrix: ITA (symmetric model)

		00	22.8	29	INA.	20	NA	155	00	00	100	104	IN .	<b>N</b> 1	NY 1
	0.00	0.000	0.0000	0.0000	LPH D TREAM	0.0040	D.CONT.	0.7979	UC DETE	LF D/2000	0.0000	O DOM:	0.0063	0.0047	0.0000
20	0.00010	4,0400	0.0000	0,0004	0.2000	0.0004	COURT OF	0,2305	0.0004	0,0000	0,0003	0.0004	0,000	C DOM	0.0000
00	0.0000	1,9100	1,0000	0.0004	0.0000	0.0001	5,0000	0.0000	0,0001	0.0000	0.0004	0,0000	0.0000	0.0001	50000
29	0,0000	0,0000	0.0000	1.0/20	0.0000	0.0000	0,0000	0,0000	0,0000	0,0005	0,0001	0.0000	0.0000	0.0002	0.0000
04	0.4436	0,0005	0,0000	0.0004	4.4888	0.0054	0,0007	0,0014	0.0447	0,0004	0,0003	0.0008	0,1085	0.0003	0.0027
100	0.0047	0.0052	0.0000	0.0040	0.0021	1 2000	0.0000	D.COLLET	0.0004	0.0000	0.0000	0.0400	0.0004	0.0040	0.0024
00	0.0000	0.0004	0.0000	0.0005	0.0004	0.0049	1.0004	0.0000	0.0000	0.0000	0,0004	0.0000	0.0004	0.0004	5.0021
~~	0,0002	0,0001	0,0000	0.0001	0.0001	0.0042	0,0009	1.3601	0,0000	0,0000	0.0001	0.0020	0,0001	0.0111	0.0002
22	0.0942	0.0048	0,0000	0.0001	D.COME	0.0047	0,00204	0,0000	4,0004	0,00043	0,0002	0.0040	0,0104	C D451	0.0000
12	0.0000	0,0040	0.0000	0.0500	0.0000	0.0040	0,0004	0.0000	0.0040	1,00.07	0.0046	0.0210	0.04.40	0.0761	0.0040
02	0,0000	0,0040	0.0000	0.0000	0.0000	0.0040	0,0004	0,0000	0,0040	0.0949	1.1454	0.1972	0,0146	0.0492	0.0045
22	0.0700	0,0035	0,0000	0.0005	0.0121	0.0008	0,0202	0,0230	0.0002	0,0045	0.0054	1 0/10/1	0,0094	0.0141	0.0100
01	0.0002	0,0019	0,0000	0,0001	0,0155	0,0000	5,0005	0,0001	0,0001	0,0005	0.0003	0.0004	1.1104	0.0404	0.0202
01	0.0090	0.0057	0.0000	0.0000	0.0180	0.0042	0.0472	0.0477	0.0000	0.0017	0.0430	0.0490	0.0220	1,2004	0.0175
~	0,0000	0,0007	0,000	0.0049	0.0102	0.0001	0,0172	0,0094	0,0000	0,0017	0.0010	0.0462	0.0022	0.0002	1,1014
0	0.0004	0,0024	0,0000	0.0040	0,0027	0.0000	0,0015	0,0031	0,0025	0,0004	0,0035	0.0068	0,0171	0.0004	0.00001
044	0,0021	0,0000	0.0000	C CONT	0.0007	0,0000	0,0000	0,000	0.0007	0,000	0,0041	0,0000	0,0001	0,0004	0,0001
000	0.0000	0.00028	0.0000	0.0000	0.0045	0.0442	0.0000	0.0005	0.0007	0.0001	0.0006	0.0043	0.0000	0.0452	0.0004
014	0.000	0.0008	0.0000	0.10/0	0.0010	0.0985	0.0023	0,0000	0,0000	0,0001	0,0021	0.0840	0,0023	0.0900	0.0030
110	0.0021	0,0209	0.0000	O TONO	D (T244	0.0887	0.0217	0,0011	0.0004	0,0007	0,0003	0.0042	0,1007	0.000	0.0203
00	0.0240	0.4994	0.0000	0.1420	0.0477	0.0130	0.0173	0.0504	0.0440	0,000	0.0004	0.0494	0.0042	0.0540	0.00900
30	0.0000	0.001	0.0000	0.0128	0.04/7	0.0414	0.0408	0.05034	0.0007	0.0000	0.0603	0.0002	0.0818	0.0140	0.0496
1	0.0000	0,0110	0,0000	0.1100	0,0004	0.07920	0,0106	0,0105	0.0607	0,0006	0.0482	0.0007	0,0130	0.042	0.0125
	0.0440	0.0007	0.0000	0,1109	0.0456	0.000	0,000	0.0000	0.0400	0,0054	0.0402	0,000	0,0710	0.000	0.0070
33	C Den3	0,006/	0,0000	0.0800	0,0400	0.0460	0,0412	0,0693	0,0469	0,0091	0,0403	C DHID	0,0516	0.03/1	0,0807
NK.	0,0718	0,0760	0,0000	0,1159	0,1101	0.0704	0,0660	0,0720	0,1000	0,0077	0,1405	0,0000	0,0507	0.0724	0,0059
100	0,0000	0,000	0,0000	0.0000	0.0000	0,0000	0.000	0.000	0,000	0,000	0,0000	0,000	0,000	0,000	0,000
	0,0006	0,0024	0,0000	0,0014	0,0015	0.0013	0,0014	0,0014	0,0021	0,0001	0,0023	0,0022	0,0022	0.0023	0.0021
1919	0.0041	0,0021	0,0000	0.0014	0,0019	0.0003	0,0012	0,0025	0,0005	0,000	0,0005	0.0007	0,0011	0.0002	0,0016
00	0.0000	0,0040	0.0000	0.0004	0,000	0.0002	0,000	0,0031	0,0001	0,000	0.0000	0.000	D.0000	0.0007	0.0000
S1184	1,0000	1.6100	1,0000	4 9499	1 9415	1 2642	1 7940	2,0000	5,0000	1.93.00	1,0000	1,6192	1,9614	4 7999	1,0000
OUM	1,0027	1,0100	1,000	1,7422	1,0410	1,7812	1,1040	4,4100	1,7814	1,1046	1,0000	1,0127	1,0014	1,1409	1,6299
	~	-	200	ee.	icc.	20	LUL I			22		1.014	N.K.	20	00
	DL.	DM 0.0000	ON 0.000	EE	FF	33	HH	11	JU	KK.	11	MM	NN DOMO	00	pp
A.A.	OL 0,0035	DM 0,0026	0N 0,0308	EE 0,0015	FF 0,0088	33	HH 0,0683	0,0039	JU 0,0024	KK 0,0057	0,0036	0.0000	NN 0,0169	00	0,0000
AA 99	0L 0,0035 0,0001	DM 0,0028 0.0000	DN 0,0308 0,0001	EE 0,0015 0,0000	FF 0,0088 0,0000	0.0092 0.0092	HH 0,0883 0,0050	11 0,0039 10000	JU 0,0004 0,000H	KK 0,0057 0.000H	LL 0,0036 0,000H	VIM 0,0020 0,0000	NN 0,0169 0,0001	00000	PP 0,0000 0,0000
AA BB CA	0,0035 0,0001 0,0000	DM 0,0028 0,0000 0,0000	DN 0,0308 0,0001 0,0000	EE 0,0015 0,0000 0,0001	FF 0,0088 0,0000 0,0000	33 0,0092 0,0002 0,0000	HH 0,0883 0,0050 0,0000	0,0000 0,0000 0,0000	JU 0,0004 0,0001 0,0000	KK 0,0057 0,000H 0,0000	LL 0,0036 0,0001 0,0000	MM 0,0020 0,0000 0,0000	NN 0,0159 0,0001 0,0000	000000	PP 0.0000 0.0000 0.0000
	DL 0,0035 0,0001 0,0000 0,0011	DM 0,0028 0,0000 0,0000 0,0022	DN 0,0308 0,0001 0,0000 0,0105	EE 0,0015 0,0001 0,0001 0,0011	FF 0.0088 0.0000 0.0000 0.0000	33 0,0092 0,0002 0,0000 0,0000	HH 0,0883 0,0050 0,0000 0,0002	0,0039 0,0001 0,0000 0,0000	0,0004 0,0001 0,0000 0,0000	KK 0,0057 0,0001 0,0000 0,0017	LL 0,0036 0,000H 0,0000 0,0019	MM 0,0020 0,0000 0,0000 0,0004	NN 0.0159 0.0001 0.0000 0.0007	00 0,0080 0,0001 0,0000 0,0013	PP 0.0000 0.0000 0.0000 0.0000
	DL 0,0009 0,0000 0,0000 0,0001 0,0002	DM 0,0028 0,0000 0,0000 0,0022 0,0029	DN 0,0008 0,0000 0,0000 0,0105 0,0064	EE 0,0015 0,0000 0,0001 0,0011 0,0014	FF 0,0088 0,0000 0,0000 0,0000 0,0048 0,0004	33 0,0092 0,0002 0,0000 0,0019 0,0019	HH 0,0883 0,0050 0,0000 0,0002 0,1682 0,1682	II 0,0039 0,0000 0,0000 0,0013 0,0047	JU 0,0004 0,0000 0,0000 0,0005 0,0007	KK 0,0057 0,0000 0,0000 0,0017 0,0048	1. 0,0036 0,0001 0,0000 0,0019 0,0050	MM 0,0000 0,0000 0,0000 0,0004 0,0004	NN 0,0159 0,0004 0,0007 0,0007 0,0007	0,0000 0,0000 0,0000 0,0000 0,0003 0,0045	PP 0.0000 0.0000 0.0000 0.0000
	DL 0,0005 0,0000 0,0000 0,0001 0,0002 0,0079	DM 0.0000 0.0000 0.0000 0.0002 0.0019 0.0090	DN 0,0001 0,0001 0,0000 0,0105 0,0064 0,0660	EE 0,0015 0,0001 0,0011 0,0011 0,0014 0,0014 0,0000	FF 0,0088 0,0000 0,0000 0,0248 0,0026 0,0007	33 0,0002 0,0002 0,0000 0,0078 0,0078 0,0078	HH 0,0885 0,0050 0,0002 0,0022 0,1682 0,0087	II 0,0039 0,0000 0,0000 0,0013 0,0047 0,0020	JU 0,0004 0,0000 0,0000 0,0005 0,0005 0,0005	KK 0,0057 0,0001 0,0000 0,0017 0,0048 0,0047	L. 0,0036 0,0001 0,0000 0,0019 0,0060 0,0022	MM 0,0020 0,0000 0,0000 0,0004 0,0004 0,0007 0,0007	NN 0,0159 0,0001 0,0007 0,0007 0,0007 0,0007 0,0000	0,0000 0,0000 0,0000 0,0000 0,0003 0,0005 0,0005	PP 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
	DL 0,0001 0,0001 0,0000 0,0011 0,0002 0,0011 0,0011	DM 0,0000 0,0000 0,0000 0,0002 0,0000 0,0000 0,0006 0,0006	DN 0,0005 0,0005 0,0105 0,0105 0,0105 0,0134 0,0134	EE 0,0015 0,0001 0,0001 0,0011 0,0014 0,0010 0,0001	FF 0,0088 0,0000 0,0000 0,0048 0,0026 0,0001 0,0002 0,0002	33 0,0092 0,0002 0,0000 0,0019 0,0019 0,0005 0,0005	HH 0.0883 0.0050 0.0000 0.0022 0.1682 0.0067 0.0002	11 0,0009 0,0001 0,0000 0,0013 0,0047 0,0020 0,0002	JU 0,0004 0,0000 0,0000 0,0005 0,0005 0,0005 0,0001	KK 0,0057 0,0001 0,0000 0,0017 0,0048 0,0017 0,0003 0,0003	L. 0,0036 0,0001 0,0009 0,0009 0,0022 0,0002 0,0002	MM Q 0000 Q 0000 Q 0000 Q 0004 Q 0004 Q 0007 Q 0007	NN 0,0169 0,0001 0,0007 0,0007 0,0007 0,0001 0,0001	CO Q.0050 Q.0000 Q.0013 Q.0045 Q.0055 Q.0005	PP 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
	DL 0,000H 0,000H 0,0000 0,001H 0,0002 0,0079 0,001H 0,000H 0,000H	DM 0.0028 0.0000 0.0000 0.0022 0.0019 0.0080 0.0086 0.0098	DN 0,0000 0,0000 0,0105 0,0064 0,0663 0,0134 0,0134 0,0437	EE 0,0015 0,0001 0,0001 0,0011 0,0014 0,0010 0,0001 0,0001 0,0001	FF 0.0088 0.0000 0.0000 0.0248 0.0026 0.0001 0.0002 0.0002 0.0423	33 0,0092 0,0002 0,0000 0,0019 0,0019 0,0019 0,0019 0,0005 0,00052 0,00052	HH 0.0883 0.0050 0.0000 0.0022 0.1682 0.0087 0.0002 0.0002 0.0002	11 0,0039 0,0001 0,0000 0,0013 0,0047 0,0020 0,0020 0,0020	JU 0,0004 0,0000 0,0006 0,0006 0,0006 0,0001 0,0001 0,0005 0,0001	KK 0,0057 0,0001 0,0000 0,0017 0,0048 0,0017 0,0003 0,0003 0,0003	LL 0,0036 0,0001 0,0000 0,0019 0,0060 0,0052 0,0052 0,0052 0,0052 0,0052	MM Q 0000 Q 0000 Q 0000 Q 0004 Q 0004 Q 0004 Q 0007 Q 0007 Q 0007	NN 0,0169 0,0001 0,0007 0,0007 0,0007 0,0001 0,0001 0,0001 0,0001	CO Q 0080 Q 0001 Q 0003 Q 0045 Q 0059 Q 0005 Q 0005 Q 0005	PP 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
	DL 0,0005 0,0001 0,0001 0,0002 0,0079 0,0079 0,0079 0,0079	DM 0,0028 0,0000 0,0000 0,0002 0,0008 0,0080 0,0088 0,0088 0,0088	DN 0,0308 0,0001 0,0000 0,0105 0,0064 0,0680 0,0134 0,0188 0,01989	EE 0.0015 0.0001 0.0011 0.0014 0.0014 0.0016 0.0016 0.0016 0.0016	FF 0.0088 0.0000 0.0248 0.0026 0.0026 0.0026 0.0002 0.0425 0.0002 0.0425	00 00000 0000 0000 0000 0000 0000 0000 0000 0000 0000 0000 0	HH 0,0883 0,0850 0,0000 0,0002 0,0002 0,0007 0,0002 0,0002 0,0002 0,0002 0,0002	II 0,0039 0,0001 0,0015 0,0047 0,0020 0,0002 0,0002 0,0002 0,0002 0,0002 0,0002 0,0002	JU 0,0004 0,0006 0,0006 0,0007 0,0006 0,0001 0,0001 0,0005 0,0055	KK 0,00257 0,0000 0,00017 0,0004 0,0004 0,0003 0,0003 0,0003 0,0003 0,0003	LL 0,0036 0,0001 0,0000 0,0002 0,0002 0,0002 0,0002 0,0002 0,0002	MM 0,0021 0,0000 0,0004 0,0004 0,0004 0,0007 0,0007 0,0007 0,0007 0,0007 0,0007	NN 0,0159 0,0001 0,0007 0,0007 0,0007 0,0001 0,0012 0,0001 0,0012	C/O C 0000 C 0000 C 0000 C 0005 C 0005 C 0005 C 0005 C 0005 C 0005	PP 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
	DL 0,0005 0,0001 0,0000 0,0001 0,0002 0,0079 0,0079 0,0079 0,0079 0,0079 0,0079	DM 0,0028 0,0000 0,0000 0,0022 0,0019 0,0080 0,0086 0,0084 0,0084 0,0084	DN 0,0008 0,0000 0,0006 0,0064 0,0660 0,0660 0,0663 0,0660 0,0758 0,0076 0,07758	EE 0.0076 0.0007 0.00071 0.0074 0.0076 0.0076 0.00772 0.0072	FF 1,0088 1,0000 1,0000 1,0008 1,0000 1,0008 1,0002 1,0403 1,0002 1,0403 1,0002 1,0403 1,0002 1,0008 1,	033 0,0052 0,0002 0,0009 0,0009 0,0009 0,0005 0,0052 0,0052 0,0052 0,0052 0,0052	HH 0.0883 0.0000 0.0002 0.0002 0.0002 0.0009 0.0009 0.0009 0.0009 0.0009 0.0009	11 0.0009 0.0007 0.0007 0.0005 0.0005 0.0005 0.0005 0.0005 0.0005 0.0005 0.0005 0.0005 0.0005	JJ 0,0004 0,0000 0,0006 0,0007 0,0006 0,0007 0,0005 0,0005 0,0075 0,0022	KK 0.0057 0.000H 0.0007 0.0046 0.0047 0.0003 0.0059 0.0051 0.0051	L 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.000	MM Q 0002 Q 0000 Q 0004 Q 0004 Q 0004 Q 0004 Q 0004 Q 0004 Q 0004 Q 0004 Q 0004 Q 0007 Q 0007 Q 0007 Q 0000 Q 000 Q 00	NN D,0169 D,0007 D,0007 D,0007 D,0007 D,0007 D,0007 D,0007 D,0007 D,0007 D,0007 D,0007 D,0007	CO Q 0000 Q 0004 Q 0004 Q 0005 Q 0055 Q	PP 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
	DL 0,0005 0,0001 0,0000 0,0011 0,0012 0,0011 0,0014 0,0014 0,0014 0,0014 0,0015 0,0016 0,0176 0,0176 0,0176	DM 0,0028 0,0000 0,0000 0,0022 0,0019 0,0060 0,0066 0,0068 0,0068 0,0068 0,0068 0,0068 0,0068 0,0068	DN 0,0308 0,0001 0,0000 0,0105 0,0064 0,0643 0,0754 0,0759 0,0075 0,0075	EE 0,0075 0,0007 0,0071 0,0074 0,0076 0,0076 0,0076 0,0075 0,0075 0,0072	FF 0,0008 0,0000 0,	C3C 0 0052 0 0002 0 0000 0 0009 0 0009 0 0005 0 005 0 0	HH 0.0883 0.000 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002	11 0,0009 0,0001 0,0000 0,0002 0,	JJ 0,0004 0,0000 0,0005 0,0005 0,0005 0,0005 0,0005 0,0005 0,0005 0,0005 0,0002 0,0002 0,0002	KK 0.0057 0.0004 0.0007 0.0047 0.0047 0.0003 0.0051 0.0051 0.0054 0.0054	L 1,000	MIM Q, 0000 Q, 0000 Q, 0004 Q, 0004 Q, 0004 Q, 0007 Q, 0007	NN D,01950 D,0000 D	C/O Q 0080 Q 0001 Q 0001 Q 0005 Q 0059 Q	PP 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
	DL 0,0005 0,0001 0,0000 0,0011 0,0002 0,0011 0,0048 0,0048 0,0048 0,0048 0,0048 0,0048 0,0048 0,0046 0,0046 0,0046 0,0046 0,0046 0,0046 0,0046 0,0048 0,	DM 0,0028 0,0000 0,0000 0,0000 0,0006 0,0006 0,0006 0,0006 0,0006 0,0006 0,0006 0,0006 0,0006 0,0006 0,0006 0,0007 0,0007 0,0007	DN 0,0001 0,0001 0,0000 0,0105 0,0064 0,0680 0,0184 0,0680 0,0184 0,0075 0,0085 0,0085 0,0085 0,0085	EE 0,0075 0,0007 0,0071 0,0074 0,0076 0,0076 0,0076 0,0076 0,0075 0,0075 0,0075 0,0075 0,0075 0,0075 0,0075	FF 0,0008 0,0000 0,0000 0,0008 0,0008 0,0008 0,0008 0,0008 0,0075 0,0175 0,0175 0,0175	CIC 0 0002 0 0002 0 0000 0 0009 0 0009 0 0009 0 0092 0 0092 0 0091 0 0091 0 0091 0 0091 0 0091 0 0094	HH 0.0883 0.0050 0.0002 0.1682 0.0067 0.0002 0.0055 0.0154 0.0057 0.0057 0.0057	11 0,0009 0,0001 0,0000 0,0015 0,0002 0,	JJ 0,0004 0,0000 0,0005 0,0005 0,0007 0,0005 0,	KK D,0057 0,0000 D,0017 D,0046 D,0077 D,0003 D,0039 D,0039 D,0031 D,0005 D,0051 D,0051 D,0051 D,0051 D,0051	L_ 0,0006 0,0001 0,0000 0,0000 0,0000 0,0000 0,0000 0,0000 0,0000 0,0000 0,0000 0,0000 0,0000 0,0000 0,0000	MIM Q, 0000 Q, 0000 Q, 0004 Q, 0004 Q, 0004 Q, 0007 Q, 0007 Q, 0007 Q, 0007 Q, 0007 Q, 0007 Q, 0008 Q, 0008 Q, 0008 Q, 0008 Q, 0008	NN D,01950 D,0000 D,0000 D,0007 D	CO Q 0080 Q 0001 Q 0001 Q 0005 Q 0059 Q	PP 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
	CL Q, 0025 Q, 0001 Q, 0001 Q, 0011 Q, 0012 Q, 0011 Q, 0012 Q, 0011 Q, 0011 Q, 0012 Q, 0011 Q, 0012 Q, 0011 Q, 0012 Q, 0011 Q, 0012 Q, 0012	DM 0,0000 0,0000 0,0000 0,0000 0,0000 0,0006 0,0006 0,0006 0,0006 0,0006 0,0006 0,0006 0,0006 0,0006 0,0006 0,0006 0,0006 0,0006 0,0006 0,0006 0,0006 0,0006 0,000000	DN 0,0001 0,0001 0,0000 0,0105 0,0064 0,0063 0,0154 0,0075 0,0042 0,0075 0,0042 0,0075 0,0042 0,0075	EE 0.0075 0.0007 0.0007 0.0074 0.0074 0.0076 0.0075 0.0075 0.0075 0.0075 0.0075 0.0075 0.0075	FF 0.0088 0.0000 0.0000 0.0006 0.0006 0.0007 0.0002 0.0002 0.0002 0.0002 0.0002 0.0008 0.0075 0.0146 0.00745	0-0 0 0002 0 0000 0 0000 0 0009 0 0009 0 0005 0 0062 0 0062 0 0062 0 0062 0 0062 0 0063 0 0064 0 0065 0 005 0 0065 0 0065 0 0065 0 0065 0 0065 0 0065 0 0065 0 0065 00	HH 0.0885 0.0850 0.0000 0.0002 0.0002 0.0005 00005005 0.000500000000	11 D,0009 D,0007 D,0007 D,0000 D,0002 D,	JJ 0,0004 0,0007 0,0008 0,0008 0,0007 0,0007 0,0005 0,0075 0,0075 0,0076 0,0075 0,0076 0,0075 0,0075	KK D,00257 0,0000 D,0017 D,0045 D,0035 D,0051 D,0055 D	L_ 0,0006 0,0000 0,0000 0,0000 0,0000 0,0000 0,0000 0,0000 0,0000 0,0000 0,0000 0,0000 0,0000 0,0000 0,0000 0,0000	MM Q 0000 Q 0000 Q 0000 Q 0004 Q 0007 Q 007 Q	NN D,0169 D,0007 D,	CO 0,0000 0,0001 0,0001 0,0003 0,0045 0,0055 0,	PP 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
	0,000 0,000000	DM 0,0000 0,0000 0,0000 0,0000 0,0000 0,0006 0,	0N 0,000 0,000 0,000 0,000 0,005	EE 0.0075 0.0007 0.0007 0.0074 0.0074 0.0075 0.0075 0.0075 0.0075 0.0075 0.0075 0.0075	FF 0.0088 0.0000 0.0000 0.0008 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0005 0.005 0	0-0 0 0002 0 0000 0 0009 0 0079 0	HH 0.0885 0.0850 0.0050 0.0002 0.0002 0.0002 0.0002 0.0005 0.0005 0.0005 0.0005 0.0005 0.0004 0.0005 0.0044 0.0145	11 D,0009 D,0007 D,0007 D,0002 D,	JU 0,0004 0,0005 0,0005 0,0005 0,0005 0,0005 0,0005 0,0005 0,0005 0,0005 0,0005 0,0005 0,0005 0,0005 0,0005	KK 0,0057 0,0004 0,0000 0,0017 0,00047 0,00047 0,0005	LL 0,0008 0,0001 0,0000 0,0002 0,	MM 0,0000 0,0000 0,0004 0,0004 0,0004 0,0004 0,0004 0,0004 0,0004 0,0004 0,0008 0,0008 0,0008 0,0009 0,0009 0,0009	NN D,0169 D,0007 D,	CO 0,0000 0,0001 0,0001 0,0005 0,	PP 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
	DL 0,0035 0,0001 0,0000 0,0011 0,0012 0,0015 0,0015 0,0015 0,0015 0,0015 0,0025 0,0025 0,0025 0,0025 0,0025 0,0025 0,0025 0,0025 0,0025 0,0025 0,0025 0,0025 0,0025 0,0025 0,0025 0,0001 0,0005 0,0001 0,0001 0,0001 0,0001 0,0001 0,0001 0,0001 0,0005 0,0001 0,0005 0,	Def D,0028 0,0000 0,0022 0,0028 0,0088 0	0.1% 0,0001 0,0001 0,0000 0,0105 0,015 0,005 0,015	EE 0.0075 0.0007 0.0071 0.0076 0.	FF 1,0088 0,0000 0,0000 0,0008 0,0009 0,		HH 0.0883 0.0880 0.0000 0.0002 0.0000 0.0000 0.0000 0.0000 0.0005 0.0005 0.0005 0.0005 0.0005 0.0004 0.0057 0.0004 0.0057 0.0004 0.0057	11 0.0259 0.0001 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	JU 0,0004 0,0007 0,0000 0,0007 0,0005 0,00000000	KK 0.0057 0.0001 0.0001 0.0017 0.0005 0.0017 0.0005 0.	LL 0,0005 0,0007 0,0000 0,0002 0,0002 0,0002 0,0002 0,0002 0,0002 0,0002 0,0002 0,0003 0,0008 0,0009 0,0009 0,0009 0,0009 0,0009 0,0009 0,0009 0,0009 0,0009 0,0009 0,0009 0,0009 0,0000 0,0009 0,0000 0,0009 0,0009 0,0000 0,0009 0,0000 0,	MIM Q.0002 Q.0000 Q.0004 Q.0004 Q.0004 Q.0004 Q.0004 Q.0004 Q.0004 Q.0004 Q.0004 Q.0004 Q.0004 Q.0004 Q.0005 Q.005 Q.05	NN 0.0169 0.0001 0.0007 0.0007 0.0007 0.0007 0.0007 0.0007 0.0007 0.0007 0.0007 0.0005 0.	000 0,0000 0,0001 0,0001 0,0005 0	PP 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000000
20202020202002002002	DL 0,0035 0,0001 0,0000 0,0011 0,0025 0,0075 0,	264 0,0028 0,0000 0,0000 0,0000 0,0008 0,0080 0,0088 0	0.1% 0,0001 0,0000 0,0000 0,0105 0,015 0,015 0,015 0,015 0,015 0,015 0,015 0,015 0,015 0,015 0,015 0,015 0,015 0,005	EE 0.0075 0.0007 0.0007 0.0074 0.0076 0.	FF 1 (0088 0 (0000 0 (0000 0 (0000 0 (0004 0 (0002 0 (0004 0 (0004		HH 0.0885 0.0080 0.0002 0.0000 0.0002 0.0087 0.0087 0.0087 0.0087 0.0087 0.0087 0.0087 0.0087 0.0087 0.0087 0.0087 0.0087 0.0087 0.0087 0.0087	11 0.0009 0.0001 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0005 0.0005 0.0005 0.0005	JJ 0,0004 0,0001 0,0006 0,0007 0,0006 0,0007 0,0006 0,	KK 0.0057 0.0001 0.0001 0.0017 0.0003 0.0017 0.0003 0.0051 0.0051 0.0051 0.0051 0.0051 0.0012 0.0018 0.0018 0.0018	LL 0.0001 0.0001 0.0000 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0005 0.	MIM Q.0002 Q.0000 Q.00004 Q.0004 Q.0004 Q.0004 Q.0004 Q.0004 Q.0004 Q.0009	NN 0.0169 0.0001 0.0007 0.0206 0.0122 0.0122 0.0122 0.0157 0.0256 0.0052 0.0052 0.0052 0.0052 0.0052	CO Q 0000 Q 0001 Q 0001 Q 0003 Q 0005 Q 005 Q	PP 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000000
200430000000000000000000000000000000000	DL 0,0028 0,0001 0,0000 0,0001 0,0000 0,0001 0,0000 0,0001 0,0000 0,	DM D,0020 D,0020 D,0022 D,0022 D,0020 D,0026 D,0006 D,0006 D,0008	014 0,0001 0,0001 0,0003 0,0105 0,0104 0,0104 0,0104 0,0104 0,0104 0,0104 0,0105 0,0105 0,0105 0,0105 0,0005 0	EE 0,0075 0,0007 0,0071 0,0074 0,0076 0,	FF 0,0088 0,0000 0,0248 0,0004 0,0004 0,0004 0,0004 0,00425 0,00425 0,00425 0,00425 0,0175 0,0146 0,00743 0,0175 0,0156 0,0070 0,0090	C-C C 0052 C 0052 C 0050 C 0079 C 0079 C 0079 C 0079 C 0052 C 0052 C 0052 C 0052 C 0055 C 005	HH 0.0853 0.0050 0.0002 0.1682 0.0007 0.0007 0.0005 0.0005 0.0005 0.0005 0.0005 0.0005 0.0005 0.0014 0.0005 0.0014 0.0005 0.0014 0.0005 0.0005	11 0,0001 0,0001 0,0015 0,0020 0,0020 0,0020 0,0020 0,0020 0,0080 0,0090 0,0090 0,0090 0,0090 0,0090	JJ 0,0001 0,0001 0,0005 0,0001 0,0005 0,0001 0,0005 0,	KK 0.0057 0.0000 0.0017 0.0048 0.0077 0.0003 0.0051 0.0055 0.	LL 0,0009 0,0001 0,0000 0,0000 0,0000 0,0000 0,0000 0,0000 0,0009 0,	MM G, 0000 G, 0000 G, 00004 G, 0004 G, 0005 G, 005 G, 005 G, 005 G, 005 G, 005 G,	NN 0,0169 0,0007 0,	CO Q 0080 Q 0073 Q 0073 Q 0073 Q 0089 Q 0089 Q 0089 Q 0089 Q 0089 Q 0089 Q 0089 Q 0080 Q 0080 Q 0084 Q 0086 Q 0094 Q 0084 Q 0086 Q 0094 Q 0086 Q 0094 Q 0086 Q	PP 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000000
2007919200100000000000000000000000000000	DL 0,0028 0,0001 0,0000 0,0001 0,0001 0,0001 0,0001 0,0001 0,0001 0,0001 0,0001 0,0001 0,0001 0,0005 0,0005 0,0005 0,0005 0,0005 0,0005 0,0005 0,0001 0,0001 0,0000 0,0001 0,0000 0,0001 0,0000 0,0001 0,0000 0,0001 0,0000 0,0001 0,0000 0,0001 0,0000 0,0001 0,0000 0,0001 0,0000 0,0001 0,0000 0,0001 0,0000 0,	Def D,0028 0,0000 D,0022 D,0022 D,0026 D,0080 D,0086 D,0086 D,0086 D,0086 D,0086 D,0086 D,0086 D,0086 D,0086 D,0184 D,0826 D,0846 D,0866 D,0866 D,0866 D,0086 D	014 0,0003 0,0001 0,0000 0,0105 0,0105 0,0104 0,0104 0,0104 0,0104 0,0104 0,0104 0,0105 0,0105 0,0105 0,0105 0,0105 0,0105 0,0105 0,0105 0,0105 0,0105 0,0105 0,0105 0,0005 0	EE 0.0075 0.0007 0.0007 0.0074 0.0074 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.00770 0.00770 0.00770 0.00770 0.007700000000	FF 0.00088 0.0000 0.0000 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0008 0.0008 0.00713 0.00713 0.00713 0.00713 0.00713 0.00713 0.00713 0.0009 0.0009 0.0009 0.0009 0.0009 0.0009 0.0008 0.		HeH 0.0883 0.0050 0.0002 0.0002 0.0002 0.0005 0.0005 0.0005 0.0005 0.0005 0.0005 0.0004 0.0005 0.0004 0.0005 0.00141 0.0005 0.00141 0.0005 0.00141 0.0005 0.00141 0.0005 0.0005 0.0005	11 0,0000 0,0000 0,0002 0,000	3.0 0,0004 0,0000 0,0008 0,0008 0,0008 0,0008 0,0008 0,0082 0	KK D,0007 D,0000 D,0017 D,0046 D,0015 D,0015 D,0015 D,0025 D,0025 D,0025 D,0025 D,0025 D,0025 D,0015 D,0015 D,0075 D,0021 D,0021	LL 0,0009 0,0001 0,0000 0,	MiM G, DDDD G, 00000 G, 00004 G, 00002 G,	NN D,0150 D,0007 D,0007 D,0007 D,0007 D,0007 D,0007 D,0005 D,000	C-C C_0000 C_0001 C_0001 C_0005 C_005	PP 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.000000 0.000000 0.00000000
48585858888888888888888888888888888888	DL 0,000	DM 0,0028 0,0000 0,0000 0,0000 0,0008 0,0088 0,	0N 0,000 0,000 0,000 0,0125 0,0054 0,0154 0,0154 0,0154 0,0155 0,0152 0,0152 0,01550000000000	EE 0,0075 0,0007 0,0074 0,0076 0,0077 0,0076 0,0077 0,00000000	FF 0.0088 0.0000 0.0000 0.0004 0.0005 0.0004 0.0005 0.0005 0.0078 0.		HH 0.0883 0.0000 0.0002 0.0000 0.0002 0.0000 0.0000 0.0000 0.0000 0.0000 0.0004 0.0014 0.0014 0.0005 0.0006 0.0006 0.0006 0.0006	11 0,0000 0,0001 0,0001 0,0005 0,0005 0,0005 0,0005 0,0006 0,0086 0,	JJ 0,0004 0,0005 0,0055 0,	KK D,0007 0,0000 D,0017 D,0046 D,0017 D,0005 D,	L. 0,0001 0,0001 0,0000 0,0002 0,0002 0,0002 0,0002 0,0002 0,0002 0,0002 0,0003 0,0003 0,0005 0,	MiM G, DOD G, DOD G, DOD G, DOD G, DOD G, DOT G, DOT G, DOT G, DOT G, DOT G, DOT G, DOT G, DOT G, DOT G, DOD G, DOT G, DOD G, DOD G	NN D,0150 D,0007 D,0007 D,0007 D,0007 D,0007 D,0007 D,0007 D,0007 D,0005 D,005	C+C C, 0000 C, 0000 C, 0001 C, 0004 C, 0005 C, 000	PP 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
A R S B S B B S S B B S S B B S B B S B B S B B S B B B S B B B S B B B S B B B S B B B S B B B S B B B S B B B	DL 0,000	DM 1.0028 0.0000 0.0022 1.0019 0.0028 1.0019 1.0019 1.0009 1.0009 1.0009 1.0009 1.0019 1.	DN 0,000	EE 0.0019 0.0001 0.0011 0.0011 0.0010 0.0010 0.0010 0.000000	FF 0.0008 0.0000 0.0000 0.0008 0.0009 0.0009 0.0009 0.0097 0.	C3G 0 00022 0 00002 0 0000 0 0009 0 0000 0 0009 0 0009 0 0009 0 0009 0 0009 0 0009 0 0009 0 0009	HH 0.0883 0.0000 0.0002 0.1682 0.0007 0.0002 0.0007 0.00057 0.0057 0.0054 0.0057 0.0044 0.0057 0.0044 0.0014 0.0014 0.0014 0.0014 0.0015 0.0014 0.0015 0.0014 0.00150000000000	11 0,0009 0,0000 0,0000 0,0002 0,0002 0,0002 0,0002 0,0002 0,0002 0,0002 0,0002 0,0002 0,0000 0,	J.J 0, 0001 0, 0001 0, 0001 0, 0005 0, 0005	KK D.(2027) D.(2007) D.	LL 0,0009 0,0000 0,	MiM C, 0000 C, 0000 C, 0000 C, 0004 C, 0004	NN D,0150 D,0007 D,	C-O C, 0080 C, 0007 C, 0007 C, 0007 C, 0089 C, 0089	PP 0 0000 0 0000 00
4 8 5 8 5 8 5 8 8 8 5 8 5 5 5 5 5 5 8 E 8 <del>3</del>	DL 0,0028 0,0001 0,0000 0,0078 0,	DM 0,0022 0,0000 0,0000 0,0022 0,0016 0,0006 0,0006 0,0006 0,0008 0,	0N 0,000	EE 0.0075 0.0007 0.0071 0.0076 0.0076 0.0076 0.0076 0.0075 0.0075 0.0075 0.0076 0.0075 0.0076 0.0076 0.0025 0.0006 0.0007 0.0006 0.0007 0.0006 0.0007 0.0006 0.0007 0.0006 0.0007 0.0006 0.0007 0.0006 0.0007 0.0006 0.0007 0.0006 0.0007 0.0006 0.0007 0.0006 0.0007 0.0006 0.0007 0.0006 0.0007 0.0006 0.0007 0.0006 0.0006 0.0006 0.0006 0.0006 0.0006 0.0007 0.0006 0.0007 0.0006 0.	FF 0.0008 0.0000 0.0248 0.0025 0.0025 0.0025 0.0025 0.0025 0.0025 0.0025 0.0025 0.0025 0.0025 0.0025 0.0125 0.0146 0.0051 0.0051 0.0051 0.0055 0.0010 0.0055 0.0010 0.0055 0.0010 0.0055 0.0015 0.0055 0.0015 0.0055 0.0055 0.0015 0.0055 0.		HH 0.0883 0.0000 0.0002 0.0002 0.0002 0.0002 0.0005005 0.0005005 0.0005005 0.000500000000	11 0.0009 0.0001 0.0015 0.0022 0.0022 0.0022 0.0025 0.005 0	JU 0,0004 0,0006 0,0007 0,0006 0,	KK D,0007 D,	L_ 0,000	MiM 0,0000 0,0000 0,0004 0,0004 0,0004 0,0004 0,0004 0,0005 0	NN 0.0159 0.0007 0.0007 0.0007 0.0007 0.0007 0.0007 0.0002 0.0052 0.0052 0.0052 0.0052 0.0052 0.0052 0.0055 0.	CO C, 0000 C, 0000 C, 0001 C, 0000 C, 0003 C, 0005 C, 0005	PP 0.0000
4 @ 5 8 4 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8	DL 0,000	DM 0.0028 0.0000 0.0000 0.0005 0.0006 0.0006 0.0006 0.0006 0.0006 0.0006 0.0006 0.0006 0.0006 0.0006 0.0006 0.0006 0.0006 0.0000	014 0,0001 0,0001 0,0002 0,005 0	EE 0.0078 0.0007 0.0071 0.0071 0.0070 0.0070 0.0070 0.0029 0.00000 0.0000 0.0000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.000000	FF 0.0008 0.0000 0.00248 0.0002 0.00248 0.0002 0.0002 0.0425 0.0175 0.0175 0.0175 0.0175 0.0175 0.0175 0.0010 0.00718 0.00718 0.00718 0.00718 0.00718 0.0070 0.00051 0.00051 0.00051 0.00051 0.00051 0.00051 0.00051 0.00051 0.00051 0.00051 0.00051 0.00051 0.00051 0.00051 0.00051 0.00051 0.00051 0.00051 0.00052 0.000510000000000	C3G 0 00022 0 00002 0 0009 0 0009	HH 0.0883 0.0000 0.0002 0.0002 0.0002 0.0002 0.0005	11 0.0009 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0005 0.	J.J 0,0024 0,0009 0,0009 0,0009 0,0009 0,0009 0,0075 0	KK 0.0257 0.0001 0.0017 0.0000 0.0017 0.0005 0.0000	LL 0,0009 0,0001 0,0000 0,0002 0,0022 0,0022 0,0022 0,0023 0,0023 0,0023 0,0023 0,0023 0,0025 0,0055 0,	MiM Q 0000 Q 0000 Q 0004 Q 0004 Q 0004 Q 0004 Q 0005 Q 005 Q 005	NN D.0189 D.0007 D.	CO 0,0000 0,0001 0,0000 0,0005 0,	PP 0.0000
40000100010001000010000000000000000000	DL 0,0005 0,0001 0,0001 0,0015 0,0016 0,	DM 0,0028 0,0000 0,0000 0,0000 0,000800000000	DN 0,000000	EE 0.0078 0.0007 0.0007 0.0074 0.0074 0.0076 0.0076 0.0077 0.0007 0.	FF 0.0008 0.0000 0.0000 0.0008 0.0008 0.0008 0.0008 0.0008 0.0075 0.0008 0.0175 0.00750000000000		HH 0.0883 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.000000	11 0.0009 0.0000 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0005 0.	JU 0,0001 0,0001 0,0005 0,0001 0,0005 0,0055 0,	KK 0.0057 0.0000 0.0077 0.0003 0.0077 0.0003 0.0051 0.0051 0.0051 0.0051 0.0051 0.0005 0.0012 0.0012 0.0012 0.0012 0.0012 0.0012 0.0012 0.0012 0.0012 0.0012 0.0012 0.0012 0.0015 0.0012 0.0015 0.0012 0.0015 0.	LL 0,0208 0,0000 0,	MIM Q 0000 Q 0000 Q 0000 Q 0004 Q 0007 Q 0008 Q 0009 Q	NN D.0159 D.0007 D.0007 D.0007 D.0007 D.0007 D.0005 D.00157 D.0005 D.0005 D.0005 D.0005 D.0005 D.0005 D.0005 D.0005 D.0005 D.0005 D.0007 D.0005 D.000	CO 0 0000 0 0000 0 0000 0 0000 0 0005 0	PP 0.0000
200501000000000000000000000000000000000	DL 0,000	D4 0.0220 0.0000 0.0222 0.0010 0.0222 0.0010 0.0020 0.0000 0.0000 0.0000 0.00000000	DN 0,0000 0,0000 0,0100 0,0100 0,000000	EE 0.0078 0.0007 0.0074 0.0074 0.0074 0.0076 0.0075 0.0070 0.00000000	FF 0.0008 0.0000 0.0028 0.0002 0.0028 0.0002 0.0028 0.0175 0.0175 0.0175 0.0175 0.0175 0.0175 0.0175 0.0175 0.0175 0.0175 0.0175 0.0071 0.0071 0.0071 0.0071 0.0075 0.0175 0.0075 0.0175 0.00750000000000	40 0 0002 0 0000 0 0000 00	HH 0.0223 0.0250 0.0000 0.0002 0.0002 0.0005 0.0000	11 0.0009 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.00000 0.0000 0	J.J 0, 0001 0, 0006 0, 0007 0, 000	KK 0.0057 0.0000 0.0017 0.0003 0.0017 0.0003 0.0017 0.0003 0.0017 0.0003 0.0017 0.0003 0.0017 0.0003 0.0017 0.0003 0.0005 0.0005 0.0051 0.0015 0.	L 0.0001 0.0001 0.0000 0.0	MiM 0 0000 0 0000 0 0000 0 0004 0 0004 0 0005 0	NN D.0159 0.0007 D.0007 D.0007 D.0007 D.0007 D.0008	CO 0 0000 0 0001 0 0003 0 0003 0 0005 0	PP 0.00000 0.0000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.000000
135 = 138 + 188 28 = 138 48 28 = 135 =	DL 0,0029 0,0001 0,0001 0,0001 0,0001 0,0001 0,0002 0,0001 0,0004 0,	D4 0.000 0.0000	DN 0,000000	EE 0 0078 0 0007 0 0007 0 0007 0 0007 0 0007 0 0007 0 0007 0 0007 0 0009 0 00000 0 0009 0 00000000	FF 0.0008 0.0000 0.0006 0.0007 0.0007 0.0007 0.0007 0.0002 0.0008 0.0175 0.0146 0.0175 0.0146 0.00713 0.0175 0.00146 0.00713 0.0057 0.00146 0.00713 0.0057 0.0057 0.0057 0.0057 0.0056 0	40 0 0002 0 0000 0 0000 00	HH 0.0823 0.0050 0.0022 0.0022 0.0022 0.0005 0.0005 0.0005 0.000400000000	11 0.0009 0.0001 0.0002 0.	JJ 0,0004 0,0005 0,	KK 0.0057 0.0000 0.0017 0.0005 0.0047 0.0005 0.0051 0.0051 0.0051 0.0055 0.0055 0.0055 0.0055 0.0055 0.0015 0.	L. 2,0000 0,	MiM 0 0000 0 0000 0 0000 0 0004 0 0005 0	NN D.0189 0.0007 0.0007 0.0007 0.0007 0.0007 0.0007 0.0007 0.0007 0.0007 0.0007 0.0007 0.0005	CO 0 0000 0 0001 0 0000 0 0003 0 0005 0	PP 0.0000
20050505000000000555555555555555555555	DL 0,000	DH 0.025 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	0.000 0.0000 0.00000 0.00000 0.00000 0.000000	EE 0.0078 0.0007 0.0074 0.0074 0.0074 0.0074 0.0076 0.0077 0.0077 0.0077 0.0077 0.0077 0.0077 0.0077 0.0077 0.0077 0.0077 0.0007 0.	FF 0.0008 0.0000 0.0000 0.0008 0.0008 0.0008 0.0008 0.0075 0.0008 0.0175 0.0075 0.0075 0.0175 0.0075 0.0175 0.0075 0.0175 0.00750000000000	C 0 0000 C 00	HH 0.0825 0.0825 0.0000 0.0002 0.0002 0.0005005 0.0005 0.0	11 0.0009 0.0000 0.0015 0.0020 0.0022 0.0022 0.0022 0.0028 0.	J.J 0,0001 0,0001 0,0001 0,0001 0,0005 0,0001 0,0015 0,0015 0,0015 0,0015 0,0015 0,0015 0,0015 0,0015 0,0015 0,0015 0,0015 0,0005 0,0005 0,0016 0,0005 0,0016 0,0005 0,0016 0,0005 0,0055 0	KK 0.0057 0.0000 0.0077 0.0005 0.0077 0.0005 0.0051 0.0051 0.0051 0.0051 0.0051 0.0051 0.0051 0.0051 0.0051 0.0012 0.0012 0.0012 0.0012 0.0012 0.0012 0.0012 0.0012 0.0015 0.0021 0.0015 0.0025 0.0015 0.00	L 0.0001 0.0001 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0001 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.000000 0.00000000	MiM Q 0000 Q	NN D.0159 D.0007 D.0007 D.0007 D.0007 D.0007 D.0007 D.0008 D.0075 D.0005 D.0075 D.0005 D.0075 D.0005 D.0075 D.0005 D.0075 D.0007 D.0075 D.0007 D.0075 D.0007 D.0075	CO 0.0000 0.0001 0.0001 0.0005 0.0059 0.	PP 0.0000
20050505000000050505050050000000000000	DL 0,000	D4 0.028 0.0000 0.000 0.000 0.000 0.000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.00000 0.00000 0.0000 0.0000 0.000000	2N 0.202000 0.20200 0.20200 0.20200000000	EE 0.0078 0.0007 0.0071 0.0071 0.0071 0.0071 0.0070 0.0072 0.0072 0.0072 0.0072 0.0072 0.0007 0.00007 0.00007 0.0007 0.0007 0.0007 0.0007 0.0007 0.000700000000	FF 0.0028 0.0000 0.0029 0.0029 0.0029 0.0029 0.0029 0.0029 0.0029 0.0029 0.0029 0.0029 0.0029 0.0029 0.0029 0.0029 0.0015 0.0029 0.0015 0.0029 0.0015 0.0029 0.0000000000	40 0 0002 0 0002 0 0002 0 0002 0 0000 0 0000 00	HH 0.0825 0.0000 0.0002 0.0002 0.0005 0.0000	11 0.0009 0.0001 0.0015 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0005 0.	JJ 0,0001 0,0005 0,0007 0,0005 0,0007 0,0005 0,0055 0,	KK 0.0057 0.0001 0.0017 0.0003 0.0017 0.0003 0.0051 0.0051 0.0051 0.0051 0.0055 0.	L 0.0001 0.0001 0.0000 0.0	MiM 0 0000 0 0000 0 0000 0 0004 0 0007 0 0007 0 0007 0 0007 0 0007 0 0007 0 0007 0 0002 0 0079 0 0002 0 0000 0 0002 0 0000 0	NN D.0159 0.0007 0.0007 0.0007 0.0007 0.0007 0.0008 0.0008 0.0008 0.0008 0.0078 0.0007 0.0008 0.0078 0.0007 0.0078 0.0007 0.0078 0.000800000000	CO C 0000 C 0001 C 0001 C 0003 C 0005 C	PP 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.000000
\$188년8년88년88년8년8년8년8년8년8년8년8년8년8년	DL 0,003 0,000	DH 0.0220 0.0000 0.0222 0.0222 0.0210 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	DN 0,000000	EE 0.0078 0.0007 0.0074 0.0074 0.0074 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0076 0.0077 0.0005 0.0077 0.0005 0.0005 0.0007 0.0005 0.0005 0.0007 0.0005	FF 0.0008 0.0000 0.0006 0.0007 0.0007 0.0002 0.0008 0.0175 0.0146 0.0175 0.0146 0.0175 0.0146 0.0073 0.0175 0.0146 0.0073 0.00748 0.00748 0.00748 0.00748 0.00748 0.00748 0.00748 0.00748 0.00748 0.00748 0.00748 0.00748 0.00748 0.0076 0.0069 0.0006 0.0006 0.0006 0.0006 0.0006 0.0006	40 0000 0 000	HH 0.0025 0.0020 0.0022 0.0022 0.0022 0.0022 0.0025 0.0024 0.0024 0.0024 0.0024 0.0024 0.0024 0.0024 0.0024 0.0025 0.0024 0.0025 0.0024 0.0025 0.0024 0.0025 0.0005 0.0000	11 0.0009 0.0001 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0005 0.0005 0.0007 0.0000 0.0007 0.0007 0.0000 0.0007 0.0000 0.0007 0.0000 0.0007 0.0000 0.0007 0.0000 0.0000 0.0007 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000000	J.J 0, 0004 0, 0007 0, 0007	KK 0.0057 0.0000 0.0017 0.0003 0.0017 0.0003 0.0017 0.0005 0.0017 0.0005 0.0051 0.0051 0.0051 0.0051 0.0015 0.0005 0.0015 0.0005 0.	L. (.000) (.	MiM 0 0000 0 0000 0 0000 0 0004 0 0004 0 0004 0 0004 0 0005 0	NN D.0189 0.0007 0.0007 0.0007 0.0007 0.0007 0.0007 0.0007 0.0080 0.0082 0.0082 0.0082 0.0082 0.0085 0.0085 0.0085 0.0085 0.0085 0.0095 0.000500000000	CO 0,0000 0,0001 0,0003 0,0045 0,0055 0,	PP 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.000000
\$ 월일 중 요구 정 같은 말 같이 알 것 만 안 같다. 이 것 이 않은 것 않는 것 같은 것 않는 것 같은 것 같은 것 같은 것 같은 것 않는 것 같은 것 같	DL 0,003 0,000	DM 0.025 0.022 0.022 0.022 0.022 0.022 0.025 0.0	DN 0.0001 0.0001 0.0001 0.0002 0.0004 0.0005 0.0734 0.0734 0.0754 0.0755 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.00000 0.00000 0.000000	EE 0.0078 0.0007 0.0074 0.0074 0.0074 0.0076 0.0076 0.0077 0.0007 0.	FF 0.0008 0.0000 0.0000 0.0008 0.0008 0.0008 0.0008 0.0075 0.0056 0.0057 0.0056 0.0056 0.0056 0.0056 0.0056 0.0056 0.0056 0.0056 0.0056 0.0056 0.0056 0.00050 0.00560 0.00560 0.00560 0.00560 0.00560 0.00560 0.0056	C 0 0000 C 00	HH 0.0855 0.0000 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0005	11 0.0009 0.0000 0.0012 0.0002 0.0002 0.0002 0.0002 0.0002 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0007 0.0000 0.0007 0.0000 0.0007 0.0000 0.0007 0.0000 0.0007 0.0000 0.0007 0.0000 0.0007 0.0000 0.0007 0.0000 0.0007 0.0000 0.0007 0.0000 0.0007 0.0000 0.0007 0.0000 0.0007 0.0000 0.0007 0.0000 0.0007 0.0000 0.0007 0.00000 0.00000 0.00000 0.00000 0.00000 0.000000 0.00000 0.00000 0.00000 0.00000 0.00000000	J.J 0,0001 0,0001 0,0001 0,0001 0,0001 0,0001 0,0015 0,0015 0,0015 0,0015 0,0015 0,0015 0,0015 0,0015 0,0015 0,0015 0,0016 0,0005 0,0006 0,0016 0,0000 0,0000 0	KK 0.0007 0.0007 0.0007 0.0077 0.0005 0.0077 0.0005 0.	L 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	MIM Q 0000 Q	NN D.0159 D.0000 D.0000 D.0000 D.0000 D.0000 D.0000 D.0000 D.0000 D.0000 D.0000 D.0000 D.0005	CO 0,0000 0,0001 0,0001 0,0005 0,	PP 0.0000 0.
	DL 0,003 0,000	DM 0.0226 0.0000	DN 0.0000 0.0001 0.0001 0.0000 0.0003 0.0003 0.0002 0.0002 0.0000 0.0002 0.0000 0.0002 0.0000 0.0002 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	EE 0.0078 0.0007 0.0074 0.0074 0.0074 0.0076 0.0076 0.0076 0.0076 0.0076 0.0007 0.0005 0.	FF 0.0008 0.0000 0.0008 0.0008 0.0008 0.0008 0.0008 0.0014 0.0008 0.0148 0.0148 0.0148 0.0148 0.0148 0.0148 0.0148 0.0010 0.0010 0.0000 0.0008008 0.0008008 0.000800800000800000000	C (C) C	HH 0.0825 0.0825 0.0000 0.0002 0.0005 0.0000	11 0.0000 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0002 0.0005 0.0005 0.0005 0.0005 0.0007 0.0000 0.0007 0.0000 0.0007 0.0000 0.0007 0.0000 0.0007 0.0000 0.0007 0.00000 0.00000 0.00000 0.00000 0.0000000 0.00000 0.00000 0.00000 0.00000000	J.J 0, 0001 0, 0000 0, 0000 0, 0001 0, 0005 0, 0005	KK 0.0057 0.0000 0.0017 0.0003 0.0017 0.0003 0.0021 0.0005 0.	L. 0.0001 0.0001 0.00000 0.00000 0.00000 0.000000	MiM 0,0000 0	NN D.0159 D.0007 D.0007 D.0007 D.0007 D.0007 D.0007 D.0008	CO 0 0000 0 0001 0 0001 0 0004 0 0059 0 0054 0 0056 0	PP 0 0000 0 0000 00



### Annex A.4 – Domestic flow bp product-by-product inverse matrix: CTA (symmetric model)

1000 0.00 100 0.000 01001 0.00 0.11 0.002 1.542 100 0.023 113 1011 D DON 510 D DE3 0.01 100 0.005 0.004 0.001 1.32 0,038 0.0014 0.064 0.005 0.0010 0.000 D DOL D.0090 0.00 0.00 1,001 0.000 100 0.000 0.00 1.00 5.000 0.00 0,002 100 100 1.37 0.000 0,0143 0,013 0.03 0,04 0.00 D,0 1,011 1,0 D,D1 dan 0.001 D DDC 1015 0.00 0.06 5.0014 5.00 0.01 0,01 0,025 1,1700 0.017 DDB 0.000 0,017 0,02 D D04 0.0005 D.D0. 0,163 αa āā 0.002 0.000 1,049 0.004 0.00 0.00 0.001 100 1.01 100 100 100 0.00 10 0,01 0,01 11 a,ac 0,008 0,06 D,D0 D,D D,D43 0.002 0.007 0.07 0.000 1.50 0.001 1 DT 5.57 dos 0.022 0.01 0.0016 0,004; 0.001 0.0014 0.001 0.06 0.00 0,000 0.00 0.00 0.004 1,00 0.00 0.000 0.000 0.00 0.00 0.00 0.00 1.00 0.00 0.004 1011 1010 100 100 100 0.00 100 10 1.01 0,108 0.00 0.0 0.54 0,03 0,013 0.022 0,04 0,10 5.531 5.63 0,113 0.050 0.00 1.94 1036 0,025 0.0508 0.03 0.0645 0.0054 0,07 1001 1.00 0.011 0.00 0.01 0.011 0.040 0.0408 0.04 0.009 0.0140 0,121 1943 0.03 0.04 0.0 108 0.01 0.05 0.050 a ax 0.054 0,113 1074 1.02 0.147 0.083 0.000 1000 1000 0.000 5 000 0.000 0.000 5 0000 0.000 0.00 1000 0.000 0.000 0.001 0.001 0.0011 1 001 0.001 0.002\* 0.000 0.000 0.000 0.00 0.0023 a acc 1,00 0,00 0,001 1,001 1,0013 0.00 0005 0,00 0.00 1,000 1000 0,003 100 0.00 5.00 0.00 0,00 1.900 10 0.00 1.50 1.515 1,7157 1.850 1,753 1.738 2,032 1,458 1.671 1.587 1.73 072

	α.	DM .	DN	EE.	FF	0G	HH	1	Ц	KK -	Ц. —	MN	NN	00	PP
AA -	0,0027	0,0005	0,0287	0,0001	0,0091	0,0046	0.0577	0,0001	0,0018	D(0008	0,0025	0,0018	0,0167	10034	0,0000
88	0.0004	0,0000	0,00011	0.0000	0,000	0,0001	1,0052	0.0001	0.0001	0.0001	0.0001	0.0000	0.0001	0.0001	0,0000
CACS	0,0013	0,0015	0,0054	0,0065	0,0116	D,0006	0.0029	D(0064	D(0007	D(0014	0,0026	0,0011	0,0046	1,0009	0,0000
DA	0,0007	0,0016	0,0050	0,0010	0,0021	0,0060	0,1748	0,0044	00045	0,000	0,0054	0,0035	0,0258	10007	0,0000
DB	0,0080	0,0088	0,0638	0,0006	0,0028	0,0016	1,0088	0,0016	0.0004	0.0008	0.0121	0,0006	0.0102	10002	0,0000
DC D	0,0010	0,0005	0,0150	0,0000	0,0001	-0,0001	0,0001	D(0001	0,0001	D(0002	0,0001	0,0000	0,0000	0,0004	0,0000
00	0,0042	0,0085	0,1500	-0,0012	0,0454	0,0042	0,0003	0,0021	0,0011	D(0001	0,0008	0,0010	0,0010	0,0001	0,0000
DE	0,0145	0,0075	0,0290	0,0071	0,0081	0,8294	0136	0,0195	0,0154	0,0246	1,0073	0,0129	0,0083	10276	0,0000
DF	0,0032	0,0004	0,0074	0,02944	0,0159	D,0082	1,0073	0,0277	0,0047	D,0009	1,0006	0,0027	0,0200	1,0105	0,0000
03	0,0158	0,0100	0,0253	0,0037	0,0151	0,0065	0,0006	0,0005	0,0011	0,0000	0,0018	0,0015	0,0401	6,0107	0,0000
DH	-0.0643	0,0215	0,0334	0,0014	0,0094	0,0087	1.0544	0.000	0.0040	0.0047	0.0012	0,0008	1,0129	1008	0,0000
	0,0068	0,0183	0,0157	-0,0041	D,1491	0,0072	0,0144	0,0042	0,0049	D (0000	0,0018	0,0015	0,00223	1,0056	0,0000
D.I	0,0858	0,0066	0,0122	0,0006	0,0759	0,0191	1,0108	0,0072	0,0021	0,0085	1,0125	0,0018	0,0048	10086	0,0000
DK –	0.0071	0,0164	0.0039	0.0017	0,0140	0,0004	0.0031	0.3011	0.3004	0.0014	0.0015	0.0004	0.0015	10012	0.0000
П.	1,2065	0,0462	0,0021	0,0121	0,0125	0,0111	0,0000	0,024	0,0009	0,0045	0,0000	0,00220	0,0000	0,0109	0,0000
054	0,0018	1,1804	0,0003	0,0003	0,0005	0,0081	1,0006	0,0000	0,0002	0,0004	0,0058	0,0002	0,0008	0,0009	0,0000
ON -	0.0020	0.0258	1,0908	0.0001	0,0062	0,0021	1,0070	0,00%	0,0048	0,000	1,0045	0.0022	0,0015	1,0092	0,0000
EE.	0,0190	0,0480	0,0284	1,6235	0,1376	0,03/11	1,0422	0,0264	0,0140	0,0141	0,0036	0,0240	0,0102	10748	0,0808
FF	0,0165	0,0121	0,0196	0,0051	1,2/10	0,031	0,0140	0,0308	0,0154	0,0577	0,0006	0,0087	0,0050	10446	0,0000
0G -	0.0449	0.0295	0.0408	0.0296	0.0582	1,1565	1,0545	0,1035	0,0191	0,0000	1,0090	0.0460	1.0424	10604	0,0000
HH	0,0134	0,0072	0,0120	0,0052	0,0061	0,0242	1,0090	0,0231	0,0121	0,0126	0,0453	0,0049	0,0107	1,0193	0,0000
	0,0343	0,530	0,0381	0,0354	0,005	0,1129	1,0081	1,2504	0,0335	0,0555	0,0417	0,0241	0,0008	0,1359	0,0000
11	-0.0872	0,0279	0,0436	0,0495	0,0467	0,0683	1,0093	0,0584	1,1036	0,0979	1,0061	0.0128	0,0248	10091	0,0000
KKC -	0,0949	0,0610	0,0650	0,1080	0,0723	0,2379	0,1042	0,1506	0,2575	1,2435	0,0112	0,065/1	0,0900	0,2337	0,0000
LL	0,0000	0,0000	0,0000	0,0000	0,0000	0,000	1,0000	0,000	10100	10100	1,0000	0,0000	0,0000	1010.0	0,0000
00	0.0045	0,0002	0.0021	0.0018	0,0005	0,0021	10012	0,0019	0,0021	0,0010	1,0125	1,0066	1,0008	- E0013	0,0000
NN	0,0009	0,0005	0,0004	0,0003	0,0007	D,0007	0,0011	D (0005	D(0001	0,0004	0,0011	0,0004	1,0838	1,0004	0,0000
00	0,0007	0,0034	0,0112	0,0058	0,0005	0,0001	0,0074	01122	0,000	10000	0,0051	0,0009	0,0055	1,1330	0,0000
PP -	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	1,0000	0,000	0,0000	0,0000	0,0000	0.0000	0,0000	00003	1,0808
_	1,7035	1,6282	1,0083	1,9450	1,3914	1,7062	1,6363	1,008	1,5022	1,6251	1,2715	1,2000	1,4751	1,1729	1,0000



Annex A.5 – Domestic flow bp industry-by-industry inverse matrix: ITA (symmetric model)

	8A.	89	CA	C9	DA	09	DC	00	00	DF .	DG	DH	DI	DJ	DK .
λλ.	1,1051	1,0007	E-0000	1,0003	0.2713	0.0345	0.0004	0.2370	0,0530	0,0009	0.0074	0.0075	0.0056	0.0048	0.0038
38	0.0002	1,0158	0,0000	1,0001	0.0017	0.0001	0.0801	0.0001	0.0001	0.0000	0.0084	0.0001	0.0001	0.0001	0.000/
CA.	0,0000	0,0000	1,0000	0,0000	0.0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0.0000	0,0000
38	0.002/0	1,0006	1,0000	1.0821	2,0004	0,0008	0,0807	0,00%	0,0018	0,0004	0,0070	0,0017	0,1058	0.0038	0.0025
ΟA.	0.1088	1,0068	1,0000	1.0541	1.1534	0.0054	0.0248	0.0247	0.0118	0.0004	0,0088	0.0037	0.0039	0.0054	0.0025
- 00	0,0050	0,0056	0,0000	0,0046	0,0023	1,3698	0,0008	0,0004	0,0027	0,0005	0,0064	0,0117	0,0036	0,0040	0,0022
00	0,0000	1,0002	1,0000	1,0002	0,0002	0,0017	1,3098	0,0002	0,0000	0,0000	0,0002	0,0015	0,0000	0,0004	0,0000
30	0.0049	0.0017	E-0000	1,0032	0,0063	0.0036	0.0029	1,3489	0,0195	0.3064	0.0001	0.0081	0.0160	1.0108	0.0049
. 3C	0,0101	1,0144	0,0000	1,0143	0.0362	0.0117	0.0223	0.0199	1,2619	0.0013	0,1245	0.0114	0,0269	0.0161	0,0105
OF .	0,0106	1,00.66	0,0000	1,0608	0,0067	0,0057	0,0844	0,0076	0,0060	1,0250	0,02985	0,0100	0,0154	0,0003	0,0040
00	0,0%68	1,0033	E0000	1,0192	0,0109	0,0064	0.022%	- 64212	0,1270	0,0302	1,1433	0,1301	0.0215	0,0168	0.0097
DH .	0,0031	1,0020	1,0000	1,0022	0.012/	0,0063	0,0258	0.0077	0,0083	0,0006	0,0116	1,0432	0,0081	0.0132	0,0191
	0,0437	0,0002	0,0000	- 1,007M	0,0184	0,0000	0,0051	0,0086	0,0070	0,00%	0,0089	0,0074	1,1180	0,0150	0,0164
24	0.0082	1,0061	1,0000	1,0101	0.0186	0,0084	0,0174	0.0172	0,0100	0,0018	0,0176	0,5456	0.0320	1,2980	0,1280
K.	0.0023	1.0028	1,0000	1.0043	0,000	0.0821	0.0015	0,0003	0.0036	0.3064	0,0038	0.0163	0.0168	0.0125	1,1040
а.	0,0021	1,0002	0,0000	1,0048	0,0022	0,0020	0,0016	0,0023	0,0027	0,0003	0,0034	0,0052	0,0049	0,0057	0,0258
010	0,0009	1,0002	1,0000	-1,0045	2,0006	0,0010	0,0807	0,0009	0,0009	0,0001	0,00%	0,0079	0,0016	0,0040	0,0080
34	0.0008	10010	1,0000	1,0011	10001	0,0145	0.0828	23080	0,0060	0,0002	0,0022	0.0085	0.0026	0.0161	0.003
EE.	0,0021	1,0212	1,0000	0,1003	0.0293	0,0381	0,0216	0.0311	0,0386	0,0029	0,0412	0,0345	0,1080	0,0396	0,0227
1	0,00238	1,0143	0,0000	1,0259	0,02%	0,0451	0,0172	0,020	0,8229	0,0095	0,1227	0,0150	0,0052	1,0436	0,0022
96	0.0710	0.1629	1,0000	0,1156	- 63536	0.0436	0.002%	0.060	0,0587	0,0100	0,1730	0,0539	0.0867	1,0096	0.0449
44	0.0071	1,0122	8,0000	1,0158	0.0089	0,0116	0.0108	0.0108	0.0112	0.3007	0,0128	0,0096	0.0144	0.0144	0.0123
-	0,0250	1,0639	0,0000	0,1008	0,0357	0,0308	0,0274	0,0449	0,0523	0,0008	0,0475	0,0395	0,0733	0,0414	0,0058
IJ.	0.0435	1,0590	E 0000	1,0636	0.0461	1.0507	0.0429	0.0643	0.0502	0.0054	0,0541	0.0419	0.0545	1,0358	0.0535
QC -	0,0556	1,06/1	1,0000	1,0964	0,0505	0,0827	0,0540	0,0577	0,0085	0,0064	0,1200	0,0712	0,0790	0,0598	0,0622
J.	0.0045	1.0545	E-0000	1,0078	0,0087	0.0548	0.0648	0,0046	0.0087	0,0005	0,0084	0.0051	0.0071	0.0048	0.0045
AM .	0,0009	1,0026	0,0000	1,0021	0.0019	0,0020	0.0016	0.00%	0,0025	0.0001	0,0027	0,0034	0,0025	0.0028	0,0025
99	0,0042	0,0004	E.0000	0,0016	0,0001	0,0014	0,0014	0,0005	0,0012	D-0000	0,0000	0,0009	0,0013	0,0004	0,0015
20	0.0031	1,0052	E GLOOD	1,0053	2006	0,0036	0,0838	E 3005	0,0057	0,0003	0,0086	0,0034	0.0043	0.0832	0.0022
Ŧ	0.0000	1,0000	E-0000	1,0000	0.0000	0,0000	0,0000	0.0000	0,0000	0.0000	0,0000	0,0000	0.0000	0.0808	0.0000
80 M	1,6529	1,5158	1,0000	1,7427	1,854	1,7508	1,7347	2,0472	1,7636	1,1046	1,6710	1,0000	1,8525	1,7246	1,6190

	D	DM .	DN .	EE .	FF	99	HH I		μ,	NK.		MM	NN	00	PP
AA	0.0035	0.0005	0.0290	0.0016	0.0090	0.0078	0.0726	0.0043	0.0027	0,0047	10040	0.0022	0,0140	0.0065	0.0000
88	0,000/1	0,000/1	0,0001	0,0001	0,0001	0,00022	0,0061	0,0002	0,0001	0,0001	0,0001	0,0000	0,0002	0,0002	0,0000
CA .	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0,0000	0.0000	0.0000	0,0000	0,0000	0.0000	0,0000	0.000	0.0000
63	0,0012	0,0024	0,0111	0,0012	0,0264	0,0016	0,0023	0,0014	0,0007	0,0016	0.0000	0,0005	0,0006	0.0014	0,0000
DA -	0.0034	0.0021	0.0082	0.0017	0.0029	0.0074	0.1623	0.0057	0.0034	0.0042	10062	0.0035	0.039	10053	0.0000
- 10	0,0086	0,0050	0,0110	0,0012	0,0036	0,0035	0,0089	0,0025	0,0009	0,0016	0,0004	0,0008	0,0106	0,0064	0,0000
00	0.0013	0.0007	0.0141	0.0001	0.0003	0.0004	0.0002	0.0003	0.0001	0.0003	E-0002	0.0001	0,0001	1,0006	0.0000
00	0,0049	0,0071	0,1464	0,0017	0,0427	0,0056	0,0036	0,0033	0,0016	0,0036	0.0022	0,0012	0,0013	0.0096	0,0000
3C	0.0154	0.0082	0.0199	0.0073	0.0087	0.0231	0.0133	0.0191	0.0458	0.1240	10102	0.0139	0.0082	10056	0.0000
5	0,0041	0,0052	0,0085	0,0220	0,0163	0,0088	0,0078	0.0258	0,0027	0,0049	0,0086	0,0030	0,1212	0,0110	0,0000
00	0.0872	0.0400	0.0322	0.0003	0.0134	0,0074	0,0065	0.0040	0.0017	0,0005	100.0	0.0015	0,150	10057	0,0000
DH	0.0672	0.0225	0.0296	0.0019	0.0058	0.0090	0,0042	0.0048	0.0015	0,0048	0.0019	0.0009	0,0027	0.0041	0.0000
0	0.0073	0.0162	0.0155	0.0049	0,1436	0.0085	0,0147	0.0071	0.0030	0,0078	1,0000	0.0020	0,0009	E-0068	0,0000
31	0.0865	0.0050	0.0685	0.0072	0.0729	0.0254	0.0113	0.0083	0.0034	0.0085	0.0063	0.0023	0,0065	0.0009	0.0000
OK .	0,0050	0.0173	0,0054	0,0004	0,0145	0,0040	0,0003	0,0015	0,0006	0,0017	0.0048	0,0005	0,0016	0.0016	0,0000
а.	1,1845	0.0416	0.0033	0.0111	0.0127	0.0427	0.0060	0.0220	0.0042	0.0061	8,003/	0.0030	0.0077	80102	0.0000
DH.	0.0034	1,1579	0,0037	0,0007	0,0014	0,0079	0,0011	0,0035	0,0007	0,0011	0,0051	0,0004	0,0009	0,0047	0,0000
05	0.0029	0.0245	1,0830	0.0007	0.0057	0.0035	0.0069	0.0019	0.0019	0.0019	10041	0.0021	0.007	1006	0.0000
11	0.0189	0.0180	0.0287	1,5585	0.0054	0,0004	0,0404	0.0262	0,0150	D,0161	0.0350	0.0232	0,0177	0.0711	0,0000
FF	0.0160	0.0540	0.0257	0.0290	1.3518	0.0313	0.0158	0.0643	0.0293	0.0573	2,9158	0.0099	0,0102	10452	0.0000
GG	0.0655	0.0072	0.0517	0.0534	0.0839	1,1530	0.0672	0,1489	0.0069	0.073	0.0466	0.0216	0,0485	0.0727	0.0000
44	0.0439	0.0079	0.0129	0.0057	0.0071	0.0241	1,0099	0.0231	0.0432	0,0109	0.0151	0.0053	0,0189	0.0198	0.0000
_	0.0069	0.0263	0,0410	0,0582	0.0050	0,1083	0,0291	1,2786	0,0438	0,0440	0.0435	0.0253	0,0221	0.050	0,0000
Ш	0.0409	0.0010	0.0464	0.0585	0.0500	0.0747	0.0430	0.0635	1,1001	0,1029	0.0214	0.0152	0.1276	0.0659	0.0000
кК. –	0.0854	0.0552	0.0542	0.0854	0.0663	0,1900	0.0879	0.1244	0.2075	1,1969	1083	0.0544	0.0606	0.1891	0.0000
11	0.0055	0.0038	0.0045	0.0432	0.0051	0.0125	0.0063	0.0089	0.0130	0.0131	1.0050	0.0040	0.0065	0.0154	0.0000
UN.	0.0047	0.0054	0.0034	0.0030	0.0010	0.0038	0.0016	0.0034	0.0027	0.0022	1003	1,0067	0.0010	0.0018	0.0000
101	0.0011	0.0008	0.0006	0.0005	0.0009	0.0012	0.0013	0.0010	0.0006	0.0008	0.0013	0.0005	1,0833	0,0009	0.0000
00	0.0036	0.0032	0.0113	0.0000	0.0034	0.0709	0.0082	0.0131	0.0063	0.0211	10084	0.0096	0.0085	1.00	0.0000
pipi -	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0,0000	0.0000	0.0000	0,0000	1,0000
50.00	1,7025	1.6317	1,0100	1,0035	2,0050	1,7764	1,6542	1,0503	13134	1.002	1,3448	1,2114	1,4636	1.0010	1,0000



### Annex A.6 – Domestic flow bp industry-by-industry inverse matrix: CTA (symmetric model)

	44	88	CAC8	CA .	08	0C	00	DE	DF	00	DH	0	DJ .	DK .
AA -	1,1412	1,0022	0,062%	0.2878	0,0257	1,0004	0,2511	0.0665	0.0013	0,0068	0.0072	0,0052	0,0043	0.0024
88	0.0002	13164	0.0801	0.0017	0.0001	10001	0,0001	0.0801	0.0000	0.0803	10001	0.0001	0.0001	0.0001
CADD	0,0034	1,0055	1,0216	0,0029	0,0820	0,0014	0,0025	0,0823	0.2084	0,0019	1,0005	0,0357	0,0001	0,0021
CA.	0,1071	1,0045	0.0820	1,1488	0,0634	10257	0.0103	0.0680	0.0084	0.0064	0.0018	0.0820	0.0026	0.0021
08	0,0044	1,0047	0,0837	0,0015	1,3847	0,0369	0,0022	0,0806	0.0007	0,0436	1,0082	0,0822	0,0018	0,0009
DC .	0,0001	-0,0001	-0,0001	0,0000	0,0013	1,3483	0,0000	0,0005	0,0000	0,0000	0,0012	0,0000	0,0001	0,0000
00	0.0048	1309	0.0824	0.0063	0.0828	1,0025	1,3787	0.0307	0.0007	0.0826	1309	0.0156	0.0104	0.0044
0E -	0,0103	0,0147	0,0143	0,0373	0,0114	0,0227	0,0301	1,2751	0,0009	0,0254	0,0102	0,0367	0,0154	0,0102
0F	0,0108	1,0283	0,0643	0,0086	0,0050	1,0087	0,0076	0,0053	1,0386	0,0251	1,0068	0,0113	0,0069	0,0044
00	0,0180	-1,0000	0,0138	0,0113	0.0091	10260	0,0343	0.0011	0.0373	1,1896	0,1580	0.0222	0.0180	0,0097
DH	0,0029	0,0016	0,0015	0,0142	0,0063	0,0286	0,0068	0,0065	0,0004	0,0109	1,0480	0,0051	0,0122	0,0212
01	0,0135	1,0000	0,0052	0,0184	0,0824	1,0027	0,0083	0,0065	-4,0036	0,0000	1,0087	1,1201	0,0197	0,0182
C)	0,0080	1,0054	0,0090	0,0191	0,0070	0,0177	0,0463	0,0094	0,0002	0,0173	1,0470	0,00223	1,3021	0,1340
DK -	0,0019	0,0021	0,0056	0,0003	0,0017	0,0007	0,0029	0,0820	0,0010	0,0053	0,0163	0,0169	0,0011	1,1134
01.	0.0007	1308	0.082%	0.0010	0.0011	1308	0,0012	0.0615	0.0009	0.0016	1,0039	0.0432	0.0035	0.0298
DM -	0,0002	0,0004	0,0001	-0,0006	0,0001	-0,0015	-0,0000	-0,00022	0,0001	0,0000	1,0046	-0,0003	0,0005	0,0005
DN -	0,0003	1,0004	0,0005	0,0006	0,0116	1,0021	-0,0018	0,0064	0,0002	0,0017	0,0084	0,0016	0,0141	0,0016
EE	0.0352	13222	0,1123	0.0318	0.0420	13235	0,0042	0.0421	0.0247	0.0450	10381	0,1138	0.0429	0.0242
FF .	0,0002	0,0110	0,0216	0,0184	0,0122	0,0157	D,0215	0,0198	0,0122	0,0190	0,0104	0,0362	0,0419	0,0297
38	0,0762	1,1845	0,1208	0,0446	0,0054	1,0220	0,0497	0,0626	0.0294	0,0964	1,0369	0,0760	0.0305	0,0382
нн	0,0066	0,0120	0,0452	0,0083	0,0115	0,0105	0,0/104	0,0109	0.0005	0.0124	1,0094	0,0131	0,0145	0,0127
	0,0048	1,0677	0,1237	0,0348	0,0304	0,0259	0,0450	0,0829	0,0276	0,0467	0,0393	0,0658	0,0415	0,0581
IJ	0,0450	1,0602	0,0654	0.0476	0,0540	1,0484	0,0454	0.0524	0.0179	0.0556	1,040	0.0526	0,0402	0.0569
XX.	0.0613	0,0594	0,0610	0.0597	0,0668	1,0570	0,0638	0.0954	0.0294	0,1367	0,0796	0,0726	0.0622	0.0541
LL.	0.0000	13000	0.0800	0.0000	0.0000	13000	0,0000	0.0800	0.0000	0.0800	13000	0.0000	0.0000	0.0000
MM.	0,0006	1,0004	0,0017	0,0015	0,0018	0,0014	D,0014	0,0821	0.0004	0,0824	0.0022	0,0821	0,0026	0.0021
NN.	0,0041	1,0021	0,0013	0,0019	0,0013	1,0013	0,0025	0,0809	0,0003	0,0005	1,0007	0,0010	0,0001	0,0017
00	0.0023	1,0040	0.0636	0.0007	0.0828	1,0025	0.002%	0.0648	0.0009	0.0857	1,0027	0.0830	0.0023	0.0021
pp -	0,0000	0,0000	0,0000	0,0000	0,0000	1,0000	0,0000	0,0800	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000
SUM	1,6853	1.5731	1,7168	1,9439	1,7531	1,7364	2,0220	1,7665	1,4784	1,6726	1,8052	1,72%	1,7256	1,6183

	α,	OM	ON .	66	FF .	99	нн	1	11	KK -	LL	MM	NN	00	PP
AA -	0,0050	0,0025	0,0021	0,0012	0,0097	0,0070	0,0735	0,000	0.031	0,0041	0,0057	0,0000	0,0181	10101	0,0000
88	0,0001	0,0000	0,0001	0,0000	0,0000	0,0001	0,0052	0,0001	0:0001	0,0001	0,0001	0,0000	0,0001	0,0001	0,0000
CACS	0,0014	0,0016	0,0058	0,00009	0,0123	0,0027	D(0001	D (0066	0,0005	0,0016	0,0051	0,0012	0,0048	0,0040	0,0000
DA	0,0122	0,0013	0,0050	0,0000	0,0011	0,0046	D,1694	0105	0.031	0,0005	0,0055	0,005/	0,0258	10004	0,0000
08	0.0877	0.0079	0,0896	0,0006	0.0824	0.0021	0.3084	03054	0.0003	0,0007	0,0018	0,0005	0,0101	1:003	0,0000
DC	0,0007	0,0005	0,0141	0,0000	0,0000	0,0001	D(0001	D (0000	0,0001	0,0002	0,0001	0,0000	0,0000	0,0004	0,0000
00	0,0040	0,0058	0,1502	0,0008	0,0463	0,0049	0,0008	0.004	0.0015	0,0002	0,0019	0,0010	0,0010	1,000	0,0000
DE	0.0143	0.0078	0.0198	0.0075	1,0083	0.0236	0,0108	0.0196	0.0163	0,1248	0.0105	0.0432	0,0085	63277	0,0000
DF	0,0038	0,0027	0,0079	0,0258	0,0162	0,0087	0,0079	0,0291	0,0000	0,0044	0,0091	0,0030	0,0216	_ BHH	0,0000
03	0,0188	0,0103	0,0247	0,0025	0,0138	0,0095	0,0045	0,0005	0,0040	0,0024	0,0015	0,0012	0,0385	1,0005	0,0000
DH	1,0636	- 0.0229	0,0036	0,0017	0,0090	0,0064	0,0044	0,0048	0,0009	0,0047	0,0017	0,0007	0,0022	6,0037	0,0000
	0,0068	0,0168	0,0153	0,0006	0,1506	0,0074	D)0146	D,0058	0,0004	0,0074	0,0058	0,0017	0,0023	0,0058	0,0000
D.I	0,0840	0,1005	0,0738	0,0056	0,0790	0,0297	0,0115	0,0087	0,0038	0,0084	0,0050	0,0021	0,0061	0,0004	0,0000
OK	1,0852	0,0145	0,0025	0,0021	1,0128	0,0029	0.3030	0,0040	0,3004	0,002	0,0016	0,0004	0,0014	0.001	- 0,0000
п.	1,2256	0,061	0,0017	0,0118	0,0125	0,0108	D)0062	0,0216	0,0004	0,0006	0,0030	0,0017	0,0075	0,0096	0,0000
CN	-5002	1,1787	0,0004	0,0001	-1,0004	0,0064	0,0002	0,0011	-0,0001	0,0000	0,0048	0,0001	0,0003	0,0001	0,0000
DN -	0,0013	1,039	1,0864	0,0000	1,0053	0,0019	0,0072	0,0043	0,0046	0,0015	0,0040	0,0022	0,0015	0,0094	0,0000
EE .	1,0201	0,0190	0,0006	1,6254	0,0290	0,0315	0,0442	0,0275	0,0149	0,0152	0,0082	0,0253	0,0183	10140	0,0000
FF	0,0156	0,0117	0,0180	0,0001	1,3808	0,0270	0,0125	0,0305	0,0130	0,0571	0,0152	0,0083	0,0083	10402	0,0000
0G -	1,065	0,0254	0,0097	0,00068	1,0851	1,1586	0,25(2)	0,1009	0,0225	0,0099	1,082	0,0180	0,0446	0,0020	0,0000
1414	1,0157	0,0076	0,0123	0,0056	1,0063	0,02236	1,0094	0,0230	0,0124	0,0131	0,0150	0,0051	0,0187	0,0192	0,0000
	1,0958	0,0229	0,0404	0,0075	1,0282	0,1185	0,0385	1,2911	0,0406	0,0411	0,041	0,0255	0,8217	0,1381	0,0000
Ш	0,0416	0,0018	0,0456	0,0550	0,0820	0,0790	0,0445	0,0544	1,9139	0,1073	0,0207	0,0150	0,8278	D(0661	0,0000
RK -	0.0870	0,0553	0,0573	0,0054	0,0817	0,2150	0,0076	0,0293	0,2464	1,2293	0,0064	0,0650	0,0004	0,2107	0,0000
UL -	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,000	0,000	0,000	0,0000	1,0808	0.0000	0,0000	0,000	0,0000
DIM .	0,0048	0,0032	0,0022	0,0018	0,0008	0,0021	0,0013	0,0019	0,0020	0,0016	0,0024	1,0066	0,0008	0,0043	0,0000
101	0,0008	0,0008	0,0006	0,0000	0,0007	0,0087	0,0011	0,0006	0,0001	0,0004	0,0011	0,0004	1,0899	0,0004	0,0000
00	0,0228	0,0025	0,0110	-4,0824	0,0824	0,0099	0,0077	0.0126	0,0054	0,82%	0,0081	0,0099	0,0061	1,1333	0,0000
PP.	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,000	0,0000	0,0000	0,0000	0,0000	0,0000	0,0000	0,000	1,0000
SUIT	1,7828	1,6296	1,8837	1,9437	1,9871	1,7749	1,6180	1.817	12136	1,8279	1,3475	1,2134	1,4785	13/05	1,0000

Mathematical Appendix

This appendix makes the mathematical proof of the full equivalence of the two methods considered in this paper, besides the practical example that was provided above. ITA is the reference technological assumption in this appendix, although an equivalent proof can be made for CTA.

Let us start with the product-by-product case. Our aim is to show that the multipliers inserted in the inverse matrix of the symmetric, domestic-flow, *bp* table (like the ones of Annex A.3), are the same that may be inferred of the upper left-hand part of the M&U's inverse (as in Annex A.1).

The multipliers of this upper left-hand block correspond to equation (7). The first step is to re-write (7) for domestic flows at *bp*. Defining  $\hat{\mathbf{t}} = (\mathbf{I} - \hat{\mathbf{c}}) (\mathbf{I} - \hat{\mathbf{f}} - \hat{\mathbf{n}})$  as the diagonal matrix that proceeds (through pre-multiplication) to the transformation of a column-vector (or of each column of one matrix) of total-flows at *pp* into its equivalent with domestic-flows at *bp*, then:

$$(\mathbf{p}^{N})^{bp} = \hat{\mathbf{t}} \mathbf{p}^{pp}$$
 and  $(\mathbf{y}^{N})^{bp} = \hat{\mathbf{t}} \mathbf{y}^{pp}$  (A.1)

(in this appendix the superscript N means domestic flows and bp/pp basic or purchasers prices)

On the other hand: 
$$\left(\mathbf{Q}^{N}\right)^{bp} = \hat{\mathbf{t}} \mathbf{Q}$$
 (A.2)

(because  $\mathbf{Q} = \mathbf{U}^{pp} (\hat{\mathbf{g}}^{bp})^{-1}$  and  $(\mathbf{Q}^N)^{bp} = (\mathbf{U}^N)^{bp} (\hat{\mathbf{g}}^{bp})^{-1}$  by the «technical» coefficient definition. So  $(\mathbf{U}^N)^{bp} = \hat{\mathbf{t}} \mathbf{U}^{pp} \Rightarrow (\mathbf{Q}^N)^{bp} = \hat{\mathbf{t}} \mathbf{Q})$ .

As for the matrix **S** (in (7) as well), this one was already calculated with domestic production only, and it was evaluated at *bp*. However, the denominator in these coefficients were the cells of  $\mathbf{p}^{pp}$ : the total product supplies, with imports included, at *pp*. This means:  $\mathbf{S} = \mathbf{V}^{bp} (\hat{\mathbf{p}}^{pp})^{-1}$ .

Being  $\mathbf{S}^{N} = \mathbf{V}^{\text{bp}} \left[ (\hat{\mathbf{p}}^{N})^{\text{bp}} \right]^{-1}$  instead, then:

$$S^{N} = V^{bp} (\hat{t} \, \hat{p}^{pp})^{-1} = V^{bp} (\hat{p}^{pp})^{-1} \hat{t}^{-1} = S \, \hat{t}^{-1}$$
(A.3)

Making use of these results, and returning to (7), we may then conclude that:

$$\begin{split} \mathbf{p}^{pp} &= \left(\mathbf{I} - \mathbf{QS}\right)^{-1} \mathbf{y}^{pp} \\ \hat{\mathbf{t}} \, \mathbf{p}^{pp} &= \hat{\mathbf{t}} \left(\mathbf{I} - \mathbf{QS}\right)^{-1} \hat{\mathbf{t}}^{-1} \mathbf{t} \, \mathbf{y}^{pp} \\ \left(\mathbf{p}^{N}\right)^{bp} &= \left[\hat{\mathbf{t}} \left(\mathbf{I} - \mathbf{QS}\right) \hat{\mathbf{t}}^{-1}\right]^{-1} \left(\mathbf{y}^{N}\right)^{bp} \qquad \text{by (A.1)} \\ \left(\mathbf{p}^{N}\right)^{bp} &= \left(\mathbf{I} - \hat{\mathbf{t}} \, \mathbf{QS} \, \hat{\mathbf{t}}^{-1}\right)^{-1} \left(\mathbf{y}^{N}\right)^{bp} \\ \left(\mathbf{p}^{N}\right)^{bp} &= \left[\mathbf{I} - \left(\mathbf{Q}^{N}\right)^{bp} \mathbf{S}^{N}\right]^{-1} \left(\mathbf{y}^{N}\right)^{bp} \qquad \text{by (A.1) and (A.3)} \end{split}$$



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On the other hand, remark that the symmetric model is not based on  $(U^N)^{bp}$ , as this is a product--by-industry matrix. Let  $(Z^N)^{bp}$  denote instead the intermediate consumption matrix of the

symmetric product-by-product domestic-flow table (at basic prices). This matrix includes the products needed for the production of each product. Making use of the ITA assumption,  $(\mathbb{Z}^N)^{bp}$  can be computed by the equation:

$$\left(\mathbf{Z}^{N}\right)^{bp} = \left(\mathbf{Q}^{N}\right)^{bp} \mathbf{V}^{bp}$$
(A.5)

The corresponding «technical» coefficients matrix is:

$$\mathbf{A}^{N} = \left(\mathbf{Z}^{N}\right)^{bp} \left[\left(\hat{\mathbf{p}}^{N}\right)^{bp}\right]^{-1}$$

$$\mathbf{A}^{N} = \left(\mathbf{Q}^{N}\right)^{bp} \mathbf{V}^{bp} \left[\left(\hat{\mathbf{p}}^{N}\right)^{bp}\right]^{-1} = \left(\mathbf{Q}^{N}\right)^{bp} \mathbf{S}^{N} \quad \text{by (A.5) and (A.3), so}$$

$$\left(\hat{\mathbf{p}}^{N}\right)^{bp} = \left(\mathbf{I} - \mathbf{A}^{N}\right)^{-1} \left(\mathbf{y}^{N}\right)^{bp} \implies \left(\mathbf{p}^{N}\right)^{bp} = \left[\mathbf{I} - \left(\mathbf{Q}^{N}\right)^{bp} \mathbf{S}^{N}\right]^{-1} \left(\mathbf{y}^{N}\right)^{bp}$$
which is the same than the outcome of (A.4).

which is the same than the outcome of (A.4).

Concerning now the industry-by-industry case, the symmetric domestic-flow ITA-based table (at basic prices) comprises an intermediate consumption matrix  $(\mathbb{Z}_{I}^{N})^{bp}$  derived as follows:

$$\begin{split} & \left(\mathbf{Z}_{I}^{N}\right)^{bp} = \mathbf{S}^{N}\left(\mathbf{U}^{N}\right)^{bp}, \quad \text{so} \\ & \left(\mathbf{Z}_{I}^{N}\right)^{bp}\left(\hat{\mathbf{g}}^{bp}\right)^{-1} = \mathbf{S}^{N}\left(\mathbf{U}^{N}\right)^{bp}\left(\hat{\mathbf{g}}^{bp}\right)^{-1} \qquad \text{and} \\ & \mathbf{A}_{I}^{N} = \mathbf{S}^{N}\left(\mathbf{Q}^{N}\right)^{bp} \Rightarrow \left(\mathbf{I} - \mathbf{A}_{I}^{N}\right)^{-1} = (\mathbf{I} - \mathbf{S}^{N}\left(\mathbf{Q}^{N}\right)^{bp})^{-1} \end{split}$$
(A.7)

It is straightforward that this is the same than the lower right-hand block in equation (6), displayed as well in our example in Annex A.1, as:

$$\mathbf{S}^{N} \left( \mathbf{Q}^{N} \right)^{bp} = \mathbf{S} \, \hat{\mathbf{t}}^{-1} \, \hat{\mathbf{t}} \, \mathbf{Q} = \mathbf{S} \mathbf{Q} \quad by (A.2) \text{ and } (A.3) \tag{A.8}$$